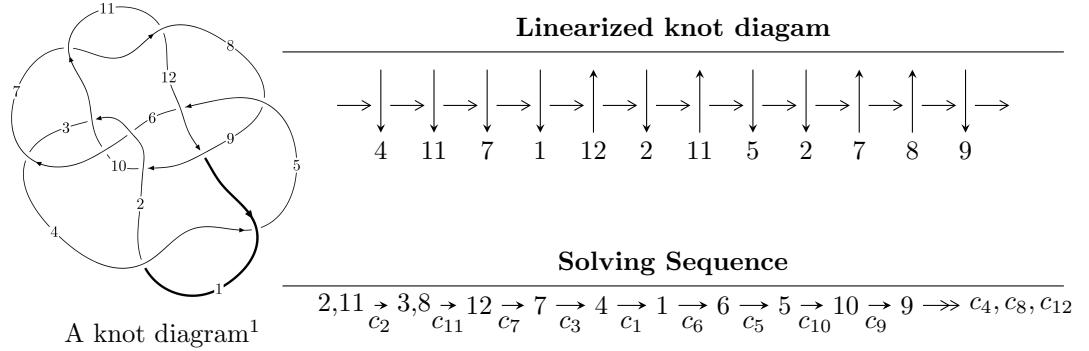


## $12n_{0737}$ ( $K12n_{0737}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle b + u, -5.39993 \times 10^{21}u^{20} - 1.73558 \times 10^{22}u^{19} + \dots + 2.47379 \times 10^{22}a - 8.83120 \times 10^{22}, u^{21} + 25u^{19} + \dots + u + 1 \rangle$$

$$I_2^u = \langle b + u, -3035105u^{12} + 837784u^{11} + \dots + 1269257a - 4665416, u^{13} + 4u^{11} - 3u^{10} - 14u^9 + 14u^8 + 30u^7 - 27u^6 - 9u^5 + 24u^4 - u^3 - 6u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle -4.67268 \times 10^{23}u^{17} - 1.17012 \times 10^{24}u^{16} + \dots + 4.11076 \times 10^{26}b - 4.67615 \times 10^{26}, 9.23360 \times 10^{24}u^{17} + 3.69267 \times 10^{25}u^{16} + \dots + 1.05852 \times 10^{28}a + 1.11492 \times 10^{28}, u^{18} + u^{17} + \dots + 512u + 206 \rangle$$

$$I_4^u = \langle b - 1, 2a - u + 2, u^2 - 2u + 2 \rangle$$

$$I_5^u = \langle b^2 + 2b + 2, a - 1, u + 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 56 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b + u, -5.40 \times 10^{21}u^{20} - 1.74 \times 10^{22}u^{19} + \cdots + 2.47 \times 10^{22}a - 8.83 \times 10^{22}, u^{21} + 25u^{19} + \cdots + u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.218285u^{20} + 0.701585u^{19} + \cdots + 4.16608u + 3.56990 \\ -u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.0236086u^{20} - 0.454671u^{19} + \cdots - 3.43605u - 1.12582 \\ -0.0461919u^{20} + 0.0773359u^{19} + \cdots + 1.91987u + 0.701585 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.218285u^{20} + 0.701585u^{19} + \cdots + 4.16608u + 3.56990 \\ 0.0461919u^{20} - 0.0773359u^{19} + \cdots - 1.91987u - 0.701585 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.701585u^{20} - 0.0461919u^{19} + \cdots - 3.35162u + 1.21829 \\ 0.0773359u^{20} - 0.0368722u^{19} + \cdots + 0.747777u + 0.0461919 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.344227u^{20} + 0.127290u^{19} + \cdots - 2.85190u + 0.707526 \\ 0.00198645u^{20} - 0.161647u^{19} + \cdots + 0.257401u - 0.164162 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.264477u^{20} + 0.624249u^{19} + \cdots + 2.24621u + 2.86832 \\ 0.0461919u^{20} - 0.0773359u^{19} + \cdots - 1.91987u - 0.701585 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.875790u^{20} + 0.451552u^{19} + \cdots - 5.00872u + 1.53539 \\ 0.266657u^{20} - 0.0156100u^{19} + \cdots + 0.224114u - 0.576327 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.0236086u^{20} + 0.454671u^{19} + \cdots + 3.43605u + 1.12582 \\ 0.200090u^{20} - 0.189555u^{19} + \cdots - 0.398150u - 1.15626 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.223699u^{20} + 0.265116u^{19} + \cdots + 3.03790u - 0.0304368 \\ 0.200090u^{20} - 0.189555u^{19} + \cdots - 0.398150u - 1.15626 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

