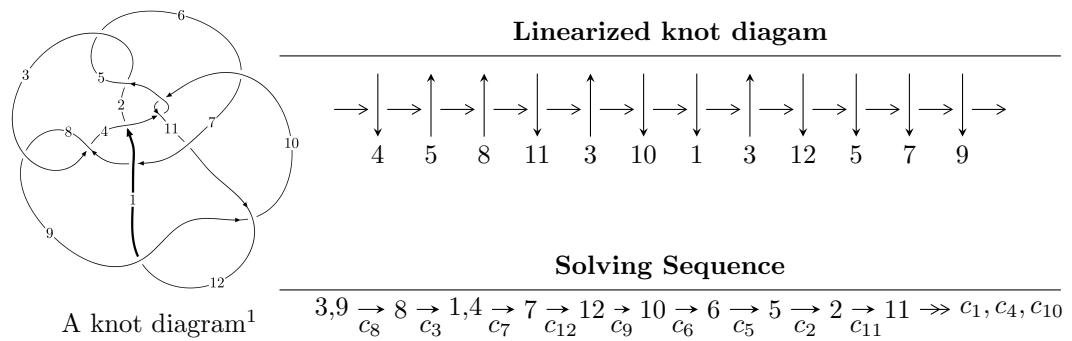


12n<sub>0757</sub> (K12n<sub>0757</sub>)



## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -1.59036 \times 10^{313} u^{84} + 4.77989 \times 10^{312} u^{83} + \dots + 6.91107 \times 10^{314} b + 1.33907 \times 10^{316}, \\ -9.31472 \times 10^{316} u^{84} + 5.83485 \times 10^{316} u^{83} + \dots + 8.06522 \times 10^{317} a + 1.67212 \times 10^{320}, \\ u^{85} + 27u^{83} + \dots + 4868u + 1167 \rangle$$

$$I_2^u = \langle -14825031610u^{27} + 18537500123u^{26} + \cdots + 6921637191b + 5273642732, \\ 305534977593367u^{27} - 790948509790679u^{26} + \cdots + 30157573241187a - 1297710378699701, \\ u^{28} - u^{27} + \cdots - u + 1 \rangle$$

$$I_3^u = \langle b - u, \ a + u - 1, \ u^2 - u + 1 \rangle$$

$$I_4^u = \langle b - u, \ a + u, \ u^2 - u + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 117 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILS/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.59 \times 10^{313}u^{84} + 4.78 \times 10^{312}u^{83} + \dots + 6.91 \times 10^{314}b + 1.34 \times 10^{316}, -9.31 \times 10^{316}u^{84} + 5.83 \times 10^{316}u^{83} + \dots + 8.07 \times 10^{317}a + 1.67 \times 10^{320}, u^{85} + 27u^{83} + \dots + 4868u + 1167 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.115492u^{84} - 0.0723458u^{83} + \dots - 355.666u - 207.324 \\ 0.0230118u^{84} - 0.00691628u^{83} + \dots - 20.4097u - 19.3757 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.110696u^{84} + 0.130681u^{83} + \dots + 956.188u + 362.084 \\ 0.0473216u^{84} + 0.0461518u^{83} + \dots + 828.691u + 175.587 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.138504u^{84} - 0.0792621u^{83} + \dots - 376.076u - 226.700 \\ 0.0230118u^{84} - 0.00691628u^{83} + \dots - 20.4097u - 19.3757 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.0884816u^{84} - 0.0814471u^{83} + \dots - 1489.39u - 309.371 \\ -0.0199738u^{84} - 0.0308531u^{83} + \dots - 502.451u - 116.544 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.0801281u^{84} + 0.0399526u^{83} + \dots + 844.648u + 163.284 \\ 0.0667657u^{84} - 0.00303016u^{83} + \dots + 340.400u + 24.5255 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.0801281u^{84} + 0.0399526u^{83} + \dots + 844.648u + 163.284 \\ 0.0299497u^{84} - 0.0114804u^{83} + \dots + 52.4010u - 22.0992 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.102164u^{84} - 0.0583120u^{83} + \dots - 240.005u - 161.556 \\ 0.0117585u^{84} + 0.00232467u^{83} + \dots + 42.4888u + 10.0149 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.00514215u^{84} + 0.0946688u^{83} + \dots + 1138.04u + 304.529 \\ 0.0345003u^{84} + 0.0325184u^{83} + \dots + 586.871u + 114.297 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $-0.274096u^{84} - 0.0366470u^{83} + \dots - 1775.76u - 145.097$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{85} - 5u^{84} + \cdots - 783263u - 43963$
$c_2, c_5$	$u^{85} + 4u^{84} + \cdots + 6399682u + 378351$
$c_3, c_8$	$u^{85} + 27u^{83} + \cdots + 4868u + 1167$
$c_4, c_{10}$	$u^{85} - 2u^{84} + \cdots - 32u + 3$
