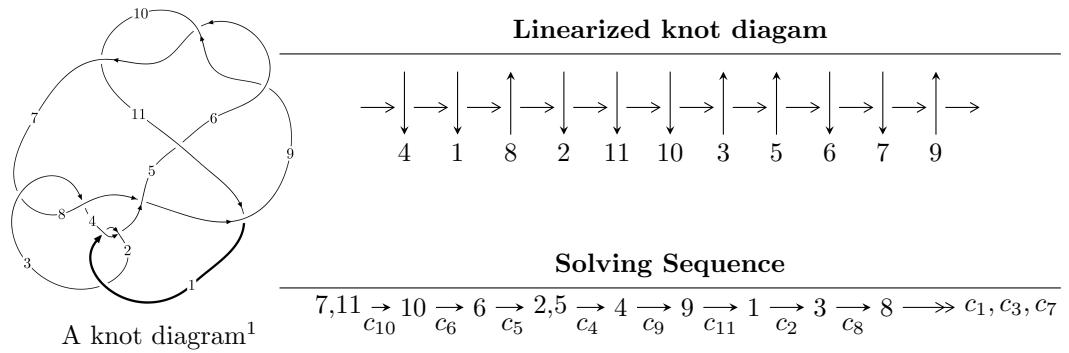


$$\frac{11a_{34}}{(K11a_{34})}$$



## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -u^{63} - u^{62} + \cdots + b - u, u^{39} - 18u^{37} + \cdots - 2u^2 + a, u^{64} + 2u^{63} + \cdots + u - 1 \rangle$$

$$I_2^u = \langle b - 1, -u^3 + a + 2u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 69 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{63} - u^{62} + \cdots + b - u, \ u^{39} - 18u^{37} + \cdots - 2u^2 + a, \ u^{64} + 2u^{63} + \cdots + u - 1 \rangle^{\text{I.}}$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{39} + 18u^{37} + \cdots + 6u^3 + 2u^2 \\ u^{63} + u^{62} + \cdots + u^2 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{63} + u^{62} + \cdots - u^2 + 2u \\ -u^{63} - u^{62} + \cdots - u^3 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ -u^8 + 4u^6 - 4u^4 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{63} + u^{62} + \cdots - u - 1 \\ u^{63} + u^{62} + \cdots + u^3 + 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{10} + 5u^8 - 8u^6 + 3u^4 + u^2 + 1 \\ -u^{10} + 4u^8 - 5u^6 + 2u^4 - u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{10} + 5u^8 - 8u^6 + 3u^4 + u^2 + 1 \\ -u^{10} + 4u^8 - 5u^6 + 2u^4 - u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-6u^{63} - 4u^{62} + \cdots - 13u + 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{64} - 6u^{63} + \cdots + 3u - 1$
$c_2$	$u^{64} + 30u^{63} + \cdots + 3u + 1$
$c_3, c_7$	$u^{64} + u^{63} + \cdots + 96u + 32$
$c_5$	$u^{64} - 6u^{63} + \cdots + 5u - 1$
$c_6, c_9, c_{10}$	$u^{64} + 2u^{63} + \cdots + u - 1$
$c_8$	$u^{64} - 2u^{63} + \cdots + 8204u - 1960$
$c_{11}$	$u^{64} + 14u^{63} + \cdots + 2787u + 207$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{64} - 30y^{63} + \cdots - 3y + 1$
$c_2$	$y^{64} + 14y^{63} + \cdots + 13y + 1$
$c_3, c_7$	$y^{64} - 33y^{63} + \cdots - 14848y + 1024$
$c_5$	$y^{64} - 2y^{63} + \cdots - 9y + 1$
$c_6, c_9, c_{10}$	$y^{64} - 58y^{63} + \cdots - y + 1$
$c_8$	$y^{64} - 18y^{63} + \cdots - 40328176y + 3841600$
$c_{11}$	$y^{64} + 18y^{63} + \cdots + 1021851y + 42849$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.004890 + 0.212052I$		
$a = 0.250176 - 1.256930I$	$3.37131 - 1.86053I$	0
$b = -0.972468 + 0.330740I$		
$u = 1.004890 - 0.212052I$		
$a = 0.250176 + 1.256930I$	$3.37131 + 1.86053I$	0
$b = -0.972468 - 0.330740I$		
$u = -1.055590 + 0.097412I$		
$a = 0.83771 - 1.53205I$	$-1.58334 + 2.05666I$	0
$b = -0.452362 + 0.922072I$		
$u = -1.055590 - 0.097412I$		
$a = 0.83771 + 1.53205I$	$-1.58334 - 2.05666I$	0
