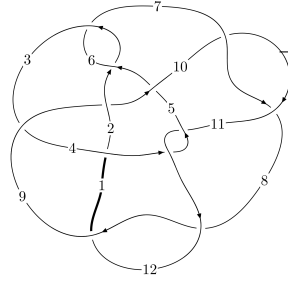
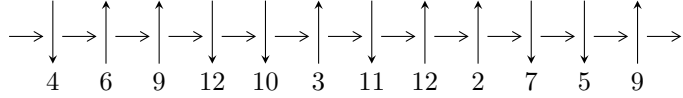


12n<sub>0782</sub> (K12n<sub>0782</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,9 \xrightarrow{c_3} 4,6 \xrightarrow{c_6} 7 \xrightarrow{c_2} 2 \xrightarrow{c_9} 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5 \xrightarrow{c_{12}} 12 \xrightarrow{c_8} 8 \twoheadrightarrow c_4, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 5.27881 \times 10^{88} u^{57} - 4.69361 \times 10^{90} u^{56} + \dots + 1.36590 \times 10^{92} b - 5.88184 \times 10^{92}, \\ - 2.96745 \times 10^{93} u^{57} - 2.47917 \times 10^{93} u^{56} + \dots + 8.04515 \times 10^{94} a + 3.43955 \times 10^{95}, \\ u^{58} + u^{57} + \dots - 223u + 38 \rangle$$

$$I_2^u = \langle 475169u^{17} + 381386u^{16} + \dots + 522553b + 471664, \\ - 688088u^{17} - 1519820u^{16} + \dots + 2612765a - 1890667, u^{18} + 15u^{16} + \dots - 6u + 5 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 76 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 5.28 \times 10^{88} u^{57} - 4.69 \times 10^{90} u^{56} + \dots + 1.37 \times 10^{92} b - 5.88 \times 10^{92}, -2.97 \times 10^{93} u^{57} - 2.48 \times 10^{93} u^{56} + \dots + 8.05 \times 10^{94} a + 3.44 \times 10^{95}, u^{58} + u^{57} + \dots - 223u + 38 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0368850u^{57} + 0.0308157u^{56} + \dots + 41.2134u - 4.27531 \\ -0.000386471u^{57} + 0.0343628u^{56} + \dots - 23.7709u + 4.30620 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0364985u^{57} + 0.0651785u^{56} + \dots + 17.4426u + 0.0308943 \\ -0.000386471u^{57} + 0.0343628u^{56} + \dots - 23.7709u + 4.30620 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0405848u^{57} + 0.0585166u^{56} + \dots + 63.4140u - 5.65068 \\ -0.0519284u^{57} - 0.0695194u^{56} + \dots - 12.5917u + 0.686208 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.106783u^{57} - 0.120253u^{56} + \dots - 87.1353u + 3.59553 \\ 0.0335600u^{57} + 0.0556513u^{56} + \dots + 0.799424u + 0.951777 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.00494700u^{57} + 0.0479532u^{56} + \dots - 57.8669u + 5.20437 \\ 0.0678161u^{57} + 0.0966838u^{56} + \dots - 15.7287u + 4.42152 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.00916084u^{57} - 0.0269986u^{56} + \dots + 53.2788u - 5.64588 \\ -0.0924440u^{57} - 0.175276u^{56} + \dots - 6.50545u - 0.673036 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.00126585u^{57} + 0.0187770u^{56} + \dots - 50.5853u + 14.2462 \\ 0.0175336u^{57} + 0.00565385u^{56} + \dots - 1.20624u + 0.716555 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.00916084u^{57} - 0.0269986u^{56} + \dots + 53.2788u - 5.64588 \\ -0.0497456u^{57} - 0.0855152u^{56} + \dots - 10.1352u + 0.00479944 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0258619u^{57} + 0.106305u^{56} + \dots + 55.7975u - 1.95424 \\ -0.0553761u^{57} + 0.0473162u^{56} + \dots - 29.4845u + 3.10494 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.0872911u^{57} - 0.355385u^{56} + \dots + 59.4278u - 12.0616$

(iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing             |
|---------------|--|
| $c_1$         | $u^{58} - 8u^{57} + \dots - 59912u + 5747$ |
| $c_2, c_6$    | $u^{58} - 13u^{56} + \dots - 638u + 247$   |
| $c_3$         | $u^{58} - u^{57} + \dots + 223u + 38$      |
| $c_4, c_{11}$ | $u^{58} + 2u^{57} + \dots - 4u + 47$       |
| $c_5$         | $u^{58} - u^{57} + \dots - 155u + 118$     |
| $c_7, c_{10}$ | $u^{58} + 3u^{57} + \dots + 410u + 25$     |
| $c_8, c_{12}$ | $u^{58} + 45u^{56} + \dots + 1851u + 269$  |
| $c_9$         | $u^{58} - u^{57} + \dots - 22u + 97$       |

(v) Riley Polynomials at the component

| Crossings     | Riley Polynomials at each crossing                  |
|---------------|---|
| $c_1$         | $y^{58} - 84y^{57} + \dots + 622723954y + 33028009$ |
| $c_2, c_6$    | $y^{58} - 26y^{57} + \dots - 629838y + 61009$       |
| $c_3$         | $y^{58} + 75y^{57} + \dots + 81523y + 1444$         |
| $c_4, c_{11}$ | $y^{58} + 2y^{57} + \dots + 4120y + 2209$           |
| $c_5$         | $y^{58} + 31y^{57} + \dots + 80523y + 13924$        |
| $c_7, c_{10}$ | $y^{58} - 53y^{57} + \dots - 18700y + 625$          |
| $c_8, c_{12}$ | $y^{58} + 90y^{57} + \dots + 3009893y + 72361$      |
| $c_9$         | $y^{58} - 23y^{57} + \dots - 9020y + 9409$          |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = 0.853751 + 0.464332I$<br>$a = -0.0493088 - 0.0773017I$<br>$b = 0.203439 - 1.110150I$ | $-2.63383 + 3.87803I$                 | $0. - 7.10067I$       |
| $u = 0.853751 - 0.464332I$<br>$a = -0.0493088 + 0.0773017I$<br>$b = 0.203439 + 1.110150I$ | $-2.63383 - 3.87803I$                 | $0. + 7.10067I$       |
| $u = -1.062870 + 0.155680I$<br>$a = 1.383060 + 0.177575I$<br>$b = -1.287020 + 0.256764I$  | $3.11643 - 0.54489I$                  | $0$                   |
| $u = -1.062870 - 0.155680I$<br>$a = 1.383060 - 0.177575I$<br>$b = -1.287020 - 0.256764I$  | $3.11643 + 0.54489I$                  | $0$                   |
| $u = -0.112581 + 0.912921I$<br>$a = 0.15835 + 1.82362I$<br>$b = -0.965630 + 0.677508I$    | $6.95013 - 2.72728I$                  | $5.05992 + 2.76752I$  |
| $u = -0.112581 - 0.912921I$<br>$a = 0.15835 - 1.82362I$<br>$b = -0.965630 - 0.677508I$    | $6.95013 + 2.72728I$                  | $5.05992 - 2.76752I$  |
| $u = -0.084433 + 0.832538I$<br>$a = 0.0357940 + 0.0140818I$<br>$b = 1.140920 - 0.525982I$ | $-0.82014 - 4.75740I$                 | $-0.14886 + 5.79153I$ |
| $u = -0.084433 - 0.832538I$<br>$a = 0.0357940 - 0.0140818I$<br>$b = 1.140920 + 0.525982I$ | $-0.82014 + 4.75740I$                 | $-0.14886 - 5.79153I$ |