$c_6$	$u^{85} + 11u^{84} + \cdots - 284299729u + 28854207$
$c_7$	$u^{85} - 6u^{83} + \cdots - 4044u + 332$
$c_9, c_{12}$	$u^{85} + 25u^{83} + \cdots - 226u + 111$
$c_{11}$	$u^{85} - u^{84} + \cdots - 107u + 49$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{85} - 71y^{84} + \cdots + 1109768547995y - 1932745369$
$c_2, c_5$	$y^{85} + 72y^{84} + \cdots + 23176806835342y - 143149479201$
$c_3, c_8$	$y^{85} + 54y^{84} + \cdots - 53028158y - 1361889$
$c_4, c_{10}$	$y^{85} + 24y^{84} + \cdots - 356y - 9$
$c_6$	$y^{85} - 49y^{84} + \cdots + 24664681049291167y - 832565261598849$
$c_7$	$y^{85} - 12y^{84} + \cdots + 8779024y - 110224$
$c_9, c_{12}$	$y^{85} + 50y^{84} + \cdots - 318554y - 12321$
$c_{11}$	$y^{85} + 5y^{84} + \cdots - 31181y - 2401$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.365366 + 0.920085I$		
$a = 1.28702 + 0.96017I$	$0.646862 - 0.894793I$	0
$b = -0.282747 + 0.799096I$		
$u = 0.365366 - 0.920085I$		
$a = 1.28702 - 0.96017I$	$0.646862 + 0.894793I$	0
$b = -0.282747 - 0.799096I$		
$u = 0.069267 + 0.986380I$		
$a = -1.81713 - 0.02982I$	$0.965648 + 0.188556I$	0
$b = 1.341330 - 0.442065I$		
$u = 0.069267 - 0.986380I$		
$a = -1.81713 + 0.02982I$	$0.965648 - 0.188556I$	0
$b = 1.341330 + 0.442065I$		
$u = -0.378590 + 0.871699I$		
$a = 0.170281 - 0.692301I$	$-2.12817 + 0.68447I$	0
$b = -0.745974 + 0.566971I$		
$u = -0.378590 - 0.871699I$		
$a = 0.170281 + 0.692301I$	$-2.12817 - 0.68447I$	0
$b = -0.745974 - 0.566971I$		
$u = 0.493819 + 0.784435I$		
$a = -0.706323 - 0.663700I$	$-0.12800 + 1.91048I$	0
$b = 0.544809 + 0.424971I$		
$u = 0.493819 - 0.784435I$		
$a = -0.706323 + 0.663700I$	$-0.12800 - 1.91048I$	0
$b = 0.544809 - 0.424971I$		
$u = -1.033160 + 0.310486I$		
$a = 0.025290 - 0.798856I$	$-3.89476 - 5.62843I$	0
$b = 0.612443 - 0.384276I$		
$u = -1.033160 - 0.310486I$		
$a = 0.025290 + 0.798856I$	$-3.89476 + 5.62843I$	0
$b = 0.612443 + 0.384276I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.114713 + 1.085940I$		
$a = -0.043507 + 0.622927I$	$-1.59278 - 4.11572I$	0
$b = 0.13074 - 1.89360I$		
$u = -0.114713 - 1.085940I$		
$a = -0.043507 - 0.622927I$	$-1.59278 + 4.11572I$	0
$b = 0.13074 + 1.89360I$		
$u = 1.005930 + 0.438338I$		
$a = -0.310192 + 0.283012I$	$3.76571 - 0.51672I$	0
$b = 0.278082 + 1.100300I$		
$u = 1.005930 - 0.438338I$		
$a = -0.310192 - 0.283012I$	$3.76571 + 0.51672I$	0
$b = 0.278082 - 1.100300I$		
$u = -0.501285 + 0.690430I$		
$a = 1.51071 - 1.24410I$	$-1.08169 - 4.30528I$	0
$b = -0.572297 - 0.943715I$		
$u = -0.501285 - 0.690430I$		
$a = 1.51071 + 1.24410I$	$-1.08169 + 4.30528I$	0
$b = -0.572297 + 0.943715I$		
$u = 0.543325 + 1.010130I$		
$a = -1.64092 - 0.54557I$	$-0.04758 + 4.80218I$	0
$b = 0.256299 - 0.878934I$		
$u = 0.543325 - 1.010130I$		
$a = -1.64092 + 0.54557I$	$-0.04758 - 4.80218I$	0
$b = 0.256299 + 0.878934I$		
$u = 0.045240 + 1.153380I$		
$a = 1.40411 - 0.37311I$	$-4.84255 + 0.02543I$	0
$b = -0.472662 - 1.183120I$		
$u = 0.045240 - 1.153380I$		
$a = 1.40411 + 0.37311I$	$-4.84255 - 0.02543I$	0