$$\text{(iii) Cusp Shapes} = -\frac{34018566246715620144259}{12368961610252189857652}u^{20} - \frac{4694223251017745076299}{12368961610252189857652}u^{19} + \cdots - \frac{153162225510311692592391}{6184480805126094928826}u - \frac{44380162749147865603681}{12368961610252189857652}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{21} - 8u^{20} + \cdots - 22u + 2$
$c_2, c_3$	$u^{21} + 25u^{19} + \cdots + u + 1$
$c_5$	$u^{21} - 19u^{20} + \cdots - 1856u + 256$
$c_6$	$u^{21} + u^{20} + \cdots + 5u + 2$
$c_7, c_{10}, c_{11}$	$u^{21} - 8u^{20} + \cdots - 26u + 10$
$c_8, c_{12}$	$u^{21} + u^{20} + \cdots + 6u + 1$
$c_9$	$u^{21} - u^{20} + \cdots + 66u + 76$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{21} + 16y^{20} + \cdots + 56y - 4$
$c_2, c_3$	$y^{21} + 50y^{20} + \cdots - 19y - 1$
$c_5$	$y^{21} - 7y^{20} + \cdots + 348160y - 65536$
$c_6$	$y^{21} + 43y^{20} + \cdots - 179y - 4$
$c_7, c_{10}, c_{11}$	$y^{21} - 32y^{20} + \cdots + 1776y - 100$
$c_8, c_{12}$	$y^{21} + 11y^{20} + \cdots + 38y - 1$
$c_9$	$y^{21} + 29y^{20} + \cdots + 6636y - 5776$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.591384 + 0.684501I$		
$a = 0.986086 - 0.952196I$	$2.90718 + 0.62164I$	$-0.21352 - 2.05306I$
$b = -0.591384 - 0.684501I$		
$u = 0.591384 - 0.684501I$		
$a = 0.986086 + 0.952196I$	$2.90718 - 0.62164I$	$-0.21352 + 2.05306I$
$b = -0.591384 + 0.684501I$		
$u = 0.633459 + 0.554243I$		
$a = 0.225131 - 0.559868I$	$3.13654 - 0.77238I$	$-1.08315 + 3.79652I$
$b = -0.633459 - 0.554243I$		
$u = 0.633459 - 0.554243I$		
$a = 0.225131 + 0.559868I$	$3.13654 + 0.77238I$	$-1.08315 - 3.79652I$
$b = -0.633459 + 0.554243I$		
$u = -0.411221 + 0.734008I$		
$a = -1.125200 - 0.068544I$	$3.06565 - 2.80817I$	$-0.13665 + 3.60000I$
$b = 0.411221 - 0.734008I$		
$u = -0.411221 - 0.734008I$		
$a = -1.125200 + 0.068544I$	$3.06565 + 2.80817I$	$-0.13665 - 3.60000I$
$b = 0.411221 + 0.734008I$		
$u = 0.433795 + 0.519955I$		
$a = -1.39067 + 1.14375I$	$8.38211 - 0.33360I$	$5.43964 + 0.18682I$
$b = -0.433795 - 0.519955I$		
$u = 0.433795 - 0.519955I$		
$a = -1.39067 - 1.14375I$	$8.38211 + 0.33360I$	$5.43964 - 0.18682I$
$b = -0.433795 + 0.519955I$		
$u = -0.449539 + 0.447984I$		
$a = 2.36305 + 0.92529I$	$9.25551 - 8.18754I$	$2.61786 + 4.84295I$
$b = 0.449539 - 0.447984I$		
$u = -0.449539 - 0.447984I$		
$a = 2.36305 - 0.92529I$	$9.25551 + 8.18754I$	$2.61786 - 4.84295I$
$b = 0.449539 + 0.447984I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.610649$		
$a = 0.463396$	-1.19744	-2.54880
$b = 0.610649$		
$u = 0.064145 + 0.480475I$		
$a = -0.97482 + 2.36314I$	$4.25500 + 4.70062I$	$0.78101 - 5.95257I$