| $u = 0.782245 + 0.038291I$<br>$a = -1.99589 - 0.35305I$<br>$b = 1.222820 + 0.263072I$     | $4.17334 + 3.33228I$                  | $6.92799 - 6.82937I$  |
| $u = 0.782245 - 0.038291I$<br>$a = -1.99589 + 0.35305I$<br>$b = 1.222820 - 0.263072I$     | $4.17334 - 3.33228I$                  | $6.92799 + 6.82937I$  |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 0.099784 + 1.239980I$<br>$a = 0.46372 - 1.67392I$<br>$b = -0.933454 - 0.370814I$    | $1.66999 + 1.54564I$                  | 0          |
| $u = 0.099784 - 1.239980I$<br>$a = 0.46372 + 1.67392I$<br>$b = -0.933454 + 0.370814I$    | $1.66999 - 1.54564I$                  | 0          |
| $u = -0.014033 + 1.261280I$<br>$a = 0.753664 - 0.681102I$<br>$b = -0.889945 - 0.068116I$ | $0.047703 + 0.198149I$                | 0          |
| $u = -0.014033 - 1.261280I$<br>$a = 0.753664 + 0.681102I$<br>$b = -0.889945 + 0.068116I$ | $0.047703 - 0.198149I$                | 0          |
| $u = -0.450292 + 1.192360I$<br>$a = -0.624837 - 0.475798I$<br>$b = 1.338790 - 0.213313I$ | $-0.33330 - 4.75057I$                 | 0          |
| $u = -0.450292 - 1.192360I$<br>$a = -0.624837 + 0.475798I$<br>$b = 1.338790 + 0.213313I$ | $-0.33330 + 4.75057I$                 | 0          |
| $u = 0.003350 + 1.288710I$<br>$a = -0.209714 - 0.410378I$<br>$b = 0.136782 - 1.254630I$  | $-4.85427 - 1.06680I$                 | 0          |
| $u = 0.003350 - 1.288710I$<br>$a = -0.209714 + 0.410378I$<br>$b = 0.136782 + 1.254630I$  | $-4.85427 + 1.06680I$                 | 0          |
| $u = 0.314738 + 1.298090I$<br>$a = 1.025510 - 0.858022I$<br>$b = -1.39942 - 0.56356I$    | $0.00633 + 7.27891I$                  | 0          |
| $u = 0.314738 - 1.298090I$<br>$a = 1.025510 + 0.858022I$<br>$b = -1.39942 + 0.56356I$    | $0.00633 - 7.27891I$                  | 0          |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -1.123890 + 0.727662I$<br>$a = -1.289100 - 0.536945I$<br>$b = 1.288900 - 0.578954I$ | $0.86445 - 9.82160I$                  | 0                     |
| $u = -1.123890 - 0.727662I$<br>$a = -1.289100 + 0.536945I$<br>$b = 1.288900 + 0.578954I$ | $0.86445 + 9.82160I$                  | 0                     |
| $u = 0.460864 + 0.418666I$<br>$a = 0.57224 - 1.90811I$<br>$b = 0.385032 - 0.536811I$     | $-3.08131 + 0.52947I$                 | $-3.73900 + 2.26505I$ |
| $u = 0.460864 - 0.418666I$<br>$a = 0.57224 + 1.90811I$<br>$b = 0.385032 + 0.536811I$     | $-3.08131 - 0.52947I$                 | $-3.73900 - 2.26505I$ |