$b = -0.472662 + 1.183120I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.353058 + 1.107940I$		
$a = 1.74143 + 0.17963I$	$-3.35900 - 6.17617I$	0
$b = -1.09518 - 1.44123I$		
$u = -0.353058 - 1.107940I$		
$a = 1.74143 - 0.17963I$	$-3.35900 + 6.17617I$	0
$b = -1.09518 + 1.44123I$		
$u = -0.028829 + 1.189170I$		
$a = 0.777609 - 0.632382I$	$-1.95596 + 1.77445I$	0
$b = -0.649162 + 0.964464I$		
$u = -0.028829 - 1.189170I$		
$a = 0.777609 + 0.632382I$	$-1.95596 - 1.77445I$	0
$b = -0.649162 - 0.964464I$		
$u = -0.541519 + 1.071560I$		
$a = 2.03935 - 0.00109I$	$1.33677 - 7.91613I$	0
$b = -0.443030 - 1.266400I$		
$u = -0.541519 - 1.071560I$		
$a = 2.03935 + 0.00109I$	$1.33677 + 7.91613I$	0
$b = -0.443030 + 1.266400I$		
$u = -0.677576 + 0.401202I$		
$a = 0.107097 + 0.653212I$	$3.26531 + 3.22906I$	0
$b = -0.287795 + 1.297880I$		
$u = -0.677576 - 0.401202I$		
$a = 0.107097 - 0.653212I$	$3.26531 - 3.22906I$	0
$b = -0.287795 - 1.297880I$		
$u = -0.534381 + 1.094250I$		
$a = 1.193530 - 0.604330I$	$-3.43230 - 3.81045I$	0
$b = -0.847656 - 0.422881I$		
$u = -0.534381 - 1.094250I$		
$a = 1.193530 + 0.604330I$	$-3.43230 + 3.81045I$	0
$b = -0.847656 + 0.422881I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.148250 + 1.246730I$		
$a = -1.46205 - 0.62108I$	$-5.66100 + 6.25301I$	0
$b = 0.397250 - 1.143730I$		
$u = 0.148250 - 1.246730I$		
$a = -1.46205 + 0.62108I$	$-5.66100 - 6.25301I$	0
$b = 0.397250 + 1.143730I$		
$u = 0.168747 + 1.299570I$		
$a = -1.160460 - 0.095231I$	$-2.41906 + 3.14939I$	0
$b = 0.621537 + 0.513207I$		
$u = 0.168747 - 1.299570I$		
$a = -1.160460 + 0.095231I$	$-2.41906 - 3.14939I$	0
$b = 0.621537 - 0.513207I$		
$u = -0.127946 + 1.305470I$		
$a = 1.01457 + 0.98940I$	$1.33477 - 3.68069I$	0
$b = -0.355180 - 0.973680I$		
$u = -0.127946 - 1.305470I$		
$a = 1.01457 - 0.98940I$	$1.33477 + 3.68069I$	0
$b = -0.355180 + 0.973680I$		
$u = 0.742301 + 1.091100I$		
$a = -1.65448 - 0.11863I$	$1.76789 + 6.80173I$	0
$b = 0.574713 - 1.106020I$		
$u = 0.742301 - 1.091100I$		
$a = -1.65448 + 0.11863I$	$1.76789 - 6.80173I$	0
$b = 0.574713 + 1.106020I$		
$u = -0.177771 + 0.654829I$		
$a = -1.54211 - 2.08388I$	$-0.28924 + 2.83636I$	$-2.71243 + 0.48181I$
$b = 0.280543 + 1.172630I$		
$u = -0.177771 - 0.654829I$		
$a = -1.54211 + 2.08388I$	$-0.28924 - 2.83636I$	$-2.71243 - 0.48181I$
$b = 0.280543 - 1.172630I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.135020 + 0.718752I$		
$a = -0.256916 - 0.429627I$	$-3.14807 - 1.00103I$	0
$b = -0.433761 - 0.655056I$		
$u = 1.135020 - 0.718752I$		
$a = -0.256916 + 0.429627I$	$-3.14807 + 1.00103I$	0
$b = -0.433761 + 0.655056I$		
$u = -0.333758 + 1.301710I$		
$a = -1.125210 - 0.453522I$	$3.88771 - 6.40116I$	0
$b = 0.660119 + 1.227750I$		
$u = -0.333758 - 1.301710I$		
$a = -1.125210 + 0.453522I$	$3.88771 + 6.40116I$	0
$b = 0.660119 - 1.227750I$		
$u = 1.357640 + 0.182554I$		
$a = -0.318137 + 0.366712I$	$4.05362 - 1.09150I$	0
$b = 0.240823 + 0.895859I$		
$u = 1.357640 - 0.182554I$		
$a = -0.318137 - 0.366712I$	$4.05362 + 1.09150I$	0
$b = 0.240823 - 0.895859I$		
$u = 0.101485 + 0.614941I$		