$b = -0.064145 - 0.480475I$		
$u = 0.064145 - 0.480475I$		
$a = -0.97482 - 2.36314I$	$4.25500 - 4.70062I$	$0.78101 + 5.95257I$
$b = -0.064145 + 0.480475I$		
$u = -0.118660 + 0.375406I$		
$a = 1.27547 - 0.90971I$	$-0.104584 + 1.401550I$	$-1.22515 - 5.35896I$
$b = 0.118660 - 0.375406I$		
$u = -0.118660 - 0.375406I$		
$a = 1.27547 + 0.90971I$	$-0.104584 - 1.401550I$	$-1.22515 + 5.35896I$
$b = 0.118660 + 0.375406I$		
$u = -0.02275 + 2.82542I$		
$a = 0.063198 - 0.686482I$	$-17.8874 + 12.7180I$	0
$b = 0.02275 - 2.82542I$		
$u = -0.02275 - 2.82542I$		
$a = 0.063198 + 0.686482I$	$-17.8874 - 12.7180I$	0
$b = 0.02275 + 2.82542I$		
$u = -0.62719 + 2.81445I$		
$a = -0.180831 - 0.609250I$	$19.4705 - 1.7019I$	0
$b = 0.62719 - 2.81445I$		
$u = -0.62719 - 2.81445I$		
$a = -0.180831 + 0.609250I$	$19.4705 + 1.7019I$	0
$b = 0.62719 + 2.81445I$		
$u = 0.21191 + 2.98201I$		
$a = 0.026904 - 0.620788I$	$15.8213 - 6.2554I$	0
$b = -0.21191 - 2.98201I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.21191 - 2.98201I$		
$a = 0.026904 + 0.620788I$	$15.8213 + 6.2554I$	0
$b = -0.21191 + 2.98201I$		

$$\text{II. } I_2^u = \langle b + u, -3.04 \times 10^6 u^{12} + 8.38 \times 10^5 u^{11} + \dots + 1.27 \times 10^6 a - 4.67 \times 10^6, u^{13} + 4u^{11} + \dots + 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 2.39125u^{12} - 0.660059u^{11} + \dots - 9.61560u + 3.67571 \\ -u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -2.96162u^{12} + 1.00248u^{11} + \dots + 12.9399u - 5.17648 \\ -0.0312159u^{12} + 0.392917u^{11} + \dots + 2.07113u - 0.660059 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 2.39125u^{12} - 0.660059u^{11} + \dots - 9.61560u + 3.67571 \\ 0.0312159u^{12} - 0.392917u^{11} + \dots - 2.07113u + 0.660059 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.660059u^{12} - 0.0312159u^{11} + \dots + 1.10678u + 3.39125 \\ 0.392917u^{12} + 0.0508833u^{11} + \dots - 0.597627u + 0.0312159 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1.65839u^{12} - 0.257842u^{11} + \dots + 2.91119u + 0.964264 \\ -0.424133u^{12} + 0.342034u^{11} + \dots + 2.66876u + 0.308725 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 2.42246u^{12} - 1.05298u^{11} + \dots - 11.6867u + 4.33576 \\ 0.0312159u^{12} - 0.392917u^{11} + \dots - 2.07113u + 0.660059 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1.26999u^{12} - 1.05851u^{11} + \dots - 6.41247u + 2.32712 \\ 0.166291u^{12} - 0.668395u^{11} + \dots + 0.612283u + 1.34966 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 2.96162u^{12} - 1.00248u^{11} + \dots - 12.9399u + 5.17648 \\ -0.0266959u^{12} - 0.872552u^{11} + \dots - 1.02779u + 1.66254 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2.93493u^{12} - 1.87504u^{11} + \dots - 13.9677u + 6.83902 \\ -0.0266959u^{12} - 0.872552u^{11} + \dots - 1.02779u + 1.66254 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

