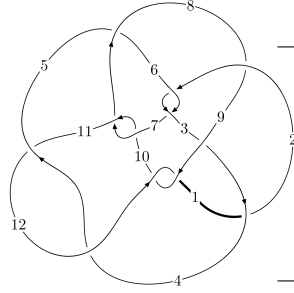
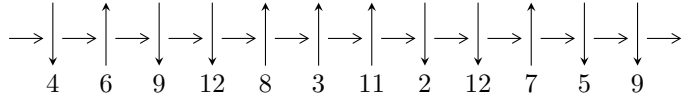


12n<sub>0781</sub> (K12n<sub>0781</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,9 \xrightarrow{c_3} 4,6 \xrightarrow{c_6} 7 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_8} 8 \xrightarrow{c_5} 5 \xrightarrow{c_{12}} 12 \xrightarrow{c_9} 10 \xrightarrow{c_{11}} 11 \rightsquigarrow c_4, c_7, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 155164409u^{19} - 1173171752u^{18} + \dots + 19656063b + 4652516609, \\ 3194027005u^{19} - 23918980957u^{18} + \dots + 864866772a + 84007929151, \\ u^{20} - 9u^{19} + \dots - 101u - 44 \rangle$$

$$I_2^u = \langle 1153398772571u^{26}a - 27659986158013u^{26} + \dots + 47932282550416a + 517986614105786, \\ 6.62034 \times 10^{14}au^{26} + 1.26437 \times 10^{15}u^{26} + \dots - 4.24307 \times 10^{15}a - 1.06993 \times 10^{16}, u^{27} + 4u^{26} + \dots - 16u + \dots \rangle$$

$$I_3^u = \langle b + u - 2, 2u^3 - 12u^2 + 5a + 19u - 7, u^4 - 6u^3 + 12u^2 - 11u + 5 \rangle$$

$$I_4^u = \langle u^{10}a + 2u^{11} + \dots - a - 3, 2u^{11}a + 4u^{11} + \dots - 3a + 10, \\ u^{12} + 3u^{11} - 2u^{10} - 14u^9 - 7u^8 + 19u^7 + 20u^6 - 4u^5 - 13u^4 - 7u^3 + 4u + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 102 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.55 \times 10^8 u^{19} - 1.17 \times 10^9 u^{18} + \dots + 1.97 \times 10^7 b + 4.65 \times 10^9, 3.19 \times 10^9 u^{19} - 2.39 \times 10^{10} u^{18} + \dots + 8.65 \times 10^8 a + 8.40 \times 10^{10}, u^{20} - 9u^{19} + \dots - 101u - 44 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -3.69309u^{19} + 27.6563u^{18} + \dots - 289.384u - 97.1340 \\ -7.89397u^{19} + 59.6850u^{18} + \dots - 701.033u - 236.696 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -11.5871u^{19} + 87.3412u^{18} + \dots - 990.417u - 333.830 \\ -7.89397u^{19} + 59.6850u^{18} + \dots - 701.033u - 236.696 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.729812u^{19} + 5.09498u^{18} + \dots - 10.5444u - 0.980246 \\ -3.00124u^{19} + 23.1501u^{18} + \dots - 293.563u - 98.7110 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.770109u^{19} + 6.89068u^{18} + \dots - 123.191u - 34.8650 \\ 1.39273u^{19} - 6.70756u^{18} + \dots - 150.601u - 35.6579 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1.32525u^{19} - 10.3344u^{18} + \dots + 119.923u + 43.4460 \\ -2.61701u^{19} + 19.7532u^{18} + \dots - 222.509u - 77.4331 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -3.35278u^{19} + 25.4969u^{18} + \dots - 322.784u - 103.076 \\ -4.67803u^{19} + 35.8313u^{18} + \dots - 442.706u - 147.522 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.770109u^{19} + 6.89068u^{18} + \dots - 123.191u - 34.8650 \\ -0.0402972u^{19} + 1.79570u^{18} + \dots - 112.646u - 33.8848 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -7.78475u^{19} + 58.9253u^{18} + \dots - 701.929u - 238.453 \\ -11.1375u^{19} + 84.4222u^{18} + \dots - 1023.71u - 342.529 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -4.05370u^{19} + 30.6802u^{18} + \dots - 397.822u - 137.762 \\ -8.13629u^{19} + 61.2722u^{18} + \dots - 730.150u - 243.818 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{1862218903}{19656063} u^{19} - \frac{13770753601}{19656063} u^{18} + \dots + \frac{47665991273}{6552021} u + \frac{49632160054}{19656063}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_9, c_{12}$	$u^{20} + 3u^{19} + \dots + 7u + 1$