| $u = -0.124818 + 0.519430I$<br>$a = -1.71837 - 1.68133I$<br>$b = 0.919845 + 0.470366I$   | $8.22063 + 1.95332I$                  | $-4.24227 - 5.07597I$ |
| $u = -0.124818 - 0.519430I$<br>$a = -1.71837 + 1.68133I$<br>$b = 0.919845 - 0.470366I$   | $8.22063 - 1.95332I$                  | $-4.24227 + 5.07597I$ |
| $u = 0.22485 + 1.46017I$<br>$a = 0.043124 - 0.507703I$<br>$b = 0.579349 - 0.997182I$     | $-5.11981 - 0.34192I$                 | 0                     |
| $u = 0.22485 - 1.46017I$<br>$a = 0.043124 + 0.507703I$<br>$b = 0.579349 + 0.997182I$     | $-5.11981 + 0.34192I$                 | 0                     |
| $u = 0.164082 + 0.484192I$<br>$a = 1.39498 - 2.02846I$<br>$b = -1.157090 - 0.710262I$    | $0.25031 + 5.18394I$                  | $-0.05460 - 3.88348I$ |
| $u = 0.164082 - 0.484192I$<br>$a = 1.39498 + 2.02846I$<br>$b = -1.157090 + 0.710262I$    | $0.25031 - 5.18394I$                  | $-0.05460 + 3.88348I$ |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = 0.10703 + 1.51586I$<br>$a = 1.05246 + 1.33886I$<br>$b = -0.837740 + 0.446217I$      | $-9.50824 + 2.34060I$                 | 0                    |
| $u = 0.10703 - 1.51586I$<br>$a = 1.05246 - 1.33886I$<br>$b = -0.837740 - 0.446217I$      | $-9.50824 - 2.34060I$                 | 0                    |
| $u = -0.03559 + 1.53038I$<br>$a = 0.256243 + 0.650105I$<br>$b = 0.747820 + 1.090540I$    | $-8.19348 + 0.77858I$                 | 0                    |
| $u = -0.03559 - 1.53038I$<br>$a = 0.256243 - 0.650105I$<br>$b = 0.747820 - 1.090540I$    | $-8.19348 - 0.77858I$                 | 0                    |
| $u = 0.06553 + 1.55280I$<br>$a = -0.549374 + 1.215700I$<br>$b = 1.141090 + 0.801942I$    | $-6.78133 + 6.11938I$                 | 0                    |
| $u = 0.06553 - 1.55280I$<br>$a = -0.549374 - 1.215700I$<br>$b = 1.141090 - 0.801942I$    | $-6.78133 - 6.11938I$                 | 0                    |
| $u = -0.190141 + 0.387639I$<br>$a = 0.446972 - 0.550746I$<br>$b = -0.192799 + 0.357060I$ | $0.080144 - 0.948408I$                | $1.62310 + 7.11083I$ |
| $u = -0.190141 - 0.387639I$<br>$a = 0.446972 + 0.550746I$<br>$b = -0.192799 - 0.357060I$ | $0.080144 + 0.948408I$                | $1.62310 - 7.11083I$ |
| $u = 0.32626 + 1.55223I$<br>$a = -0.241997 + 0.425422I$<br>$b = -0.520923 + 1.219600I$   | $-9.24266 + 8.26916I$                 | 0                    |
| $u = 0.32626 - 1.55223I$<br>$a = -0.241997 - 0.425422I$<br>$b = -0.520923 - 1.219600I$   | $-9.24266 - 8.26916I$                 | 0                    |



| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = -0.26330 + 1.59853I$<br>$a = -0.745743 - 1.025400I$<br>$b = 1.115300 - 0.653239I$    | $-3.26110 - 5.59088I$                 | 0                    |
| $u = -0.26330 - 1.59853I$<br>$a = -0.745743 + 1.025400I$<br>$b = 1.115300 + 0.653239I$    | $-3.26110 + 5.59088I$                 | 0                    |
| $u = -0.08919 + 1.63634I$<br>$a = -0.271146 + 0.443919I$<br>$b = -0.871244 + 0.410826I$   | $-9.42034 - 5.91809I$                 | 0                    |
| $u = -0.08919 - 1.63634I$<br>$a = -0.271146 - 0.443919I$<br>$b = -0.871244 - 0.410826I$   | $-9.42034 + 5.91809I$                 | 0                    |
| $u = -0.061244 + 0.334869I$<br>$a = -1.148350 - 0.458209I$<br>$b = -0.615190 - 1.052660I$ | $-1.66078 + 1.21898I$                 | $2.81157 + 3.35584I$ |
| $u = -0.061244 - 0.334869I$<br>$a = -1.148350 + 0.458209I$<br>$b = -0.615190 + 1.052660I$ | $-1.66078 - 1.21898I$                 | $2.81157 - 3.35584I$ |
| $u = -0.36544 + 1.64783I$<br>$a = 0.783570 + 1.030920I$<br>$b = -1.25562 + 0.75255I$      | $-6.7816 - 15.2640I$                  | 0                    |
| $u = -0.36544 - 1.64783I$<br>$a = 0.783570 - 1.030920I$<br>$b = -1.25562 - 0.75255I$      | $-6.7816 + 15.2640I$                  | 0                    |
| $u = 0.27885 + 1.66834I$<br>$a = -1.15451 + 0.99467I$<br>$b = 0.909700 + 0.469646I$       | $-9.60927 + 6.45837I$                 | 0                    |
| $u = 0.27885 - 1.66834I$<br>$a = -1.15451 - 0.99467I$<br>$b = 0.909700 - 0.469646I$       | $-9.60927 - 6.45837I$                 | 0                    |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = -0.18362 + 1.69215I$<br>$a = 0.093625 + 0.232044I$<br>$b = 0.763246 + 0.498750I$  | $-10.07870 - 2.49709I$                | 0                    |
| $u = -0.18362 - 1.69215I$<br>$a = 0.093625 - 0.232044I$<br>$b = 0.763246 - 0.498750I$  | $-10.07870 + 2.49709I$                | 0                    |
| $u = 0.37845 + 1.71205I$<br>$a = 0.706342 - 0.499000I$<br>$b = -0.905333 - 0.120347I$  | $-0.134835 + 0.852804I$               | 0                    |
| $u = 0.37845 - 1.71205I$<br>$a = 0.706342 + 0.499000I$<br>$b = -0.905333 + 0.120347I$  | $-0.134835 - 0.852804I$               | 0                    |
| $u = 0.140544 + 0.178449I$<br>$a = -6.15520 + 5.78279I$<br>$b = 0.906472 - 0.175526I$  | $5.16615 - 0.70559I$                  | $5.44585 - 4.12571I$ |
| $u = 0.140544 - 0.178449I$<br>$a = -6.15520 - 5.78279I$<br>$b = 0.906472 + 0.175526I$  | $5.16615 + 0.70559I$                  | $5.44585 + 4.12571I$ |
| $u = -0.53888 + 1.87728I$<br>$a = 0.760193 - 0.092180I$<br>$b = -0.968080 - 0.226728I$ | $0.106752 + 0.734447I$                | 0                    |
| $u = -0.53888 - 1.87728I$<br>$a = 0.760193 + 0.092180I$<br>$b = -0.968080 + 0.226728I$ | $0.106752 - 0.734447I$                | 0                    |