$$(iii) \text{ Cusp Shapes} = -\frac{11098661}{1269257}u^{12} + \frac{5890928}{1269257}u^{11} + \dots + \frac{9880480}{1269257}u - \frac{16615848}{1269257}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{13} - 5u^{12} + \cdots + 27u - 4$
$c_2$	$u^{13} + 4u^{11} + \cdots + 2u + 1$
$c_3$	$u^{13} + 4u^{11} + \cdots + 2u - 1$
$c_4$	$u^{13} + 5u^{12} + \cdots + 27u + 4$
$c_5$	$u^{13} + 6u^{12} + \cdots + u - 1$
$c_6$	$u^{13} - u^{12} + \cdots - u + 1$
$c_7$	$u^{13} - 5u^{12} + \cdots + 3u + 2$
$c_8, c_{12}$	$u^{13} - u^{12} + u^{11} + u^{10} + 2u^9 - 3u^8 + u^7 + 3u^6 - u^5 - 2u^4 + 2u^3 - u - 1$
$c_9$	$u^{13} - u^{12} + 6u^{11} + u^{10} + 12u^9 + 10u^8 + 9u^7 + 7u^6 + 6u^4 + 3u^3 - 3u^2 + 1$
$c_{10}, c_{11}$	$u^{13} + 5u^{12} + \cdots + 3u - 2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{13} + 9y^{12} + \cdots + 97y - 16$
$c_2, c_3$	$y^{13} + 8y^{12} + \cdots + 16y - 1$
$c_5$	$y^{13} - 6y^{12} + \cdots + 7y - 1$
$c_6$	$y^{13} + 9y^{12} + \cdots + 11y - 1$
$c_7, c_{10}, c_{11}$	$y^{13} - 19y^{12} + \cdots - 11y - 4$
$c_8, c_{12}$	$y^{13} + y^{12} + \cdots + y - 1$
$c_9$	$y^{13} + 11y^{12} + \cdots + 6y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.584682 + 0.557508I$		
$a = 0.467799 + 0.459309I$	$1.87818 - 5.16888I$	$-5.45109 + 5.60438I$
$b = -0.584682 - 0.557508I$		
$u = 0.584682 - 0.557508I$		
$a = 0.467799 - 0.459309I$	$1.87818 + 5.16888I$	$-5.45109 - 5.60438I$
$b = -0.584682 + 0.557508I$		
$u = -0.646836 + 0.067688I$		
$a = 0.529126 - 0.404517I$	$-1.42512 - 0.47239I$	$-7.52545 + 9.55816I$
$b = 0.646836 - 0.067688I$		
$u = -0.646836 - 0.067688I$		
$a = 0.529126 + 0.404517I$	$-1.42512 + 0.47239I$	$-7.52545 - 9.55816I$
$b = 0.646836 + 0.067688I$		
$u = 0.498804 + 0.404257I$		
$a = -2.04698 + 0.60897I$	$6.09438 - 1.34909I$	$0.36538 + 1.86326I$
$b = -0.498804 - 0.404257I$		
$u = 0.498804 - 0.404257I$		
$a = -2.04698 - 0.60897I$	$6.09438 + 1.34909I$	$0.36538 - 1.86326I$
$b = -0.498804 + 0.404257I$		
$u = -1.254250 + 0.588394I$		
$a = -0.840675 - 0.538825I$	$6.40935 + 7.59409I$	$1.22194 - 5.34686I$
$b = 1.254250 - 0.588394I$		
$u = -1.254250 - 0.588394I$		
$a = -0.840675 + 0.538825I$	$6.40935 - 7.59409I$	$1.22194 + 5.34686I$
$b = 1.254250 + 0.588394I$		
$u = 1.245380 + 0.642473I$		
$a = 0.984992 - 0.368357I$	$4.54418 + 2.44460I$	$2.99018 - 2.95945I$
$b = -1.245380 - 0.642473I$		
$u = 1.245380 - 0.642473I$		
$a = 0.984992 + 0.368357I$	$4.54418 - 2.44460I$	$2.99018 + 2.95945I$
$b = -1.245380 + 0.642473I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.328910$		
$a = 4.07049$	1.84881	-6.67710
