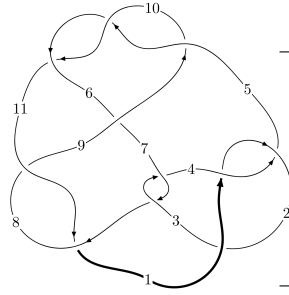
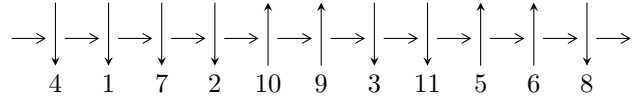


11a<sub>39</sub> (K11a<sub>39</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,10 \xrightarrow{c_5} 6 \xrightarrow{c_{10}} 2,11 \xrightarrow{c_4} 4 \xrightarrow{c_1} 1 \xrightarrow{c_9} 9 \xrightarrow{c_6} 7 \xrightarrow{c_3} 3 \xrightarrow{c_8} 8 \longrightarrow c_2, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{54} - u^{53} + \dots + b - 3u, -2u^{54} + 2u^{53} + \dots + a + 6u, u^{55} - 2u^{54} + \dots + 2u + 1 \rangle$$

$$I_2^u = \langle b + 1, u^3 + a - 2u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 60 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{54} - u^{53} + \dots + b - 3u, -2u^{54} + 2u^{53} + \dots + a + 6u, u^{55} - 2u^{54} + \dots + 2u + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^{54} - 2u^{53} + \dots + 13u^2 - 6u \\ -u^{54} + u^{53} + \dots - 2u^2 + 3u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{54} - u^{53} + \dots - 5u + 1 \\ -u^{54} + u^{53} + \dots - 3u^2 + 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^9 - 4u^7 + 5u^5 - 2u^3 + u \\ -u^{11} + 5u^9 - 8u^7 + 3u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 3u^{54} - 3u^{53} + \dots + 11u^2 - 7u \\ -u^{54} + u^{53} + \dots - u^2 + 3u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-2u^{54} + 4u^{53} + \dots + 3u - 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{55} - 6u^{54} + \dots - 8u + 1$
$c_2$	$u^{55} + 24u^{54} + \dots + 8u + 1$
$c_3, c_7$	$u^{55} + u^{54} + \dots + 64u + 32$
$c_5, c_9, c_{10}$	$u^{55} - 2u^{54} + \dots + 2u + 1$
$c_6$	$u^{55} + 6u^{54} + \dots + 302u + 77$
$c_8, c_{11}$	$u^{55} - 8u^{54} + \dots + 94u - 7$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{55} - 24y^{54} + \dots + 8y - 1$
$c_2$	$y^{55} + 20y^{54} + \dots - 220y - 1$
$c_3, c_7$	$y^{55} + 33y^{54} + \dots - 14848y - 1024$
$c_5, c_9, c_{10}$	$y^{55} - 52y^{54} + \dots + 14y - 1$
$c_6$	$y^{55} - 20y^{54} + \dots + 146490y - 5929$
$c_8, c_{11}$	$y^{55} + 48y^{54} + \dots + 4314y - 49$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.078520 + 0.133677I$ $a = 0.516431 + 0.026697I$ $b = 0.912992 + 0.503784I$	$1.55049 - 1.99776I$	0
$u = 1.078520 - 0.133677I$ $a = 0.516431 - 0.026697I$ $b = 0.912992 - 0.503784I$	$1.55049 + 1.99776I$	0
$u = -0.405577 + 0.698559I$ $a = 1.19426 - 1.95218I$ $b = 1.131320 + 0.693924I$	$4.79235 - 10.53540I$	$-0.79776 + 8.38025I$
$u = -0.405577 - 0.698559I$ $a = 1.19426 + 1.95218I$ $b = 1.131320 - 0.693924I$	$4.79235 + 10.53540I$	$-0.79776 - 8.38025I$
$u = -0.429702 + 0.678403I$ $a = -0.970506 + 0.157558I$ $b = 0.496725 - 0.933713I$	$6.73070 - 4.57214I$	$1.95904 + 4.03979I$
$u = -0.429702 - 0.678403I$ $a = -0.970506 - 0.157558I$ $b = 0.496725 + 0.933713I$	$6.73070 + 4.57214I$	$1.95904 - 4.03979I$
$u = -0.544877 + 0.580820I$ $a = -0.164386 + 0.526147I$ $b = 1.103900 - 0.704264I$	$5.32499 + 6.24906I$	$0.59828 - 2.50741I$
$u = -0.544877 - 0.580820I$ $a = -0.164386 - 0.526147I$ $b = 1.103900 + 0.704264I$	$5.32499 - 6.24906I$	$0.59828 + 2.50741I$