**II.**

$$I_2^u = \langle 4.75 \times 10^5 u^{17} + 3.81 \times 10^5 u^{16} + \dots + 5.23 \times 10^5 b + 4.72 \times 10^5, -6.88 \times 10^5 u^{17} - 1.52 \times 10^6 u^{16} + \dots + 2.61 \times 10^6 a - 1.89 \times 10^6, u^{18} + 15u^{16} + \dots - 6u + 5 \rangle$$

**(i) Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.263356u^{17} + 0.581690u^{16} + \dots + 6.31256u + 0.723627 \\ -0.909322u^{17} - 0.729851u^{16} + \dots - 3.71667u - 0.902615 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.645966u^{17} - 0.148161u^{16} + \dots + 2.59588u - 0.178988 \\ -0.909322u^{17} - 0.729851u^{16} + \dots - 3.71667u - 0.902615 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.438599u^{17} - 1.04958u^{16} + \dots + 8.33106u - 1.44807 \\ 1.21931u^{17} - 1.02358u^{16} + \dots + 6.40039u - 4.90381 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.292901u^{17} + 0.539668u^{16} + \dots - 11.1573u + 0.328021 \\ -0.421190u^{17} + 0.836061u^{16} + \dots - 0.273739u + 3.38165 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.838553u^{17} + 1.62104u^{16} + \dots - 13.6838u + 2.62121 \\ -0.360666u^{17} + 1.17548u^{16} + \dots - 0.934409u + 3.26121 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1.03879u^{17} - 0.114254u^{16} + \dots + 6.24100u - 1.10401 \\ 2.15736u^{17} + 1.13651u^{16} + \dots + 3.78942u - 0.227208 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1.03604u^{17} + 0.677147u^{16} + \dots + 0.313120u + 5.40611 \\ 0.552819u^{17} + 0.423534u^{16} + \dots + 1.35440u - 0.433577 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1.03879u^{17} - 0.114254u^{16} + \dots + 6.24100u - 1.10401 \\ 0.600192u^{17} + 0.935321u^{16} + \dots - 2.09006u + 0.344065 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.337287u^{17} - 2.39152u^{16} + \dots + 13.1418u - 7.78875 \\ 0.219099u^{17} - 1.77164u^{16} + \dots + 6.41323u - 6.77742 \end{pmatrix} \end{aligned}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes** =  $-\frac{2079650}{522553}u^{17} - \frac{452334}{522553}u^{16} + \dots - \frac{15376048}{522553}u + \frac{7059214}{522553}$

(iv)  $u$ -Polynomials at the component

| Crossings | u-Polynomials at each crossing         |
|-----------|--|
| $c_1$     | $u^{18} - 3u^{17} + \dots + 2u + 1$    |
| $c_2$     | $u^{18} - u^{17} + \dots - 2u + 1$     |
| $c_3$     | $u^{18} + 15u^{16} + \dots - 6u + 5$   |
| $c_4$     | $u^{18} - u^{17} + \dots + 4u^2 + 1$   |
| $c_5$     | $u^{18} + 11u^{16} + \dots - 2u + 5$   |
| $c_6$     | $u^{18} + u^{17} + \dots + 2u + 1$     |
| $c_7$     | $u^{18} + 2u^{17} + \dots + 16u^2 + 7$ |
| $c_8$     | $u^{18} - u^{17} + \dots - 5u + 1$     |
| $c_9$     | $u^{18} + 4u^{17} + \dots + 8u + 1$    |
| $c_{10}$  | $u^{18} - 2u^{17} + \dots + 16u^2 + 7$ |
| $c_{11}$  | $u^{18} + u^{17} + \dots + 4u^2 + 1$   |
| $c_{12}$  | $u^{18} + u^{17} + \dots + 5u + 1$     |