$c_2, c_6, c_7$ $c_{10}$	$u^{20} - 3u^{18} + \dots - 2u - 1$
$c_3$	$u^{20} - 9u^{19} + \dots - 101u - 44$
$c_4, c_8, c_{11}$	$u^{20} - u^{19} + \dots + u - 1$
$c_5$	$u^{20} + 4u^{19} + \dots + 371u + 44$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_9, c_{12}$	$y^{20} - 31y^{19} + \dots - 53y + 1$
$c_2, c_6, c_7$ $c_{10}$	$y^{20} - 6y^{19} + \dots - 2y + 1$
$c_3$	$y^{20} - 29y^{19} + \dots - 23841y + 1936$
$c_4, c_8, c_{11}$	$y^{20} + 9y^{19} + \dots + 3y + 1$
$c_5$	$y^{20} - 22y^{19} + \dots - 10041y + 1936$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.052670 + 0.214579I$		
$a = 0.32175 - 1.92778I$	$6.83483 + 4.33332I$	$0.05876 - 7.63423I$
$b = -0.836827 - 0.543539I$		
$u = -1.052670 - 0.214579I$		
$a = 0.32175 + 1.92778I$	$6.83483 - 4.33332I$	$0.05876 + 7.63423I$
$b = -0.836827 + 0.543539I$		
$u = 1.120110 + 0.346275I$		
$a = -0.233306 - 0.424229I$	$-5.30551 - 1.26066I$	$2.12940 + 5.78685I$
$b = -0.38707 - 1.48766I$		
$u = 1.120110 - 0.346275I$		
$a = -0.233306 + 0.424229I$	$-5.30551 + 1.26066I$	$2.12940 - 5.78685I$
$b = -0.38707 + 1.48766I$		
$u = -0.476182 + 0.251897I$		
$a = 0.298266 + 0.199444I$	$-0.934143 + 0.731157I$	$-6.62873 - 3.56102I$
$b = 0.127716 - 0.483656I$		
$u = -0.476182 - 0.251897I$		
$a = 0.298266 - 0.199444I$	$-0.934143 - 0.731157I$	$-6.62873 + 3.56102I$
$b = 0.127716 + 0.483656I$		
$u = 1.46200 + 0.11516I$		
$a = -0.105955 + 0.364783I$	$-7.00266 + 1.06770I$	$-8.57959 - 5.53529I$
$b = 0.313911 + 0.848453I$		
$u = 1.46200 - 0.11516I$		
$a = -0.105955 - 0.364783I$	$-7.00266 - 1.06770I$	$-8.57959 + 5.53529I$
$b = 0.313911 - 0.848453I$		
$u = -0.42309 + 1.47138I$		
$a = -1.165830 + 0.209425I$	$7.84975 + 9.25606I$	$2.98645 - 8.19728I$
$b = 1.44769 + 0.49745I$		
$u = -0.42309 - 1.47138I$		
$a = -1.165830 - 0.209425I$	$7.84975 - 9.25606I$	$2.98645 + 8.19728I$
$b = 1.44769 - 0.49745I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.44287 + 0.52695I$ $a = 1.215020 + 0.143277I$ $b = -0.794041 - 0.102232I$	$2.39136 + 0.46763I$	$16.5681 - 6.4930I$
$u = 1.44287 - 0.52695I$ $a = 1.215020 - 0.143277I$ $b = -0.794041 + 0.102232I$	$2.39136 - 0.46763I$	$16.5681 + 6.4930I$
$u = -0.374420 + 0.266879I$ $a = -3.88796 + 1.78468I$ $b = 0.790015 - 0.335634I$	$9.03012 - 2.73757I$	$11.18044 + 1.41623I$
$u = -0.374420 - 0.266879I$ $a = -3.88796 - 1.78468I$ $b = 0.790015 + 0.335634I$	$9.03012 + 2.73757I$	$11.18044 - 1.41623I$
$u = 1.67183$ $a = 0.0164989$ $b = 0.556210$	$-7.42843$	$21.0830$
$u = 1.64455 + 0.32821I$ $a = -0.97484 - 1.07134I$ $b = 0.955066 - 0.584622I$	$-3.92374 - 8.34608I$	$0. + 8.57009I$
$u = 1.64455 - 0.32821I$ $a = -0.97484 + 1.07134I$ $b = 0.955066 + 0.584622I$	$-3.92374 + 8.34608I$	$0. - 8.57009I$
$u = 1.66385 + 0.49105I$ $a = 0.747318 + 0.938443I$ $b = -1.33112 + 0.78381I$	$1.0956 - 16.1913I$	$1.21980 + 7.93611I$
$u = 1.66385 - 0.49105I$ $a = 0.747318 - 0.938443I$ $b = -1.33112 - 0.78381I$	$1.0956 + 16.1913I$	$1.21980 - 7.93611I$
$u = -2.68586$ $a = 0.713636$ $b = -1.12689$	$3.80648$	$0$