$b = -0.452362 - 0.922072I$		
$u = 1.08657$		
$a = 0.517514$	$-2.98700$	0
$b = 1.28011$		
$u = 1.076070 + 0.243448I$		
$a = 0.50549 + 1.44435I$	$1.75966 - 7.47908I$	0
$b = 0.069484 - 0.831677I$		
$u = 1.076070 - 0.243448I$		
$a = 0.50549 - 1.44435I$	$1.75966 + 7.47908I$	0
$b = 0.069484 + 0.831677I$		
$u = 0.292951 + 0.725218I$		
$a = -3.13866 + 0.47208I$	$2.46662 - 11.29940I$	$-1.16462 + 9.08913I$
$b = -2.45175 + 0.82611I$		
$u = 0.292951 - 0.725218I$		
$a = -3.13866 - 0.47208I$	$2.46662 + 11.29940I$	$-1.16462 - 9.08913I$
$b = -2.45175 - 0.82611I$		
$u = 0.674453 + 0.386464I$		
$a = -0.00066 - 2.55544I$	$1.05339 + 7.31803I$	$-3.59936 - 4.11166I$
$b = -1.110180 - 0.550037I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.674453 - 0.386464I$		
$a = -0.00066 + 2.55544I$	$1.05339 - 7.31803I$	$-3.59936 + 4.11166I$
$b = -1.110180 + 0.550037I$		
$u = 0.705088 + 0.302401I$		
$a = 0.83956 + 1.15317I$	$3.02952 + 1.83201I$	$-0.533486 + 0.085386I$
$b = 0.077388 - 0.254328I$		
$u = 0.705088 - 0.302401I$		
$a = 0.83956 - 1.15317I$	$3.02952 - 1.83201I$	$-0.533486 - 0.085386I$
$b = 0.077388 + 0.254328I$		
$u = 0.265999 + 0.717941I$		
$a = 1.40926 + 0.47850I$	$4.64833 - 5.64259I$	$2.08406 + 5.05177I$
$b = 1.178360 + 0.621823I$		
$u = 0.265999 - 0.717941I$		
$a = 1.40926 - 0.47850I$	$4.64833 + 5.64259I$	$2.08406 - 5.05177I$
$b = 1.178360 - 0.621823I$		
$u = -0.268310 + 0.684190I$		
$a = -3.11925 - 1.34879I$	$-0.18871 + 5.19299I$	$-2.32409 - 6.82469I$
$b = -2.29400 - 1.31119I$		
$u = -0.268310 - 0.684190I$		
$a = -3.11925 + 1.34879I$	$-0.18871 - 5.19299I$	$-2.32409 + 6.82469I$
$b = -2.29400 + 1.31119I$		
$u = 0.166461 + 0.708672I$		
$a = -1.78632 + 0.78559I$	$5.88443 - 1.71228I$	$4.06856 + 3.31380I$
$b = -1.57846 + 0.71331I$		
$u = 0.166461 - 0.708672I$		
$a = -1.78632 - 0.78559I$	$5.88443 + 1.71228I$	$4.06856 - 3.31380I$
$b = -1.57846 - 0.71331I$		
$u = -1.27342$		
$a = 0.512497$	$-2.82174$	$0$
$b = -0.111947$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.379910 + 0.618311I$		
$a = 0.888593 - 0.950785I$	$-1.309430 + 0.220190I$	$-2.16669 + 0.94520I$
$b = 0.785579 + 0.082329I$		
$u = -0.379910 - 0.618311I$		
$a = 0.888593 + 0.950785I$	$-1.309430 - 0.220190I$	$-2.16669 - 0.94520I$
$b = 0.785579 - 0.082329I$		
$u = 0.116871 + 0.709884I$		
$a = 1.79401 - 0.11144I$	$4.64291 + 3.88634I$	$2.43594 - 2.51707I$
$b = 1.312960 + 0.524885I$		
$u = 0.116871 - 0.709884I$		
$a = 1.79401 + 0.11144I$	$4.64291 - 3.88634I$	$2.43594 + 2.51707I$
$b = 1.312960 - 0.524885I$		
$u = -0.460178 + 0.533945I$		