(v) Riley Polynomials at the component

| Crossings     | Riley Polynomials at each crossing      |
|---------------|---|
| $c_1$         | $y^{18} - 13y^{17} + \dots - 22y + 1$   |
| $c_2, c_6$    | $y^{18} - 7y^{17} + \dots + 2y + 1$     |
| $c_3$         | $y^{18} + 30y^{17} + \dots + 264y + 25$ |
| $c_4, c_{11}$ | $y^{18} + 13y^{17} + \dots + 8y + 1$    |
| $c_5$         | $y^{18} + 22y^{17} + \dots + 166y + 25$ |
| $c_7, c_{10}$ | $y^{18} - 18y^{17} + \dots + 224y + 49$ |
| $c_8, c_{12}$ | $y^{18} + 13y^{17} + \dots - 23y + 1$   |
| $c_9$         | $y^{18} - 16y^{17} + \dots - 16y + 1$   |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = 0.123064 + 1.252120I$<br>$a = 0.124206 - 1.294110I$<br>$b = -1.018510 - 0.849224I$ | $5.67755 + 3.28436I$                  | $-0.59775 - 3.64061I$ |
| $u = 0.123064 - 1.252120I$<br>$a = 0.124206 + 1.294110I$<br>$b = -1.018510 + 0.849224I$ | $5.67755 - 3.28436I$                  | $-0.59775 + 3.64061I$ |
| $u = -0.188606 + 1.266260I$<br>$a = -0.60866 - 1.59214I$<br>$b = 0.938103 - 0.153898I$  | $2.12876 - 0.69203I$                  | $6.40220 - 1.90887I$  |
| $u = -0.188606 - 1.266260I$<br>$a = -0.60866 + 1.59214I$<br>$b = 0.938103 + 0.153898I$  | $2.12876 + 0.69203I$                  | $6.40220 + 1.90887I$  |
| $u = -0.360505 + 1.231030I$<br>$a = -0.873740 - 0.802822I$<br>$b = 1.42199 - 0.68694I$  | $-0.69011 - 7.09449I$                 | $-4.20097 + 7.45897I$ |
| $u = -0.360505 - 1.231030I$<br>$a = -0.873740 + 0.802822I$<br>$b = 1.42199 + 0.68694I$  | $-0.69011 + 7.09449I$                 | $-4.20097 - 7.45897I$ |
| $u = 0.327917 + 0.627027I$<br>$a = 0.633937 - 0.499000I$<br>$b = -0.479081 - 0.805088I$ | $-1.92128 + 1.96048I$                 | $-1.19573 - 5.62148I$ |
| $u = 0.327917 - 0.627027I$<br>$a = 0.633937 + 0.499000I$<br>$b = -0.479081 + 0.805088I$ | $-1.92128 - 1.96048I$                 | $-1.19573 + 5.62148I$ |
| $u = 0.148616 + 1.285620I$<br>$a = 0.178421 - 0.531885I$<br>$b = 0.442168 - 1.232720I$  | $-4.20955 - 0.11620I$                 | $1.70521 - 1.04373I$  |
| $u = 0.148616 - 1.285620I$<br>$a = 0.178421 + 0.531885I$<br>$b = 0.442168 + 1.232720I$  | $-4.20955 + 0.11620I$                 | $1.70521 + 1.04373I$  |



| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.406284 + 0.439609I$<br>$a = 2.21319 + 2.32607I$<br>$b = -1.023940 + 0.328001I$ | $5.13345 - 1.40589I$                  | $4.79141 + 5.59291I$  |
| $u = -0.406284 - 0.439609I$<br>$a = 2.21319 - 2.32607I$<br>$b = -1.023940 - 0.328001I$ | $5.13345 + 1.40589I$                  | $4.79141 - 5.59291I$  |
| $u = 0.302439 + 0.399611I$<br>$a = -2.61290 + 1.39154I$<br>$b = 0.981313 - 0.425718I$  | $8.63907 - 1.80668I$                  | $13.61479 - 1.09393I$ |
| $u = 0.302439 - 0.399611I$<br>$a = -2.61290 - 1.39154I$<br>$b = 0.981313 + 0.425718I$  | $8.63907 + 1.80668I$                  | $13.61479 + 1.09393I$ |
| $u = 0.15623 + 1.60918I$<br>$a = 0.029868 + 0.885546I$<br>$b = 0.182577 + 0.324170I$   | $-9.81955 + 4.31607I$                 | $-1.44430 - 2.37878I$ |
| $u = 0.15623 - 1.60918I$<br>$a = 0.029868 - 0.885546I$<br>$b = 0.182577 - 0.324170I$   | $-9.81955 - 4.31607I$                 | $-1.44430 + 2.37878I$ |
| $u = -0.10287 + 2.43450I$<br>$a = 0.815671 - 0.193645I$<br>$b = -0.944622 - 0.152003I$ | $-0.003534 + 0.615030I$               | $-5.0749 + 47.0439I$  |
| $u = -0.10287 - 2.43450I$<br>$a = 0.815671 + 0.193645I$<br>$b = -0.944622 + 0.152003I$ | $-0.003534 - 0.615030I$               | $-5.0749 - 47.0439I$  |