$b = 0.328910$		
$u = -0.26332 + 2.64930I$		
$a = -0.129510 - 0.704018I$	$17.7632 - 2.2039I$	$0.237574 + 0.419872I$
$b = 0.26332 - 2.64930I$		
$u = -0.26332 - 2.64930I$		
$a = -0.129510 + 0.704018I$	$17.7632 + 2.2039I$	$0.237574 - 0.419872I$
$b = 0.26332 + 2.64930I$		

$$\text{III. } I_3^u = \langle -4.67 \times 10^{23}u^{17} - 1.17 \times 10^{24}u^{16} + \dots + 4.11 \times 10^{26}b - 4.68 \times 10^{26}, 9.23 \times 10^{24}u^{17} + 3.69 \times 10^{25}u^{16} + \dots + 1.06 \times 10^{28}a + 1.11 \times 10^{28}, u^{18} + u^{17} + \dots + 512u + 206 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.000872310u^{17} - 0.00348851u^{16} + \dots - 0.911938u - 1.05328 \\ 0.00113669u^{17} + 0.00284649u^{16} + \dots + 0.0571899u + 1.13754 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.00619818u^{17} - 0.00659840u^{16} + \dots - 3.79065u - 2.55336 \\ -0.000735882u^{17} + 0.00238650u^{16} + \dots + 0.849826u + 0.901098 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.000872310u^{17} - 0.00348851u^{16} + \dots - 0.911938u - 1.05328 \\ 0.00337890u^{17} + 0.00352881u^{16} + \dots + 1.57638u + 1.67648 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.00437426u^{17} - 0.00511014u^{16} + \dots - 3.81879u - 1.38980 \\ 0.00392577u^{17} + 0.00295684u^{16} + \dots + 1.78231u + 1.86297 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.00326686u^{17} - 0.00265625u^{16} + \dots + 2.02077u - 1.22406 \\ -0.00672287u^{17} - 0.00269067u^{16} + \dots - 2.56234u - 1.01072 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.00250659u^{17} + 0.0000402959u^{16} + \dots + 0.664442u + 0.623194 \\ 0.00337890u^{17} + 0.00352881u^{16} + \dots + 1.57638u + 1.67648 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.00870477u^{17} + 0.00663870u^{16} + \dots + 4.45509u + 3.17656 \\ 0.00411478u^{17} + 0.00114230u^{16} + \dots + 0.726555u + 0.775377 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.00619818u^{17} + 0.00659840u^{16} + \dots + 3.79065u + 2.55336 \\ -0.00116233u^{17} - 0.00210654u^{16} + \dots - 0.331565u - 0.983544 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.00503585u^{17} + 0.00449186u^{16} + \dots + 3.45908u + 1.56982 \\ -0.00116233u^{17} - 0.00210654u^{16} + \dots - 0.331565u - 0.983544 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{2356314796722538609456367}{205538248502201329427999196}u^{17} - \frac{197356226700656101872041}{102769124251100664713999598}u^{16} + \dots - \frac{644603608722482183906910875}{102769124251100664713999598}u + \frac{7790438242139030196174041}{102769124251100664713999598}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$(u^9 + u^8 + 5u^7 + 4u^6 + 8u^5 + 5u^4 + 2u^3 + u^2 - 4u - 1)^2$