$a = 0.637038 - 0.795810I$	$-1.65255 + 3.56868I$	$-3.94595 - 7.64427I$
$b = 1.111230 - 0.236500I$		
$u = -0.460178 - 0.533945I$		
$a = 0.637038 + 0.795810I$	$-1.65255 - 3.56868I$	$-3.94595 + 7.64427I$
$b = 1.111230 + 0.236500I$		
$u = 0.259055 + 0.653388I$		
$a = 1.06464 + 0.97600I$	$-1.20405 - 2.76775I$	$-0.87874 + 6.15771I$
$b = 0.990905 - 0.182467I$		
$u = 0.259055 - 0.653388I$		
$a = 1.06464 - 0.97600I$	$-1.20405 + 2.76775I$	$-0.87874 - 6.15771I$
$b = 0.990905 + 0.182467I$		
$u = -0.204298 + 0.641678I$		
$a = 2.07861 - 0.64563I$	$0.748257 + 0.939190I$	$0.11212 - 1.46039I$
$b = 1.34976 - 0.78269I$		
$u = -0.204298 - 0.641678I$		
$a = 2.07861 + 0.64563I$	$0.748257 - 0.939190I$	$0.11212 + 1.46039I$
$b = 1.34976 + 0.78269I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.319680 + 0.270463I$		
$a = 0.628923 - 0.555572I$	$0.150980 - 0.347116I$	0
$b = 2.00427 + 0.11792I$		
$u = -1.319680 - 0.270463I$		
$a = 0.628923 + 0.555572I$	$0.150980 + 0.347116I$	0
$b = 2.00427 - 0.11792I$		
$u = -1.353850 + 0.278392I$		
$a = -0.922498 + 0.572074I$	$1.08775 + 5.28117I$	0
$b = -1.59733 - 1.65323I$		
$u = -1.353850 - 0.278392I$		
$a = -0.922498 - 0.572074I$	$1.08775 - 5.28117I$	0
$b = -1.59733 + 1.65323I$		
$u = -0.556271 + 0.257738I$		
$a = 1.06140 + 2.71158I$	$-1.60289 - 1.70495I$	$-6.10429 + 1.65168I$
$b = -0.484179 + 0.678880I$		
$u = -0.556271 - 0.257738I$		
$a = 1.06140 - 2.71158I$	$-1.60289 + 1.70495I$	$-6.10429 - 1.65168I$
$b = -0.484179 - 0.678880I$		
$u = 1.387450 + 0.186851I$		
$a = -0.335032 + 0.455289I$	$-5.22435 - 3.56448I$	0
$b = 0.124901 + 1.401000I$		
$u = 1.387450 - 0.186851I$		
$a = -0.335032 - 0.455289I$	$-5.22435 + 3.56448I$	0
$b = 0.124901 - 1.401000I$		
$u = 1.384430 + 0.250118I$		
$a = 0.470700 + 0.975593I$	$-4.32280 - 4.18388I$	0
$b = 2.41332 + 0.37758I$		
$u = 1.384430 - 0.250118I$		
$a = 0.470700 - 0.975593I$	$-4.32280 + 4.18388I$	0
$b = 2.41332 - 0.37758I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.410150 + 0.091621I$	$-3.31779 - 0.73149I$	0
$a = 0.171722 - 0.446103I$		
$b = -0.051337 - 0.869147I$		
$u = -1.410150 - 0.091621I$	$-3.31779 + 0.73149I$	0
$a = 0.171722 + 0.446103I$		
$b = -0.051337 + 0.869147I$		
$u = -1.404660 + 0.156512I$	$-7.96725 + 2.25757I$	0
$a = -0.481712 - 0.823798I$		
$b = 1.44039 + 0.27511I$		
$u = -1.404660 - 0.156512I$	$-7.96725 - 2.25757I$	0
$a = -0.481712 + 0.823798I$		
$b = 1.44039 - 0.27511I$		
$u = 1.407530 + 0.132731I$	$-7.47816 + 0.17720I$	0
$a = 1.36353 - 0.57844I$		
$b = 0.66427 - 2.25478I$		