$a = -0.51389 - 2.78335I$	$-2.99772 + 0.49314I$	$-10.20779 - 0.54757I$
$b = -0.384229 + 0.574149I$		
$u = 0.101485 - 0.614941I$		
$a = -0.51389 + 2.78335I$	$-2.99772 - 0.49314I$	$-10.20779 + 0.54757I$
$b = -0.384229 - 0.574149I$		
$u = -0.043621 + 0.608805I$		
$a = -0.337990 + 0.982054I$	$4.25302 + 3.14758I$	$-13.3582 - 6.4211I$
$b = -0.158002 + 1.375520I$		
$u = -0.043621 - 0.608805I$		
$a = -0.337990 - 0.982054I$	$4.25302 - 3.14758I$	$-13.3582 + 6.4211I$
$b = -0.158002 - 1.375520I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.083490 + 0.574146I$		
$a = 3.28146 - 3.09096I$	$-2.83373 - 5.57072I$	$-9.83182 + 3.03437I$
$b = 0.139490 + 0.602255I$		
$u = -0.083490 - 0.574146I$		
$a = 3.28146 + 3.09096I$	$-2.83373 + 5.57072I$	$-9.83182 - 3.03437I$
$b = 0.139490 - 0.602255I$		
$u = 0.24843 + 1.41104I$		
$a = 1.201970 + 0.193297I$	$-10.03120 + 2.76694I$	0
$b = -1.311850 - 0.332674I$		
$u = 0.24843 - 1.41104I$		
$a = 1.201970 - 0.193297I$	$-10.03120 - 2.76694I$	0
$b = -1.311850 + 0.332674I$		
$u = -1.42356 + 0.20208I$		
$a = -0.157691 - 0.245300I$	$-1.82116 + 10.24000I$	0
$b = 0.541627 - 1.092830I$		
$u = -1.42356 - 0.20208I$		
$a = -0.157691 + 0.245300I$	$-1.82116 - 10.24000I$	0
$b = 0.541627 + 1.092830I$		
$u = -0.43993 + 1.38434I$		
$a = -1.127230 + 0.341272I$	$-9.01735 - 10.63490I$	0
$b = 1.278150 - 0.291752I$		
$u = -0.43993 - 1.38434I$		
$a = -1.127230 - 0.341272I$	$-9.01735 + 10.63490I$	0
$b = 1.278150 + 0.291752I$		
$u = 1.46492 + 0.00723I$		
$a = 0.100561 + 0.306556I$	$-2.04812 + 2.89700I$	0
$b = -0.484657 + 0.984843I$		
$u = 1.46492 - 0.00723I$		
$a = 0.100561 - 0.306556I$	$-2.04812 - 2.89700I$	0
$b = -0.484657 - 0.984843I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.348648 + 0.367582I$		
$a = -1.90907 - 1.02160I$	$-1.08052 + 3.03153I$	$-4.19529 - 6.98712I$
$b = -0.458537 + 1.167530I$		
$u = -0.348648 - 0.367582I$		
$a = -1.90907 + 1.02160I$	$-1.08052 - 3.03153I$	$-4.19529 + 6.98712I$
$b = -0.458537 - 1.167530I$		
$u = -0.450720$		
$a = -0.0844993$	$-1.01434$	$-9.80070$
$b = -0.597318$		
$u = 0.434220 + 0.100177I$		
$a = -1.42778 - 0.53080I$	$1.81943 + 1.47313I$	$2.23841 - 5.05567I$
$b = 0.458829 - 0.425755I$		
$u = 0.434220 - 0.100177I$		
$a = -1.42778 + 0.53080I$	$1.81943 - 1.47313I$	$2.23841 + 5.05567I$
$b = 0.458829 + 0.425755I$		
$u = 0.48637 + 1.49061I$		
$a = -1.218430 + 0.238886I$	$-0.84154 + 7.69049I$	$0$
$b = 0.531464 - 1.038740I$		
$u = 0.48637 - 1.49061I$		
$a = -1.218430 - 0.238886I$	$-0.84154 - 7.69049I$	$0$
$b = 0.531464 + 1.038740I$		
$u = 0.08112 + 1.57336I$		
$a = -0.159001 - 1.055490I$	$-8.24646 + 3.36594I$	$0$
$b = 0.081345 + 0.516147I$		
$u = 0.08112 - 1.57336I$		
$a = -0.159001 + 1.055490I$	$-8.24646 - 3.36594I$	$0$
$b = 0.081345 - 0.516147I$		
$u = -0.69079 + 1.42046I$		
$a = -1.335130 + 0.029753I$	$-5.7735 - 17.5282I$	$0$
$b = 0.70729 + 1.31503I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.69079 - 1.42046I$		
$a = -1.335130 - 0.029753I$	$-5.7735 + 17.5282I$	0
$b = 0.70729 - 1.31503I$		
$u = 0.34818 + 1.54269I$		
$a = 0.602664 - 0.112346I$	$-8.25680 + 4.07430I$	0