$$\text{II. } I_2^u = \langle 1.15 \times 10^{12} au^{26} - 2.77 \times 10^{13} u^{26} + \dots + 4.79 \times 10^{13} a + 5.18 \times 10^{14}, 6.62 \times 10^{14} au^{26} + 1.26 \times 10^{15} u^{26} + \dots - 4.24 \times 10^{15} a - 1.07 \times 10^{16}, u^{27} + 4u^{26} + \dots - 16u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ -0.0242410au^{26} + 0.581330u^{26} + \dots - 1.00739a - 10.8865 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0242410au^{26} + 0.581330u^{26} + \dots - 0.00739376a - 10.8865 \\ -0.0242410au^{26} + 0.581330u^{26} + \dots - 1.00739a - 10.8865 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.08669au^{26} + 0.00739376u^{26} + \dots + 7.02849a + 7.42850 \\ -0.0360384au^{26} - 1.26454u^{26} + \dots - 0.689023a + 8.59574 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.841478au^{26} - u^{26} + \dots + 6.18701a + 16 \\ 0.337969au^{26} - 1.00739u^{26} + \dots - 0.596266a + 8.57150 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1.50664au^{26} - 2.66029u^{26} + \dots + 10.2782a + 26.5660 \\ -0.242104au^{26} - 1.76324u^{26} + \dots + 1.68247a + 6.29618 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.513982au^{26} - 4.80755u^{26} + \dots - 2.50550a + 27.3198 \\ 0.513982au^{26} + 1.68297u^{26} + \dots - 2.50550a - 9.53524 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.841478au^{26} - u^{26} + \dots + 6.18701a + 16 \\ 0.245212au^{26} - 1.00739u^{26} + \dots - 0.841478a + 8.57150 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2.50550au^{26} + 4.15537u^{26} + \dots - 10.7922a - 38.4438 \\ 0.398816u^{26} + 2.23271u^{25} + \dots + 57.1829u - 5.41613 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.92417au^{26} + 3.36740u^{26} + \dots + 0.0943422a - 27.9026 \\ -0.396547u^{26} + 0.153675u^{25} + \dots + 32.0090u - 1.30351 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{195093488669178}{47580483876995} u^{26} + \frac{621166284588117}{47580483876995} u^{25} + \dots + \frac{10739526635696416}{47580483876995} u - \frac{1670488305527964}{47580483876995}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_9, c_{12}$	$u^{54} - 9u^{53} + \dots - 817482u + 44911$
$c_2, c_6, c_7$ $c_{10}$	$u^{54} - 2u^{53} + \dots - 7504u + 1667$
$c_3$	$(u^{27} + 4u^{26} + \dots - 16u + 1)^2$
$c_4, c_8, c_{11}$	$u^{54} + 3u^{53} + \dots - 7068u + 1763$
$c_5$	$(u^{27} - 2u^{26} + \dots - 67u + 47)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_9, c_{12}$	$y^{54} - 53y^{53} + \dots + 26272962362y + 2016997921$
$c_2, c_6, c_7$ $c_{10}$	$y^{54} - 28y^{53} + \dots - 34895734y + 2778889$
$c_3$	$(y^{27} - 30y^{26} + \dots + 108y - 1)^2$
$c_4, c_8, c_{11}$	$y^{54} + 27y^{53} + \dots + 38637652y + 3108169$
$c_5$	$(y^{27} - 20y^{26} + \dots + 14171y - 2209)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.158532 + 0.935582I$ $a = -1.50310 + 0.50723I$ $b = 1.316050 - 0.206467I$	$2.66520 - 3.11494I$	$4.06258 + 4.43870I$
$u = -0.158532 + 0.935582I$ $a = -0.232784 + 0.158230I$ $b = -0.125783 + 1.310910I$	$2.66520 - 3.11494I$	$4.06258 + 4.43870I$
$u = -0.158532 - 0.935582I$ $a = -1.50310 - 0.50723I$ $b = 1.316050 + 0.206467I$	$2.66520 + 3.11494I$	$4.06258 - 4.43870I$