$u = 1.407530 - 0.132731I$	$-7.47816 - 0.17720I$	0
$a = 1.36353 + 0.57844I$		
$b = 0.66427 + 2.25478I$		
$u = -1.40289 + 0.25793I$	$-6.51086 + 6.10114I$	0
$a = -0.099708 - 0.974841I$		
$b = 0.717554 + 0.201107I$		
$u = -1.40289 - 0.25793I$	$-6.51086 - 6.10114I$	0
$a = -0.099708 + 0.974841I$		
$b = 0.717554 - 0.201107I$		
$u = 1.40734 + 0.26932I$	$-5.53651 - 8.66838I$	0
$a = -1.68136 - 0.99882I$		
$b = -2.91941 + 2.36420I$		
$u = 1.40734 - 0.26932I$	$-5.53651 + 8.66838I$	0
$a = -1.68136 + 0.99882I$		
$b = -2.91941 - 2.36420I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.40814 + 0.28394I$		
$a = 0.280476 - 0.719527I$	$-0.68966 + 9.28326I$	0
$b = 1.97690 - 0.33914I$		
$u = -1.40814 - 0.28394I$		
$a = 0.280476 + 0.719527I$	$-0.68966 - 9.28326I$	0
$b = 1.97690 + 0.33914I$		
$u = -1.42115 + 0.28534I$		
$a = -1.34480 + 1.32214I$	$-3.0092 + 14.9742I$	0
$b = -3.09851 - 1.54301I$		
$u = -1.42115 - 0.28534I$		
$a = -1.34480 - 1.32214I$	$-3.0092 - 14.9742I$	0
$b = -3.09851 + 1.54301I$		
$u = -1.44601 + 0.10453I$		
$a = 0.955221 + 0.877194I$	$-5.55732 - 5.80431I$	0
$b = -0.16080 + 1.87965I$		
$u = -1.44601 - 0.10453I$		
$a = 0.955221 - 0.877194I$	$-5.55732 + 5.80431I$	0
$b = -0.16080 - 1.87965I$		
$u = 1.44004 + 0.23244I$		
$a = -0.095745 + 0.853500I$	$-7.13968 - 3.33308I$	0
$b = 0.714563 + 0.171726I$		
$u = 1.44004 - 0.23244I$		
$a = -0.095745 - 0.853500I$	$-7.13968 + 3.33308I$	0
$b = 0.714563 - 0.171726I$		
$u = 1.44782 + 0.18947I$		
$a = -0.258808 + 0.695694I$	$-7.74951 - 6.19199I$	0
$b = 1.43274 + 0.05713I$		
$u = 1.44782 - 0.18947I$		
$a = -0.258808 - 0.695694I$	$-7.74951 + 6.19199I$	0
$b = 1.43274 - 0.05713I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.234891 + 0.464221I$		
$a = 0.496892 - 0.920682I$	$-0.038168 + 1.118320I$	$-0.73760 - 6.33469I$
$b = 0.051241 - 0.444007I$		
$u = -0.234891 - 0.464221I$		
$a = 0.496892 + 0.920682I$	$-0.038168 - 1.118320I$	$-0.73760 + 6.33469I$
$b = 0.051241 + 0.444007I$		
$u = 0.382966 + 0.305636I$		
$a = 0.015592 + 1.148670I$	$-2.38212 - 0.33638I$	$-5.62748 - 1.67456I$
$b = 1.170900 + 0.079635I$		
$u = 0.382966 - 0.305636I$		
$a = 0.015592 - 1.148670I$	$-2.38212 + 0.33638I$	$-5.62748 + 1.67456I$
$b = 1.170900 - 0.079635I$		

$$\text{II. } I_2^u = \langle b - 1, -u^3 + a + 2u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 - 2u \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -u^3 + u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 - 2u \\ u^3 - u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -u^3 + u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $5u^3 - u^2 - 8u - 9$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^5$