### III. u-Polynomials

| Crossings | u-Polynomials at each crossing  |
|-----------|---|
| $c_1$     | $(u^{18} - 3u^{17} + \dots + 2u + 1)(u^{58} - 8u^{57} + \dots - 59912u + 5747)$ |
| $c_2$     | $(u^{18} - u^{17} + \dots - 2u + 1)(u^{58} - 13u^{56} + \dots - 638u + 247)$    |
| $c_3$     | $(u^{18} + 15u^{16} + \dots - 6u + 5)(u^{58} - u^{57} + \dots + 223u + 38)$     |
| $c_4$     | $(u^{18} - u^{17} + \dots + 4u^2 + 1)(u^{58} + 2u^{57} + \dots - 4u + 47)$      |
| $c_5$     | $(u^{18} + 11u^{16} + \dots - 2u + 5)(u^{58} - u^{57} + \dots - 155u + 118)$    |
| $c_6$     | $(u^{18} + u^{17} + \dots + 2u + 1)(u^{58} - 13u^{56} + \dots - 638u + 247)$    |
| $c_7$     | $(u^{18} + 2u^{17} + \dots + 16u^2 + 7)(u^{58} + 3u^{57} + \dots + 410u + 25)$  |
| $c_8$     | $(u^{18} - u^{17} + \dots - 5u + 1)(u^{58} + 45u^{56} + \dots + 1851u + 269)$   |
| $c_9$     | $(u^{18} + 4u^{17} + \dots + 8u + 1)(u^{58} - u^{57} + \dots - 22u + 97)$       |
| $c_{10}$  | $(u^{18} - 2u^{17} + \dots + 16u^2 + 7)(u^{58} + 3u^{57} + \dots + 410u + 25)$  |
| $c_{11}$  | $(u^{18} + u^{17} + \dots + 4u^2 + 1)(u^{58} + 2u^{57} + \dots - 4u + 47)$      |
| $c_{12}$  | $(u^{18} + u^{17} + \dots + 5u + 1)(u^{58} + 45u^{56} + \dots + 1851u + 269)$   |

#### IV. Riley Polynomials

| Crossings     | Riley Polynomials at each crossing  |
|---------------|---|
| $c_1$         | $(y^{18} - 13y^{17} + \dots - 22y + 1)$ $\cdot (y^{58} - 84y^{57} + \dots + 622723954y + 33028009)$ |
| $c_2, c_6$    | $(y^{18} - 7y^{17} + \dots + 2y + 1)(y^{58} - 26y^{57} + \dots - 629838y + 61009)$                  |
| $c_3$         | $(y^{18} + 30y^{17} + \dots + 264y + 25)(y^{58} + 75y^{57} + \dots + 81523y + 1444)$                |
| $c_4, c_{11}$ | $(y^{18} + 13y^{17} + \dots + 8y + 1)(y^{58} + 2y^{57} + \dots + 4120y + 2209)$                     |
| $c_5$         | $(y^{18} + 22y^{17} + \dots + 166y + 25)(y^{58} + 31y^{57} + \dots + 80523y + 13924)$               |
| $c_7, c_{10}$ | $(y^{18} - 18y^{17} + \dots + 224y + 49)(y^{58} - 53y^{57} + \dots - 18700y + 625)$                 |
| $c_8, c_{12}$ | $(y^{18} + 13y^{17} + \dots - 23y + 1)(y^{58} + 90y^{57} + \dots + 3009893y + 72361)$               |
| $c_9$         | $(y^{18} - 16y^{17} + \dots - 16y + 1)(y^{58} - 23y^{57} + \dots - 9020y + 9409)$                   |