$b = -0.672908 - 0.149542I$		
$u = 0.34818 - 1.54269I$		
$a = 0.602664 + 0.112346I$	$-8.25680 - 4.07430I$	0
$b = -0.672908 + 0.149542I$		
$u = 0.57420 + 1.47874I$		
$a = 1.222600 - 0.079987I$	$-6.97944 + 9.81769I$	0
$b = -0.73659 + 1.29574I$		
$u = 0.57420 - 1.47874I$		
$a = 1.222600 + 0.079987I$	$-6.97944 - 9.81769I$	0
$b = -0.73659 - 1.29574I$		
$u = -1.59091 + 0.16862I$		
$a = 0.128237 - 0.245162I$	$9.22842 + 0.69070I$	0
$b = 0.166901 - 0.946580I$		
$u = -1.59091 - 0.16862I$		
$a = 0.128237 + 0.245162I$	$9.22842 - 0.69070I$	0
$b = 0.166901 + 0.946580I$		
$u = -0.69996 + 1.44725I$		
$a = -0.860669 + 0.298264I$	$-7.15592 - 1.23427I$	0
$b = 0.565060 + 1.060420I$		
$u = -0.69996 - 1.44725I$		
$a = -0.860669 - 0.298264I$	$-7.15592 + 1.23427I$	0
$b = 0.565060 - 1.060420I$		
$u = 0.82426 + 1.38827I$		
$a = 0.882873 + 0.248570I$	$-5.40898 + 8.75488I$	0
$b = -0.533007 + 1.170240I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.82426 - 1.38827I$		
$a = 0.882873 - 0.248570I$	$-5.40898 - 8.75488I$	0
$b = -0.533007 - 1.170240I$		
$u = -0.085056 + 0.336008I$		
$a = -0.56056 + 1.33121I$	$8.09208 + 4.40093I$	$12.3851 - 9.4173I$
$b = 0.25862 - 1.46830I$		
$u = -0.085056 - 0.336008I$		
$a = -0.56056 - 1.33121I$	$8.09208 - 4.40093I$	$12.3851 + 9.4173I$
$b = 0.25862 + 1.46830I$		
$u = -0.20418 + 1.71330I$		
$a = -0.487948 + 0.042312I$	$-8.99209 + 3.35535I$	0
$b = 0.556415 - 0.423879I$		
$u = -0.20418 - 1.71330I$		
$a = -0.487948 - 0.042312I$	$-8.99209 - 3.35535I$	0
$b = 0.556415 + 0.423879I$		

$$I_2^u = \langle -1.48 \times 10^{10} u^{27} + 1.85 \times 10^{10} u^{26} + \dots + 6.92 \times 10^9 b + 5.27 \times 10^9, \ 3.06 \times 10^{14} u^{27} - 7.91 \times 10^{14} u^{26} + \dots + 3.02 \times 10^{13} a - 1.30 \times 10^{15}, \ u^{28} - u^{27} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -10.1313u^{27} + 26.2272u^{26} + \dots - 73.0464u + 43.0310 \\ 2.14184u^{27} - 2.67820u^{26} + \dots + 7.64335u - 0.761907 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -15.5591u^{27} + 3.96166u^{26} + \dots - 13.7516u - 28.8358 \\ -14.2009u^{27} + 16.9863u^{26} + \dots - 40.4383u + 0.727670 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -7.98945u^{27} + 23.5490u^{26} + \dots - 65.4030u + 42.2691 \\ 2.14184u^{27} - 2.67820u^{26} + \dots + 7.64335u - 0.761907 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 41.4725u^{27} - 39.0584u^{26} + \dots + 93.9212u + 17.8821 \\ -2.81965u^{27} - 0.703457u^{26} + \dots + 2.08339u - 6.66495 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -16.3340u^{27} + 14.6107u^{26} + \dots - 34.9812u - 14.2498 \\ -2.88685u^{27} + 25.9054u^{26} + \dots - 87.0963u + 49.7467 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -16.3340u^{27} + 14.6107u^{26} + \dots - 34.9812u - 14.2498 \\ 2.37034u^{27} + 20.0121u^{26} + \dots - 72.4857u + 51.4700 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -6.62994u^{27} + 18.3565u^{26} + \dots - 52.7997u + 32.1923 \\ 4.27994u^{27} - 7.24008u^{26} + \dots + 20.0194u - 7.23132 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 16.4780u^{27} - 9.58480u^{26} + \dots + 30.2298u + 18.3185 \\ -9.23901u^{27} - 3.57653u^{26} + \dots + 48.8854u - 44.8137 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= \frac{180804181519969}{1436074916247} u^{27} - \frac{227368293507968}{1436074916247} u^{26} + \dots + \frac{399031079592181}{1436074916247} u - \frac{17801125744790}{1436074916247}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{28} - 11u^{27} + \cdots + 33u + 7$