$u = -0.510509 + 0.609052I$ $a = 0.325943 - 1.106180I$ $b = 0.541319 + 0.917635I$	$7.04434 + 0.29231I$	$2.77654 + 2.24461I$
$u = -0.510509 - 0.609052I$ $a = 0.325943 + 1.106180I$ $b = 0.541319 - 0.917635I$	$7.04434 - 0.29231I$	$2.77654 - 2.24461I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.412834 + 0.641001I$ $a = -0.42450 - 2.15007I$ $b = -0.881787 + 0.589772I$	$1.48241 + 4.33310I$	$-1.64326 - 6.16138I$
$u = 0.412834 - 0.641001I$ $a = -0.42450 + 2.15007I$ $b = -0.881787 - 0.589772I$	$1.48241 - 4.33310I$	$-1.64326 + 6.16138I$
$u = 0.458268 + 0.584600I$ $a = 0.817122 + 0.781457I$ $b = -0.813432 - 0.582817I$	$1.70221 - 0.32794I$	$-0.771677 - 0.468923I$
$u = 0.458268 - 0.584600I$ $a = 0.817122 - 0.781457I$ $b = -0.813432 + 0.582817I$	$1.70221 + 0.32794I$	$-0.771677 + 0.468923I$
$u = -0.415395 + 0.603187I$ $a = -0.756841 + 1.109310I$ $b = -1.302130 + 0.031330I$	$0.07504 - 1.93289I$	$-0.05787 + 3.96687I$
$u = -0.415395 - 0.603187I$ $a = -0.756841 - 1.109310I$ $b = -1.302130 - 0.031330I$	$0.07504 + 1.93289I$	$-0.05787 - 3.96687I$
$u = -1.265410 + 0.116454I$ $a = -0.756900 - 0.079067I$ $b = -1.162780 + 0.205267I$	$0.59955 - 1.29811I$	0
$u = -1.265410 - 0.116454I$ $a = -0.756900 + 0.079067I$ $b = -1.162780 - 0.205267I$	$0.59955 + 1.29811I$	0
$u = 1.297170 + 0.044309I$ $a = 1.149320 + 0.636439I$ $b = -0.351487 - 0.343411I$	$2.99828 + 0.14721I$	0
$u = 1.297170 - 0.044309I$ $a = 1.149320 - 0.636439I$ $b = -0.351487 + 0.343411I$	$2.99828 - 0.14721I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.288550 + 0.158962I$ $a = -0.51700 - 2.28808I$ $b = -1.022630 + 0.390914I$	$1.08244 + 3.51008I$	0
$u = 1.288550 - 0.158962I$ $a = -0.51700 + 2.28808I$ $b = -1.022630 - 0.390914I$	$1.08244 - 3.51008I$	0
$u = -1.292250 + 0.245052I$ $a = 0.94579 - 1.66072I$ $b = 1.053490 + 0.579410I$	$3.09735 - 8.51931I$	0
$u = -1.292250 - 0.245052I$ $a = 0.94579 + 1.66072I$ $b = 1.053490 - 0.579410I$	$3.09735 + 8.51931I$	0
$u = 0.659363 + 0.177799I$ $a = 0.370767 + 0.659351I$ $b = 0.825967 - 0.561444I$	$1.63950 + 2.24198I$	$1.57550 - 4.32492I$
$u = 0.659363 - 0.177799I$ $a = 0.370767 - 0.659351I$ $b = 0.825967 + 0.561444I$	$1.63950 - 2.24198I$	$1.57550 + 4.32492I$
$u = 0.108922 + 0.669976I$ $a = 2.05168 + 0.39909I$ $b = 0.999297 - 0.553816I$	$-1.25442 + 5.19790I$	$-5.46768 - 6.87562I$
$u = 0.108922 - 0.669976I$ $a = 2.05168 - 0.39909I$ $b = 0.999297 + 0.553816I$	$-1.25442 - 5.19790I$	$-5.46768 + 6.87562I$
$u = 0.223843 + 0.635800I$ $a = 0.619795 + 0.836958I$ $b = 0.682905 + 0.426557I$	$-0.093506 + 0.957018I$	$-1.47250 - 1.22419I$
$u = 0.223843 - 0.635800I$ $a = 0.619795 - 0.836958I$ $b = 0.682905 - 0.426557I$	$-0.093506 - 0.957018I$	$-1.47250 + 1.22419I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.345750 + 0.196757I$ $a = -0.348002 + 0.275917I$ $b = 0.325642 - 0.591557I$	$4.93016 - 3.86526I$	0
$u = -1.345750 - 0.196757I$ $a = -0.348002 - 0.275917I$ $b = 0.325642 + 0.591557I$	$4.93016 + 3.86526I$	0
$u = -1.39666 + 0.23010I$ $a = -0.011407 - 0.386009I$ $b = 0.636512 - 0.224540I$	$5.07190 - 4.05462I$	0
$u = -1.39666 - 0.23010I$ $a = -0.011407 + 0.386009I$ $b = 0.636512 + 0.224540I$	$5.07190 + 4.05462I$	0