$u = -0.158532 - 0.935582I$ $a = -0.232784 - 0.158230I$ $b = -0.125783 - 1.310910I$	$2.66520 + 3.11494I$	$4.06258 - 4.43870I$
$u = 1.07088$ $a = 0.20349 + 1.69086I$ $b = -1.039390 + 0.501438I$	$7.61014$	$2.10720$
$u = 1.07088$ $a = 0.20349 - 1.69086I$ $b = -1.039390 - 0.501438I$	$7.61014$	$2.10720$
$u = 0.221976 + 0.825159I$ $a = 0.865041 - 0.769539I$ $b = -0.188178 - 0.427579I$	$1.85443 + 1.12451I$	$2.23685 + 3.40792I$
$u = 0.221976 + 0.825159I$ $a = 1.56832 + 0.15522I$ $b = -1.056960 - 0.253260I$	$1.85443 + 1.12451I$	$2.23685 + 3.40792I$
$u = 0.221976 - 0.825159I$ $a = 0.865041 + 0.769539I$ $b = -0.188178 + 0.427579I$	$1.85443 - 1.12451I$	$2.23685 - 3.40792I$
$u = 0.221976 - 0.825159I$ $a = 1.56832 - 0.15522I$ $b = -1.056960 + 0.253260I$	$1.85443 - 1.12451I$	$2.23685 - 3.40792I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.772781 + 0.145831I$		
$a = -0.955249 + 0.172273I$	$5.86045 + 0.50074I$	$-0.026133 - 1.385067I$
$b = 0.942406 - 0.743444I$		
$u = -0.772781 + 0.145831I$		
$a = -0.03004 - 1.56141I$	$5.86045 + 0.50074I$	$-0.026133 - 1.385067I$
$b = -0.956615 - 0.919647I$		
$u = -0.772781 - 0.145831I$		
$a = -0.955249 - 0.172273I$	$5.86045 - 0.50074I$	$-0.026133 + 1.385067I$
$b = 0.942406 + 0.743444I$		
$u = -0.772781 - 0.145831I$		
$a = -0.03004 + 1.56141I$	$5.86045 - 0.50074I$	$-0.026133 + 1.385067I$
$b = -0.956615 + 0.919647I$		
$u = 0.732746 + 0.037797I$		
$a = -0.197320 + 0.642818I$	$6.70782 - 6.19371I$	$1.04615 + 5.14040I$
$b = 1.097490 - 0.609563I$		
$u = 0.732746 + 0.037797I$		
$a = 0.39411 + 1.87802I$	$6.70782 - 6.19371I$	$1.04615 + 5.14040I$
$b = -1.136770 + 0.758571I$		
$u = 0.732746 - 0.037797I$		
$a = -0.197320 - 0.642818I$	$6.70782 + 6.19371I$	$1.04615 - 5.14040I$
$b = 1.097490 + 0.609563I$		
$u = 0.732746 - 0.037797I$		
$a = 0.39411 - 1.87802I$	$6.70782 + 6.19371I$	$1.04615 - 5.14040I$
$b = -1.136770 - 0.758571I$		
$u = -1.41462 + 0.08838I$		
$a = 0.262151 - 0.521305I$	$-3.85325 - 2.16315I$	$0.43125 + 2.34406I$
$b = 0.744839 - 1.008240I$		
$u = -1.41462 + 0.08838I$		
$a = 0.94161 + 1.25020I$	$-3.85325 - 2.16315I$	$0.43125 + 2.34406I$
$b = -0.893423 + 0.347194I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.41462 - 0.08838I$ $a = 0.262151 + 0.521305I$ $b = 0.744839 + 1.008240I$	$-3.85325 + 2.16315I$	$0.43125 - 2.34406I$
$u = -1.41462 - 0.08838I$ $a = 0.94161 - 1.25020I$ $b = -0.893423 - 0.347194I$	$-3.85325 + 2.16315I$	$0.43125 - 2.34406I$
$u = 0.96419 + 1.06250I$ $a = -0.777537 - 0.509617I$ $b = 1.49984 - 0.06654I$	$7.39896 - 3.81582I$	$3.19122 + 3.12687I$
$u = 0.96419 + 1.06250I$ $a = 0.996480 + 0.564354I$ $b = -1.52086 + 0.54966I$	$7.39896 - 3.81582I$	$3.19122 + 3.12687I$
$u = 0.96419 - 1.06250I$ $a = -0.777537 + 0.509617I$ $b = 1.49984 + 0.06654I$	$7.39896 + 3.81582I$	$3.19122 - 3.12687I$
$u = 0.96419 - 1.06250I$ $a = 0.996480 - 0.564354I$ $b = -1.52086 - 0.54966I$	$7.39896 + 3.81582I$	$3.19122 - 3.12687I$
$u = 1.46227 + 0.17089I$ $a = -0.70585 - 1.22803I$ $b = 1.080150 - 0.757376I$	$-2.64494 - 4.30028I$	$1.62045 + 0.54924I$
$u = 1.46227 + 0.17089I$ $a = 1.11356 - 1.22226I$ $b = -0.794850 - 0.366906I$	$-2.64494 - 4.30028I$	$1.62045 + 0.54924I$