$c_2, c_3$	$u^{18} + u^{17} + \dots + 512u + 206$
$c_5$	$(u + 1)^{18}$
$c_6$	$u^{18} - u^{17} + \dots - 532u + 401$
$c_7, c_{10}, c_{11}$	$(u^9 + 3u^8 - 3u^7 - 12u^6 + 6u^5 + 21u^4 - 2u^3 - 11u^2 - 6u - 1)^2$
$c_8, c_{12}$	$u^{18} + 3u^{17} + \dots + 8u + 2$
$c_9$	$u^{18} - u^{17} + \dots + 3168u + 1504$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^9 + 9y^8 + 33y^7 + 58y^6 + 34y^5 - 39y^4 - 62y^3 - 7y^2 + 18y - 1)^2$
$c_2, c_3$	$y^{18} + 37y^{17} + \cdots - 103112y + 42436$
$c_5$	$(y - 1)^{18}$
$c_6$	$y^{18} + 39y^{17} + \cdots + 109154y + 160801$
$c_7, c_{10}, c_{11}$	$(y^9 - 15y^8 + \cdots + 14y - 1)^2$
$c_8, c_{12}$	$y^{18} + y^{17} + \cdots + 72y + 4$
$c_9$	$y^{18} + 25y^{17} + \cdots - 7100416y + 2262016$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.886434 + 0.371388I$		
$a = 1.096950 - 0.459588I$	3.15999	$-1.78243 + 0.I$
$b = -0.886434 + 0.371388I$		
$u = 0.886434 - 0.371388I$		
$a = 1.096950 + 0.459588I$	3.15999	$-1.78243 + 0.I$
$b = -0.886434 - 0.371388I$		
$u = 0.205642 + 0.879714I$		
$a = 0.257101 + 0.425056I$	2.95021 + 4.83805I	$3.38372 - 2.81539I$
$b = -1.095690 + 0.759227I$		
$u = 0.205642 - 0.879714I$		
$a = 0.257101 - 0.425056I$	2.95021 - 4.83805I	$3.38372 + 2.81539I$
$b = -1.095690 - 0.759227I$		
$u = -0.653145 + 0.189006I$		
$a = 0.414794 + 0.120032I$	-1.18935	$-6 - 0.171800 + 0.10I$
$b = 0.653145 + 0.189006I$		
$u = -0.653145 - 0.189006I$		
$a = 0.414794 - 0.120032I$	-1.18935	$-6 - 0.171800 + 0.10I$
$b = 0.653145 - 0.189006I$		
$u = 1.095690 + 0.759227I$		
$a = -0.331949 - 0.056184I$	2.95021 - 4.83805I	$3.38372 + 2.81539I$
$b = -0.205642 + 0.879714I$		
$u = 1.095690 - 0.759227I$		
$a = -0.331949 + 0.056184I$	2.95021 + 4.83805I	$3.38372 - 2.81539I$
$b = -0.205642 - 0.879714I$		
$u = -0.419711 + 0.477941I$		
$a = -0.60540 - 2.16213I$	7.78134 - 1.20594I	$6.24179 + 1.20422I$
$b = 1.40135 + 0.64766I$		
$u = -0.419711 - 0.477941I$		
$a = -0.60540 + 2.16213I$	7.78134 + 1.20594I	$6.24179 - 1.20422I$
$b = 1.40135 - 0.64766I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.40135 + 0.64766I$		
$a = -0.925008 + 0.013582I$	$7.78134 + 1.20594I$	$6.24179 - 1.20422I$
$b = 0.419711 + 0.477941I$		
$u = -1.40135 - 0.64766I$		
$a = -0.925008 - 0.013582I$	$7.78134 - 1.20594I$	$6.24179 + 1.20422I$
$b = 0.419711 - 0.477941I$		
$u = -0.22580 + 2.48577I$		
$a = 0.159711 + 0.767946I$	$19.3983 - 3.3753I$	$4.74375 + 2.72891I$
$b = 0.15187 + 2.78180I$		
$u = -0.22580 - 2.48577I$		
$a = 0.159711 - 0.767946I$	$19.3983 + 3.3753I$	$4.74375 - 2.72891I$
$b = 0.15187 - 2.78180I$		
$u = 0.16411 + 2.66586I$		
$a = -0.043531 + 0.707136I$	15.0815	$-6 - 0.784284 + 0.10I$
$b = -0.16411 + 2.66586I$		
$u = 0.16411 - 2.66586I$		
$a = -0.043531 - 0.707136I$	15.0815	$-6 - 0.784284 + 0.10I$