$c_2, c_4$	$(u + 1)^5$
$c_3, c_7$	$u^5$
$c_5$	$u^5 - 3u^4 + 4u^3 - u^2 - u + 1$
$c_6$	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
$c_8, c_{11}$	$u^5 + u^4 + 2u^3 + u^2 + u + 1$
$c_9, c_{10}$	$u^5 - u^4 - 2u^3 + u^2 + u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^5$
$c_3, c_7$	$y^5$
$c_5$	$y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$
$c_6, c_9, c_{10}$	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$
$c_8, c_{11}$	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.21774$		
$a = 0.629714$	-4.04602	-9.76980
$b = 1.00000$		
$u = -0.309916 + 0.549911I$		
$a = 0.871221 - 1.107660I$	$-1.97403 + 1.53058I$	$-5.05737 - 4.09764I$
$b = 1.00000$		
$u = -0.309916 - 0.549911I$		
$a = 0.871221 + 1.107660I$	$-1.97403 - 1.53058I$	$-5.05737 + 4.09764I$
$b = 1.00000$		
$u = 1.41878 + 0.21917I$		
$a = -0.186078 + 0.874646I$	$-7.51750 - 4.40083I$	$-9.05774 + 4.18967I$
$b = 1.00000$		
$u = 1.41878 - 0.21917I$		
$a = -0.186078 - 0.874646I$	$-7.51750 + 4.40083I$	$-9.05774 - 4.18967I$
$b = 1.00000$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^5)(u^{64} - 6u^{63} + \dots + 3u - 1)$
$c_2$	$((u + 1)^5)(u^{64} + 30u^{63} + \dots + 3u + 1)$
$c_3, c_7$	$u^5(u^{64} + u^{63} + \dots + 96u + 32)$
$c_4$	$((u + 1)^5)(u^{64} - 6u^{63} + \dots + 3u - 1)$
$c_5$	$(u^5 - 3u^4 + 4u^3 - u^2 - u + 1)(u^{64} - 6u^{63} + \dots + 5u - 1)$
$c_6$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)(u^{64} + 2u^{63} + \dots + u - 1)$
$c_8$	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)(u^{64} - 2u^{63} + \dots + 8204u - 1960)$
$c_9, c_{10}$	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)(u^{64} + 2u^{63} + \dots + u - 1)$
$c_{11}$	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)(u^{64} + 14u^{63} + \dots + 2787u + 207)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y - 1)^5)(y^{64} - 30y^{63} + \cdots - 3y + 1)$
$c_2$	$((y - 1)^5)(y^{64} + 14y^{63} + \cdots + 13y + 1)$
$c_3, c_7$	$y^5(y^{64} - 33y^{63} + \cdots - 14848y + 1024)$
$c_5$	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)(y^{64} - 2y^{63} + \cdots - 9y + 1)$
$c_6, c_9, c_{10}$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)(y^{64} - 58y^{63} + \cdots - y + 1)$
$c_8$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1) \\ \cdot (y^{64} - 18y^{63} + \cdots - 40328176y + 3841600)$
$c_{11}$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)(y^{64} + 18y^{63} + \cdots + 1021851y + 42849)$