$u = 1.46227 - 0.17089I$ $a = -0.70585 + 1.22803I$ $b = 1.080150 + 0.757376I$	$-2.64494 + 4.30028I$	$1.62045 - 0.54924I$
$u = 1.46227 - 0.17089I$ $a = 1.11356 + 1.22226I$ $b = -0.794850 + 0.366906I$	$-2.64494 + 4.30028I$	$1.62045 - 0.54924I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.53479$ $a = 0.414758 + 0.269711I$ $b = -1.024280 - 0.077414I$	3.41879	6.41080
$u = -1.53479$ $a = 0.414758 - 0.269711I$ $b = -1.024280 + 0.077414I$	3.41879	6.41080
$u = -1.46424 + 0.50584I$ $a = 0.865744 - 0.882179I$ $b = -1.37593 - 0.68985I$	$-1.70679 + 8.63753I$	$0.70129 - 5.57252I$
$u = -1.46424 + 0.50584I$ $a = -0.222321 + 0.420033I$ $b = -0.51373 + 1.37153I$	$-1.70679 + 8.63753I$	$0.70129 - 5.57252I$
$u = -1.46424 - 0.50584I$ $a = 0.865744 + 0.882179I$ $b = -1.37593 + 0.68985I$	$-1.70679 - 8.63753I$	$0.70129 + 5.57252I$
$u = -1.46424 - 0.50584I$ $a = -0.222321 - 0.420033I$ $b = -0.51373 - 1.37153I$	$-1.70679 - 8.63753I$	$0.70129 + 5.57252I$
$u = 1.60572 + 0.14635I$ $a = 0.143649 + 0.671229I$ $b = 0.676206 + 1.121340I$	$-3.96610 - 0.49039I$	$2.17660 + 0.87451I$
$u = 1.60572 + 0.14635I$ $a = -0.032560 + 0.591612I$ $b = -0.898818 + 0.272522I$	$-3.96610 - 0.49039I$	$2.17660 + 0.87451I$
$u = 1.60572 - 0.14635I$ $a = 0.143649 - 0.671229I$ $b = 0.676206 - 1.121340I$	$-3.96610 + 0.49039I$	$2.17660 - 0.87451I$
$u = 1.60572 - 0.14635I$ $a = -0.032560 - 0.591612I$ $b = -0.898818 - 0.272522I$	$-3.96610 + 0.49039I$	$2.17660 - 0.87451I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.61132 + 0.29006I$ $a = -0.953605 + 0.809181I$ $b = 1.074430 + 0.451641I$	$-4.62159 + 3.33366I$	$0. - 1.64502I$
$u = -1.61132 + 0.29006I$ $a = 0.079718 - 0.306892I$ $b = 0.745769 - 0.725411I$	$-4.62159 + 3.33366I$	$0. - 1.64502I$
$u = -1.61132 - 0.29006I$ $a = -0.953605 - 0.809181I$ $b = 1.074430 - 0.451641I$	$-4.62159 - 3.33366I$	$0. + 1.64502I$
$u = -1.61132 - 0.29006I$ $a = 0.079718 + 0.306892I$ $b = 0.745769 + 0.725411I$	$-4.62159 - 3.33366I$	$0. + 1.64502I$
$u = -1.64260 + 0.12656I$ $a = -0.539122 + 1.081180I$ $b = 1.193170 + 0.752557I$	$-2.09892 + 7.32302I$	$1.91859 - 5.85391I$
$u = -1.64260 + 0.12656I$ $a = -0.147988 - 0.383193I$ $b = -0.958048 - 0.349092I$	$-2.09892 + 7.32302I$	$1.91859 - 5.85391I$
$u = -1.64260 - 0.12656I$ $a = -0.539122 - 1.081180I$ $b = 1.193170 - 0.752557I$	$-2.09892 - 7.32302I$	$1.91859 + 5.85391I$
$u = -1.64260 - 0.12656I$ $a = -0.147988 + 0.383193I$ $b = -0.958048 + 0.349092I$	$-2.09892 - 7.32302I$	$1.91859 + 5.85391I$
$u = 0.341878$ $a = -0.80620 + 4.25915I$ $b = 1.024170 - 0.310510I$	$10.0079$	$6.39560$
$u = 0.341878$ $a = -0.80620 - 4.25915I$ $b = 1.024170 + 0.310510I$	$10.0079$	$6.39560$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.1382100 + 0.0296626I$ $a = -2.23980 - 1.90608I$ $b = -0.676102 + 0.783648I$	$1.15814 - 2.56837I$	$-5.68616 + 5.09265I$
$u = 0.1382100 + 0.0296626I$ $a = -4.00516 - 10.10660I$ $b = 0.765217 - 0.171124I$	$1.15814 - 2.56837I$	$-5.68616 + 5.09265I$
$u = 0.1382100 - 0.0296626I$ $a = -2.23980 + 1.90608I$ $b = -0.676102 - 0.783648I$	$1.15814 + 2.56837I$	$-5.68616 - 5.09265I$
$u = 0.1382100 - 0.0296626I$ $a = -4.00516 + 10.10660I$ $b = 0.765217 + 0.171124I$	$1.15814 + 2.56837I$	$-5.68616 - 5.09265I$