$c_2$	$u^{28} + u^{27} + \cdots - u + 1$
$c_3$	$u^{28} + u^{27} + \cdots + u + 1$
$c_4$	$u^{28} - u^{27} + \cdots - u + 1$
$c_5$	$u^{28} - u^{27} + \cdots + u + 1$
$c_6$	$u^{28} - 3u^{27} + \cdots - 259u + 49$
$c_7$	$u^{28} + 3u^{26} + \cdots + 53u^2 + 48$
$c_8$	$u^{28} - u^{27} + \cdots - u + 1$
$c_9$	$u^{28} + u^{27} + \cdots + 5u + 1$
$c_{10}$	$u^{28} + u^{27} + \cdots + u + 1$
$c_{11}$	$u^{28} - 2u^{27} + \cdots - 5u + 1$
$c_{12}$	$u^{28} - u^{27} + \cdots - 5u + 1$



**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{28} - 19y^{27} + \cdots + 2369y + 49$
$c_2, c_5$	$y^{28} + 5y^{27} + \cdots - 13y + 1$
$c_3, c_8$	$y^{28} + 11y^{27} + \cdots + 23y + 1$
$c_4, c_{10}$	$y^{28} + 21y^{27} + \cdots + 33y + 1$
$c_6$	$y^{28} - 13y^{27} + \cdots - 63063y + 2401$
$c_7$	$y^{28} + 6y^{27} + \cdots + 5088y + 2304$
$c_9, c_{12}$	$y^{28} + 23y^{27} + \cdots + 19y + 1$
$c_{11}$	$y^{28} + 12y^{27} + \cdots + 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.237894 + 0.956664I$		
$a = 1.62413 - 0.61086I$	$1.17000 - 0.96284I$	$2.75739 + 5.45614I$
$b = -1.348680 + 0.253251I$		
$u = -0.237894 - 0.956664I$		
$a = 1.62413 + 0.61086I$	$1.17000 + 0.96284I$	$2.75739 - 5.45614I$
$b = -1.348680 - 0.253251I$		
$u = -0.075270 + 0.920982I$		
$a = 1.46046 + 0.61112I$	$0.10200 - 1.96445I$	$-3.39434 + 3.81435I$
$b = -0.154790 - 0.165445I$		
$u = -0.075270 - 0.920982I$		
$a = 1.46046 - 0.61112I$	$0.10200 + 1.96445I$	$-3.39434 - 3.81435I$
$b = -0.154790 + 0.165445I$		
$u = 0.767899 + 0.489005I$		
$a = 0.28195 - 1.49523I$	$-1.76432 + 0.94657I$	$-3.08016 - 1.47243I$
$b = 0.288649 - 0.938440I$		
$u = 0.767899 - 0.489005I$		
$a = 0.28195 + 1.49523I$	$-1.76432 - 0.94657I$	$-3.08016 + 1.47243I$
$b = 0.288649 + 0.938440I$		
$u = 0.345981 + 1.078720I$		
$a = -1.29799 - 0.58885I$	$-1.11821 + 3.08885I$	$-3.90201 - 4.91311I$
$b = 0.464033 + 0.523133I$		
$u = 0.345981 - 1.078720I$		
$a = -1.29799 + 0.58885I$	$-1.11821 - 3.08885I$	$-3.90201 + 4.91311I$
$b = 0.464033 - 0.523133I$		
$u = 0.361782 + 1.161100I$		
$a = -1.44305 - 0.02533I$	$-3.30691 + 5.70672I$	$-6.21178 - 1.53244I$
$b = 0.83558 - 1.28549I$		
$u = 0.361782 - 1.161100I$		
$a = -1.44305 + 0.02533I$	$-3.30691 - 5.70672I$	$-6.21178 + 1.53244I$
$b = 0.83558 + 1.28549I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.460734 + 0.557400I$		
$a = 1.67016 - 3.00711I$	$-2.40630 - 6.12716I$	$-2.90922 + 11.28305I$
$b = -0.283700 - 0.830897I$		
$u = -0.460734 - 0.557400I$		
$a = 1.67016 + 3.00711I$	$-2.40630 + 6.12716I$	$-2.90922 - 11.28305I$
$b = -0.283700 + 0.830897I$		
$u = 1.283280 + 0.227081I$		
$a = -0.422310 + 0.369260I$	$4.34526 - 0.97725I$	$15.3469 + 0.I$