$b = -0.16411 - 2.66586I$		
$u = -0.15187 + 2.78180I$		
$a = -0.042083 + 0.701486I$	$19.3983 + 3.3753I$	$4.74375 - 2.72891I$
$b = 0.22580 + 2.48577I$		
$u = -0.15187 - 2.78180I$		
$a = -0.042083 - 0.701486I$	$19.3983 - 3.3753I$	$4.74375 + 2.72891I$
$b = 0.22580 - 2.48577I$		

$$\text{IV. } I_4^u = \langle b - 1, 2a - u + 2, u^2 - 2u + 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 2u - 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} \frac{1}{2}u - 1 \\ 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -\frac{1}{2}u + 1 \\ u - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{1}{2}u - 1 \\ -u + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{1}{2}u \\ u - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -\frac{1}{2}u + 2 \\ 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{1}{2}u \\ -u + 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u + 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{1}{2}u - 1 \\ 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} \frac{1}{2}u \\ 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_6$ $c_8$	$u^2 + 1$
$c_2, c_{12}$	$u^2 - 2u + 2$
$c_3, c_5, c_{10}$ $c_{11}$	$(u - 1)^2$
$c_7, c_9$	$(u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_6$ $c_8$	$(y + 1)^2$
$c_2, c_{12}$	$y^2 + 4$
$c_3, c_5, c_7$ $c_9, c_{10}, c_{11}$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000 + 1.00000I$		
$a = -0.500000 + 0.500000I$	4.93480	4.00000
$b = 1.00000$		
$u = 1.00000 - 1.00000I$		
$a = -0.500000 - 0.500000I$	4.93480	4.00000
$b = 1.00000$		

$$\mathbf{V. } I_5^u = \langle b^2 + 2b + 2, a - 1, u + 1 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -b - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ b + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} b + 1 \\ -b - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b + 2 \\ b + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} b + 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

$$a_9 = \begin{pmatrix} b + 1 \\ b \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes = 4**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_6$ $c_{12}$	$u^2 + 1$
$c_2, c_7$	$(u + 1)^2$
$c_3$	$u^2 + 2u + 2$
$c_5, c_{10}, c_{11}$	$(u - 1)^2$
$c_8, c_9$	$u^2 - 2u + 2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_6$ $c_{12}$	$(y + 1)^2$
$c_2, c_5, c_7$ $c_{10}, c_{11}$	$(y - 1)^2$
$c_3, c_8, c_9$	$y^2 + 4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 1.00000$	4.93480	4.00000
$b = -1.00000 + 1.00000I$		
$u = -1.00000$		
$a = 1.00000$	4.93480	4.00000
$b = -1.00000 - 1.00000I$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 + 1)^2(u^9 + u^8 + 5u^7 + 4u^6 + 8u^5 + 5u^4 + 2u^3 + u^2 - 4u - 1)^2 \\ \cdot (u^{13} - 5u^{12} + \dots + 27u - 4)(u^{21} - 8u^{20} + \dots - 22u + 2)$