$$\text{III. } I_3^u = \langle b + u - 2, 2u^3 - 12u^2 + 5a + 19u - 7, u^4 - 6u^3 + 12u^2 - 11u + 5 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{2}{5}u^3 + \frac{12}{5}u^2 - \frac{19}{5}u + \frac{7}{5} \\ -u + 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{2}{5}u^3 + \frac{12}{5}u^2 - \frac{24}{5}u + \frac{17}{5} \\ -u + 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{4}{5}u^3 + \frac{19}{5}u^2 - \frac{23}{5}u + \frac{9}{5} \\ u^2 - 4u + 4 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{5}u^3 - \frac{1}{5}u^2 - \frac{8}{5}u + \frac{4}{5} \\ 3u^3 - 13u^2 + 13u - 6 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{5}u^3 + \frac{1}{5}u^2 + \frac{8}{5}u - \frac{4}{5} \\ -u^3 + 5u^2 - 5u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{4}{5}u^3 - \frac{19}{5}u^2 + \frac{28}{5}u - \frac{19}{5} \\ u^3 - 3u^2 + 4u - 4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{5}u^3 - \frac{1}{5}u^2 - \frac{8}{5}u + \frac{4}{5} \\ u^3 - 4u^2 + 3u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{11}{5}u^3 - \frac{51}{5}u^2 + \frac{62}{5}u - \frac{31}{5} \\ 3u^3 - 14u^2 + 19u - 11 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{7}{5}u^3 - \frac{27}{5}u^2 + \frac{19}{5}u - \frac{7}{5} \\ 3u^3 - 13u^2 + 15u - 7 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-22u^2 + 35u - 21$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u^4 - u^3 - 2u^2 - 4u + 1$
$c_2, c_7$	$u^4 - 2u^3 + 3u - 1$
$c_3$	$u^4 - 6u^3 + 12u^2 - 11u + 5$
$c_4$	$u^4 - u^3 - 2u + 1$
$c_5$	$u^4 - 5u^3 + 6u^2 + 2u - 5$
$c_6, c_{10}$	$u^4 + 2u^3 - 3u - 1$
$c_8, c_{11}$	$u^4 + u^3 + 2u + 1$
$c_{12}$	$u^4 + u^3 - 2u^2 + 4u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_9, c_{12}$	$y^4 - 5y^3 - 2y^2 - 20y + 1$
$c_2, c_6, c_7$ $c_{10}$	$y^4 - 4y^3 + 10y^2 - 9y + 1$
$c_3$	$y^4 - 12y^3 + 22y^2 - y + 25$
$c_4, c_8, c_{11}$	$y^4 - y^3 - 2y^2 - 4y + 1$
$c_5$	$y^4 - 13y^3 + 46y^2 - 64y + 25$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.620433 + 0.769480I$ $a = -1.109540 - 0.805650I$ $b = 1.37957 - 0.76948I$	$8.50524 - 7.16341I$	$5.27273 + 5.92572I$
$u = 0.620433 - 0.769480I$ $a = -1.109540 + 0.805650I$ $b = 1.37957 + 0.76948I$	$8.50524 + 7.16341I$	$5.27273 - 5.92572I$
$u = 1.64145$ $a = -0.140116$ $b = 0.358555$	$-7.61222$	$-22.8250$
$u = 3.11769$ $a = 0.759190$ $b = -1.11769$	$3.76121$	$-125.720$

$$\text{IV. } I_4^u = \langle u^{10}a + 2u^{11} + \dots - a - 3, 2u^{11}a + 4u^{11} + \dots - 3a + 10, u^{12} + 3u^{11} + \dots + 4u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ -u^{10}a - 2u^{11} + \dots + a + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{10}a - 2u^{11} + \dots + 2a + 3 \\ -u^{10}a - 2u^{11} + \dots + a + 3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 3u^{11}a + 9u^{10}a + \dots - 14u - 5 \\ u^{10}a + 2u^9a + \dots - 2u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 3u^{10}a + u^{11} + \dots - 8u - 4 \\ -6u^{11}a + 3u^{11} + \dots - 3a + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{10}a + u^{11} + \dots + u + 4 \\ u^{10}a - u^{11} + \dots - a + 4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{10}a - u^{11} + \dots + a - 8 \\ -u^{10}a + 3u^{10} + \dots + a - 4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 3u^{10}a + u^{11} + \dots - 8u - 4 \\ -3u^{11}a + u^{11} + \dots + 6u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{11}a - 3u^{10}a + \dots - 7u - 9 \\ -u^{10} - u^9 + 5u^8 + 6u^7 - 7u^6 - 11u^5 + u^4 + 5u^3 + 2u^2 + 2u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -3u^{11}a - 10u^{10}a + \dots + 3a - 1 \\ -u^{10} - 2u^9 + 3u^8 + 9u^7 + u^6 - 11u^5 - 7u^4 + u^3 + 2u^2 + 3u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= 2u^{11} + 3u^{10} - 11u^9 - 19u^8 + 17u^7 + 42u^6 + 2u^5 - 34u^4 - 22u^3 - 2u^2 + 11u + 10$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u^{24} - 6u^{23} + \dots + 10u + 1$
$c_2, c_7$	$u^{24} - u^{23} + \dots + u^2 + 1$
$c_3$	$(u^{12} + 3u^{11} + \dots + 4u + 1)^2$
$c_4$	$u^{24} + 10u^{22} + \dots + 8u + 1$
$c_5$	$(u^{12} + 5u^{11} + \dots - u + 1)^2$
$c_6, c_{10}$	$u^{24} + u^{23} + \dots + u^2 + 1$
$c_8, c_{11}$	$u^{24} + 10u^{22} + \dots - 8u + 1$
$c_{12}$	$u^{24} + 6u^{23} + \dots - 10u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_9, c_{12}$	$y^{24} - 12y^{23} + \dots - 22y + 1$
$c_2, c_6, c_7$ $c_{10}$	$y^{24} - 7y^{23} + \dots + 2y + 1$
$c_3$	$(y^{12} - 13y^{11} + \dots - 16y + 1)^2$
$c_4, c_8, c_{11}$	$y^{24} + 20y^{23} + \dots - 12y + 1$
$c_5$	$(y^{12} - 11y^{11} + \dots - 15y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.825594 + 0.098170I$ $a = -0.53917 - 2.00160I$ $b = -0.762732 - 0.663101I$	$7.88103 + 3.00613I$	$2.46057 - 2.77569I$
$u = 0.825594 + 0.098170I$ $a = -1.31555 - 1.91865I$ $b = 0.818361 + 0.141778I$	$7.88103 + 3.00613I$	$2.46057 - 2.77569I$
$u = 0.825594 - 0.098170I$ $a = -0.53917 + 2.00160I$ $b = -0.762732 + 0.663101I$	$7.88103 - 3.00613I$	$2.46057 + 2.77569I$
$u = 0.825594 - 0.098170I$ $a = -1.31555 + 1.91865I$ $b = 0.818361 - 0.141778I$	$7.88103 - 3.00613I$	$2.46057 + 2.77569I$
$u = 1.25362$ $a = 0.243567 + 0.537746I$ $b = 0.160883 + 1.179440I$	$-5.74068$	$-1.95790$
$u = 1.25362$ $a = 0.243567 - 0.537746I$ $b = 0.160883 - 1.179440I$	$-5.74068$	$-1.95790$
$u = -1.107540 + 0.627422I$ $a = 0.725858 - 1.187980I$ $b = -1.244680 - 0.659147I$	$9.51415 + 2.44072I$	$5.50124 - 2.26022I$
$u = -1.107540 + 0.627422I$ $a = -0.974699 + 0.995211I$ $b = 1.183370 + 0.002215I$	$9.51415 + 2.44072I$	$5.50124 - 2.26022I$
$u = -1.107540 - 0.627422I$ $a = 0.725858 + 1.187980I$ $b = -1.244680 + 0.659147I$	$9.51415 - 2.44072I$	$5.50124 + 2.26022I$
$u = -1.107540 - 0.627422I$ $a = -0.974699 - 0.995211I$ $b = 1.183370 - 0.002215I$	$9.51415 - 2.44072I$	$5.50124 + 2.26022I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.197871 + 0.665613I$ $a = 0.544098 + 0.505503I$ $b = -0.506495 + 0.897042I$	$1.83491 - 2.17307I$	$2.44305 + 0.96656I$
$u = -0.197871 + 0.665613I$ $a = 2.11053 - 0.83148I$ $b = -1.074320 + 0.072465I$	$1.83491 - 2.17307I$	$2.44305 + 0.96656I$
$u = -0.197871 - 0.665613I$ $a = 0.544098 - 0.505503I$ $b = -0.506495 - 0.897042I$	$1.83491 + 2.17307I$	$2.44305 - 0.96656I$
$u = -0.197871 - 0.665613I$ $a = 2.11053 + 0.83148I$ $b = -1.074320 - 0.072465I$	$1.83491 + 2.17307I$	$2.44305 - 0.96656I$
$u = -1.47309$ $a = 0.960868 + 0.116818I$ $b = -0.725226 - 0.147080I$	$2.06794$	$-0.326150$
$u = -1.47309$ $a = 0.960868 - 0.116818I$ $b = -0.725226 + 0.147080I$	$2.06794$	$-0.326150$