$b = 0.241891 + 0.958455I$		
$u = 1.283280 - 0.227081I$		
$a = -0.422310 - 0.369260I$	$4.34526 + 0.97725I$	$15.3469 + 0.I$
$b = 0.241891 - 0.958455I$		
$u = -0.499201 + 1.214250I$		
$a = 1.39941 + 0.31082I$	$4.75725 - 7.02891I$	$1.79878 + 6.91651I$
$b = -0.583152 - 1.238720I$		
$u = -0.499201 - 1.214250I$		
$a = 1.39941 - 0.31082I$	$4.75725 + 7.02891I$	$1.79878 - 6.91651I$
$b = -0.583152 + 1.238720I$		
$u = 0.616251 + 1.161350I$		
$a = -1.77881 + 0.02178I$	$1.08473 + 7.05378I$	$-5.34427 - 7.49870I$
$b = 0.500258 - 1.145780I$		
$u = 0.616251 - 1.161350I$		
$a = -1.77881 - 0.02178I$	$1.08473 - 7.05378I$	$-5.34427 + 7.49870I$
$b = 0.500258 + 1.145780I$		
$u = -0.121598 + 0.618770I$		
$a = 0.363385 - 0.311626I$	$7.80044 + 4.25334I$	$-9.98560 + 1.63731I$
$b = -0.28392 + 1.51928I$		
$u = -0.121598 - 0.618770I$		
$a = 0.363385 + 0.311626I$	$7.80044 - 4.25334I$	$-9.98560 - 1.63731I$
$b = -0.28392 - 1.51928I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.060992 + 0.612880I$		
$a = 0.79439 - 2.52484I$	$0.00703 - 3.49133I$	$2.69813 + 10.38411I$
$b = -0.15044 + 1.57854I$		
$u = -0.060992 - 0.612880I$		
$a = 0.79439 + 2.52484I$	$0.00703 + 3.49133I$	$2.69813 - 10.38411I$
$b = -0.15044 - 1.57854I$		
$u = 0.132401 + 0.495278I$		
$a = 0.05605 + 1.75947I$	$4.54210 - 3.04662I$	$11.87871 - 1.91283I$
$b = 0.175425 + 1.332670I$		
$u = 0.132401 - 0.495278I$		
$a = 0.05605 - 1.75947I$	$4.54210 + 3.04662I$	$11.87871 + 1.91283I$
$b = 0.175425 - 1.332670I$		
$u = -1.60870 + 0.24907I$		
$a = -0.047493 + 0.236281I$	$9.18806 + 0.90073I$	$0. - 20.1489I$
$b = -0.220934 + 0.958878I$		
$u = -1.60870 - 0.24907I$		
$a = -0.047493 - 0.236281I$	$9.18806 - 0.90073I$	$0. + 20.1489I$
$b = -0.220934 - 0.958878I$		
$u = 0.05679 + 1.65897I$		
$a = -0.160288 - 0.878952I$	$-7.95181 + 3.45202I$	0
$b = 0.019782 + 0.634182I$		
$u = 0.05679 - 1.65897I$		
$a = -0.160288 + 0.878952I$	$-7.95181 - 3.45202I$	0
$b = 0.019782 - 0.634182I$		

$$\text{III. } I_3^u = \langle b - u, a + u - 1, u^2 - u + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u + 1 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u + 1 \\ u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 2u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2 \\ 2u - 1 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes =  $4u - 8$**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$(u - 1)^2$
$c_2, c_3, c_4$ $c_{12}$	$u^2 + u + 1$
$c_5, c_8, c_9$ $c_{10}$	$u^2 - u + 1$
$c_7$	$u^2$
$c_{11}$	$(u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_{11}$	$(y - 1)^2$
$c_2, c_3, c_4$ $c_5, c_8, c_9$ $c_{10}, c_{12}$	$y^2 + y + 1$
$c_7$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$		
$a = 0.500000 - 0.866025I$	$-1.64493 - 2.02988I$	$-6.00000 + 3.46410I$
$b = 0.500000 + 0.866025I$		
$u = 0.500000 - 0.866025I$		
$a = 0.500000 + 0.866025I$	$-1.64493 + 2.02988I$	$-6.00000 - 3.46410I$
$b = 0.500000 - 0.866025I$		

$$\text{IV. } I_4^u = \langle b - u, a + u, u^2 - u + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 3u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u + 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^2 + 3u + 3$