$c_2$	$((u + 1)^2)(u^2 - 2u + 2)(u^{13} + 4u^{11} + \dots + 2u + 1) \\ \cdot (u^{18} + u^{17} + \dots + 512u + 206)(u^{21} + 25u^{19} + \dots + u + 1)$
$c_3$	$((u - 1)^2)(u^2 + 2u + 2)(u^{13} + 4u^{11} + \dots + 2u - 1) \\ \cdot (u^{18} + u^{17} + \dots + 512u + 206)(u^{21} + 25u^{19} + \dots + u + 1)$
$c_4$	$(u^2 + 1)^2(u^9 + u^8 + 5u^7 + 4u^6 + 8u^5 + 5u^4 + 2u^3 + u^2 - 4u - 1)^2 \\ \cdot (u^{13} + 5u^{12} + \dots + 27u + 4)(u^{21} - 8u^{20} + \dots - 22u + 2)$
$c_5$	$((u - 1)^4)(u + 1)^{18}(u^{13} + 6u^{12} + \dots + u - 1) \\ \cdot (u^{21} - 19u^{20} + \dots - 1856u + 256)$
$c_6$	$((u^2 + 1)^2)(u^{13} - u^{12} + \dots - u + 1)(u^{18} - u^{17} + \dots - 532u + 401) \\ \cdot (u^{21} + u^{20} + \dots + 5u + 2)$
$c_7$	$(u + 1)^4 \\ \cdot (u^9 + 3u^8 - 3u^7 - 12u^6 + 6u^5 + 21u^4 - 2u^3 - 11u^2 - 6u - 1)^2 \\ \cdot (u^{13} - 5u^{12} + \dots + 3u + 2)(u^{21} - 8u^{20} + \dots - 26u + 10)$
$c_8, c_{12}$	$(u^2 + 1)(u^2 - 2u + 2) \\ \cdot (u^{13} - u^{12} + u^{11} + u^{10} + 2u^9 - 3u^8 + u^7 + 3u^6 - u^5 - 2u^4 + 2u^3 - u - 1) \\ \cdot (u^{18} + 3u^{17} + \dots + 8u + 2)(u^{21} + u^{20} + \dots + 6u + 1)$
$c_9$	$(u + 1)^2(u^2 - 2u + 2) \\ \cdot (u^{13} - u^{12} + 6u^{11} + u^{10} + 12u^9 + 10u^8 + 9u^7 + 7u^6 + 6u^4 + 3u^3 - 3u^2 + 1) \\ \cdot (u^{18} - u^{17} + \dots + 3168u + 1504)(u^{21} - u^{20} + \dots + 66u + 76)$
$c_{10}, c_{11}$	$(u - 1)^4 \\ \cdot (u^9 + 3u^8 - 3u^7 - 12u^6 + 6u^5 + 21u^4 - 2u^3 - 11u^2 - 6u - 1)^2 \\ \cdot (u^{13} + 5u^{12} + \dots + 3u - 2)(u^{21} - 8u^{20} + \dots - 26u + 10)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y+1)^4$ $\cdot (y^9 + 9y^8 + 33y^7 + 58y^6 + 34y^5 - 39y^4 - 62y^3 - 7y^2 + 18y - 1)^2$ $\cdot (y^{13} + 9y^{12} + \dots + 97y - 16)(y^{21} + 16y^{20} + \dots + 56y - 4)$
$c_2, c_3$	$((y-1)^2)(y^2 + 4)(y^{13} + 8y^{12} + \dots + 16y - 1)$ $\cdot (y^{18} + 37y^{17} + \dots - 103112y + 42436)(y^{21} + 50y^{20} + \dots - 19y - 1)$
$c_5$	$((y-1)^{22})(y^{13} - 6y^{12} + \dots + 7y - 1)$ $\cdot (y^{21} - 7y^{20} + \dots + 348160y - 65536)$
$c_6$	$((y+1)^4)(y^{13} + 9y^{12} + \dots + 11y - 1)$ $\cdot (y^{18} + 39y^{17} + \dots + 109154y + 160801)$ $\cdot (y^{21} + 43y^{20} + \dots - 179y - 4)$
$c_7, c_{10}, c_{11}$	$((y-1)^4)(y^9 - 15y^8 + \dots + 14y - 1)^2(y^{13} - 19y^{12} + \dots - 11y - 4)$ $\cdot (y^{21} - 32y^{20} + \dots + 1776y - 100)$
$c_8, c_{12}$	$((y+1)^2)(y^2 + 4)(y^{13} + y^{12} + \dots + y - 1)(y^{18} + y^{17} + \dots + 72y + 4)$ $\cdot (y^{21} + 11y^{20} + \dots + 38y - 1)$
$c_9$	$((y-1)^2)(y^2 + 4)(y^{13} + 11y^{12} + \dots + 6y - 1)$ $\cdot (y^{18} + 25y^{17} + \dots - 7100416y + 2262016)$ $\cdot (y^{21} + 29y^{20} + \dots + 6636y - 5776)$