$u = 1.53037$ $a = 0.142205 + 0.666213I$ $b = 0.518363 + 0.759712I$	$-5.45448$	$-3.70880$
$u = 1.53037$ $a = 0.142205 - 0.666213I$ $b = 0.518363 - 0.759712I$	$-5.45448$	$-3.70880$
$u = -1.54061 + 0.22982I$ $a = 0.308882 + 0.905973I$ $b = 0.028277 + 0.455528I$	$-3.33520 + 5.64987I$	$-0.48217 - 4.54553I$
$u = -1.54061 + 0.22982I$ $a = -0.757657 + 1.082380I$ $b = 1.133770 + 0.656888I$	$-3.33520 + 5.64987I$	$-0.48217 - 4.54553I$



Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.54061 - 0.22982I$		
$a = 0.308882 - 0.905973I$	$-3.33520 - 5.64987I$	$-0.48217 + 4.54553I$
$b = 0.028277 - 0.455528I$		
$u = -1.54061 - 0.22982I$		
$a = -0.757657 - 1.082380I$	$-3.33520 - 5.64987I$	$-0.48217 + 4.54553I$
$b = 1.133770 - 0.656888I$		
$u = -0.270030$		
$a = 1.05107 + 3.12255I$	$6.94627$	$7.14740$
$b = 0.970434 + 0.909500I$		
$u = -0.270030$		
$a = 1.05107 - 3.12255I$	$6.94627$	$7.14740$
$b = 0.970434 - 0.909500I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$(u^4 - u^3 - 2u^2 - 4u + 1)(u^{20} + 3u^{19} + \dots + 7u + 1)$ $\cdot (u^{24} - 6u^{23} + \dots + 10u + 1)(u^{54} - 9u^{53} + \dots - 817482u + 44911)$
$c_2, c_7$	$(u^4 - 2u^3 + 3u - 1)(u^{20} - 3u^{18} + \dots - 2u - 1)(u^{24} - u^{23} + \dots + u^2 + 1)$ $\cdot (u^{54} - 2u^{53} + \dots - 7504u + 1667)$
$c_3$	$(u^4 - 6u^3 + 12u^2 - 11u + 5)(u^{12} + 3u^{11} + \dots + 4u + 1)^2$ $\cdot (u^{20} - 9u^{19} + \dots - 101u - 44)(u^{27} + 4u^{26} + \dots - 16u + 1)^2$
$c_4$	$(u^4 - u^3 - 2u + 1)(u^{20} - u^{19} + \dots + u - 1)(u^{24} + 10u^{22} + \dots + 8u + 1)$ $\cdot (u^{54} + 3u^{53} + \dots - 7068u + 1763)$
$c_5$	$(u^4 - 5u^3 + 6u^2 + 2u - 5)(u^{12} + 5u^{11} + \dots - u + 1)^2$ $\cdot (u^{20} + 4u^{19} + \dots + 371u + 44)(u^{27} - 2u^{26} + \dots - 67u + 47)^2$
$c_6, c_{10}$	$(u^4 + 2u^3 - 3u - 1)(u^{20} - 3u^{18} + \dots - 2u - 1)(u^{24} + u^{23} + \dots + u^2 + 1)$ $\cdot (u^{54} - 2u^{53} + \dots - 7504u + 1667)$
$c_8, c_{11}$	$(u^4 + u^3 + 2u + 1)(u^{20} - u^{19} + \dots + u - 1)(u^{24} + 10u^{22} + \dots - 8u + 1)$ $\cdot (u^{54} + 3u^{53} + \dots - 7068u + 1763)$
$c_{12}$	$(u^4 + u^3 - 2u^2 + 4u + 1)(u^{20} + 3u^{19} + \dots + 7u + 1)$ $\cdot (u^{24} + 6u^{23} + \dots - 10u + 1)(u^{54} - 9u^{53} + \dots - 817482u + 44911)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_9, c_{12}$	$(y^4 - 5y^3 - 2y^2 - 20y + 1)(y^{20} - 31y^{19} + \dots - 53y + 1)$ $\cdot (y^{24} - 12y^{23} + \dots - 22y + 1)$ $\cdot (y^{54} - 53y^{53} + \dots + 26272962362y + 2016997921)$
$c_2, c_6, c_7$ $c_{10}$	$(y^4 - 4y^3 + 10y^2 - 9y + 1)(y^{20} - 6y^{19} + \dots - 2y + 1)$ $\cdot (y^{24} - 7y^{23} + \dots + 2y + 1)$ $\cdot (y^{54} - 28y^{53} + \dots - 34895734y + 2778889)$
$c_3$	$(y^4 - 12y^3 + 22y^2 - y + 25)(y^{12} - 13y^{11} + \dots - 16y + 1)^2$ $\cdot (y^{20} - 29y^{19} + \dots - 23841y + 1936)(y^{27} - 30y^{26} + \dots + 108y - 1)^2$
$c_4, c_8, c_{11}$	$(y^4 - y^3 - 2y^2 - 4y + 1)(y^{20} + 9y^{19} + \dots + 3y + 1)$ $\cdot (y^{24} + 20y^{23} + \dots - 12y + 1)$ $\cdot (y^{54} + 27y^{53} + \dots + 38637652y + 3108169)$
$c_5$	$(y^4 - 13y^3 + 46y^2 - 64y + 25)(y^{12} - 11y^{11} + \dots - 15y + 1)^2$ $\cdot (y^{20} - 22y^{19} + \dots - 10041y + 1936)$ $\cdot (y^{27} - 20y^{26} + \dots + 14171y - 2209)^2$