$c_2, c_4, c_5$ $c_7, c_{10}$	$u^2 + u + 1$
$c_3, c_6, c_8$ $c_9, c_{12}$	$u^2 - u + 1$
$c_{11}$	$u^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^2 - 3y + 9$
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{12}$	$y^2 + y + 1$
$c_{11}$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$		
$a = -0.500000 - 0.866025I$	$2.02988I$	$0. - 3.46410I$
$b = 0.500000 + 0.866025I$		
$u = 0.500000 - 0.866025I$		
$a = -0.500000 + 0.866025I$	$-2.02988I$	$0. + 3.46410I$
$b = 0.500000 - 0.866025I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^2)(u^2 + 3u + 3)(u^{28} - 11u^{27} + \dots + 33u + 7)$ $\cdot (u^{85} - 5u^{84} + \dots - 783263u - 43963)$
$c_2$	$((u^2 + u + 1)^2)(u^{28} + u^{27} + \dots - u + 1)$ $\cdot (u^{85} + 4u^{84} + \dots + 6399682u + 378351)$
$c_3$	$(u^2 - u + 1)(u^2 + u + 1)(u^{28} + u^{27} + \dots + u + 1)$ $\cdot (u^{85} + 27u^{83} + \dots + 4868u + 1167)$
$c_4$	$((u^2 + u + 1)^2)(u^{28} - u^{27} + \dots - u + 1)(u^{85} - 2u^{84} + \dots - 32u + 3)$
$c_5$	$(u^2 - u + 1)(u^2 + u + 1)(u^{28} - u^{27} + \dots + u + 1)$ $\cdot (u^{85} + 4u^{84} + \dots + 6399682u + 378351)$
$c_6$	$((u - 1)^2)(u^2 - u + 1)(u^{28} - 3u^{27} + \dots - 259u + 49)$ $\cdot (u^{85} + 11u^{84} + \dots - 284299729u + 28854207)$
$c_7$	$u^2(u^2 + u + 1)(u^{28} + 3u^{26} + \dots + 53u^2 + 48)$ $\cdot (u^{85} - 6u^{83} + \dots - 4044u + 332)$
$c_8$	$((u^2 - u + 1)^2)(u^{28} - u^{27} + \dots - u + 1)$ $\cdot (u^{85} + 27u^{83} + \dots + 4868u + 1167)$
$c_9$	$((u^2 - u + 1)^2)(u^{28} + u^{27} + \dots + 5u + 1)$ $\cdot (u^{85} + 25u^{83} + \dots - 226u + 111)$
$c_{10}$	$(u^2 - u + 1)(u^2 + u + 1)(u^{28} + u^{27} + \dots + u + 1)$ $\cdot (u^{85} - 2u^{84} + \dots - 32u + 3)$
$c_{11}$	$u^2(u + 1)^2(u^{28} - 2u^{27} + \dots - 5u + 1)(u^{85} - u^{84} + \dots - 107u + 49)$
$c_{12}$	$(u^2 - u + 1)(u^2 + u + 1)(u^{28} - u^{27} + \dots - 5u + 1)$ $\cdot (u^{85} + 25u^{83} + \dots - 326u + 111)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^2)(y^2 - 3y + 9)(y^{28} - 19y^{27} + \dots + 2369y + 49)$ $\cdot (y^{85} - 71y^{84} + \dots + 1109768547995y - 1932745369)$
$c_2, c_5$	$((y^2 + y + 1)^2)(y^{28} + 5y^{27} + \dots - 13y + 1)$ $\cdot (y^{85} + 72y^{84} + \dots + 23176806835342y - 143149479201)$
$c_3, c_8$	$((y^2 + y + 1)^2)(y^{28} + 11y^{27} + \dots + 23y + 1)$ $\cdot (y^{85} + 54y^{84} + \dots - 53028158y - 1361889)$
$c_4, c_{10}$	$((y^2 + y + 1)^2)(y^{28} + 21y^{27} + \dots + 33y + 1)$ $\cdot (y^{85} + 24y^{84} + \dots - 356y - 9)$
$c_6$	$((y - 1)^2)(y^2 + y + 1)(y^{28} - 13y^{27} + \dots - 63063y + 2401)$ $\cdot (y^{85} - 49y^{84} + \dots + 24664681049291167y - 832565261598849)$
$c_7$	$y^2(y^2 + y + 1)(y^{28} + 6y^{27} + \dots + 5088y + 2304)$ $\cdot (y^{85} - 12y^{84} + \dots + 8779024y - 110224)$
$c_9, c_{12}$	$((y^2 + y + 1)^2)(y^{28} + 23y^{27} + \dots + 19y + 1)$ $\cdot (y^{85} + 50y^{84} + \dots - 318554y - 12321)$
$c_{11}$	$y^2(y - 1)^2(y^{28} + 12y^{27} + \dots + 5y + 1)$ $\cdot (y^{85} + 5y^{84} + \dots - 31181y - 2401)$