$u = -1.43083 + 0.02750I$ $a = -0.66190 - 1.48550I$ $b = 0.838321 + 0.728876I$	$7.99304 - 2.76322I$	0
$u = -1.43083 - 0.02750I$ $a = -0.66190 + 1.48550I$ $b = 0.838321 - 0.728876I$	$7.99304 + 2.76322I$	0
$u = 0.220263 + 0.502370I$ $a = 0.543936 + 0.221214I$ $b = 0.182425 + 0.252129I$	$-0.008201 + 1.198200I$	$-0.25143 - 5.38204I$
$u = 0.220263 - 0.502370I$ $a = 0.543936 - 0.221214I$ $b = 0.182425 - 0.252129I$	$-0.008201 - 1.198200I$	$-0.25143 + 5.38204I$
$u = -0.046404 + 0.536106I$ $a = -2.41342 + 1.29245I$ $b = -1.047030 - 0.274962I$	$-3.02612 - 0.98819I$	$-10.81757 + 0.62676I$
$u = -0.046404 - 0.536106I$ $a = -2.41342 - 1.29245I$ $b = -1.047030 + 0.274962I$	$-3.02612 + 0.98819I$	$-10.81757 - 0.62676I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.45734 + 0.22515I$ $a = 0.507704 - 0.942507I$ $b = -1.341850 - 0.047444I$	$6.09964 + 4.98197I$	0
$u = 1.45734 - 0.22515I$ $a = 0.507704 + 0.942507I$ $b = -1.341850 + 0.047444I$	$6.09964 - 4.98197I$	0
$u = -1.46520 + 0.21259I$ $a = 1.47883 - 1.30859I$ $b = -0.786253 + 0.638767I$	$7.88540 - 2.59431I$	0
$u = -1.46520 - 0.21259I$ $a = 1.47883 + 1.30859I$ $b = -0.786253 - 0.638767I$	$7.88540 + 2.59431I$	0
$u = -1.46151 + 0.23703I$ $a = 0.35860 + 2.60378I$ $b = -0.903696 - 0.627740I$	$7.52118 - 7.54900I$	0
$u = -1.46151 - 0.23703I$ $a = 0.35860 - 2.60378I$ $b = -0.903696 + 0.627740I$	$7.52118 + 7.54900I$	0
$u = 1.46676 + 0.25976I$ $a = 0.13179 + 2.56805I$ $b = 1.150220 - 0.701224I$	$10.8274 + 14.0334I$	0
$u = 1.46676 - 0.25976I$ $a = 0.13179 - 2.56805I$ $b = 1.150220 + 0.701224I$	$10.8274 - 14.0334I$	0
$u = 1.47287 + 0.24797I$ $a = -1.38353 - 1.05356I$ $b = 0.483891 + 0.966514I$	$12.8723 + 7.9548I$	0
$u = 1.47287 - 0.24797I$ $a = -1.38353 + 1.05356I$ $b = 0.483891 - 0.966514I$	$12.8723 - 7.9548I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.48811 + 0.18811I$ $a = -1.12025 - 1.22948I$ $b = 1.099520 + 0.737359I$	$11.90410 - 3.49537I$	0
$u = 1.48811 - 0.18811I$ $a = -1.12025 + 1.22948I$ $b = 1.099520 - 0.737359I$	$11.90410 + 3.49537I$	0
$u = 1.48611 + 0.20604I$ $a = -0.20805 + 1.92611I$ $b = 0.576460 - 0.947356I$	$13.50700 + 2.65879I$	0
$u = 1.48611 - 0.20604I$ $a = -0.20805 - 1.92611I$ $b = 0.576460 + 0.947356I$	$13.50700 - 2.65879I$	0
$u = -0.217641$ $a = 2.44944$ $b = -0.855618$	-1.24884	-7.99830

$$\text{II. } I_2^u = \langle b + 1, u^3 + a - 2u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 + 2u \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 + 2u + 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 + 2u + 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5u^3 + u^2 + 8u - 3$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^5$
$c_2, c_4$	$(u + 1)^5$
$c_3, c_7$	$u^5$
$c_5$	$u^5 - u^4 - 2u^3 + u^2 + u + 1$
$c_6$	$u^5 + 3u^4 + 4u^3 + u^2 - u - 1$
$c_8$	$u^5 + u^4 + 2u^3 + u^2 + u + 1$
$c_9, c_{10}$	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
$c_{11}$	$u^5 - u^4 + 2u^3 - u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^5$
$c_3, c_7$	$y^5$
$c_5, c_9, c_{10}$	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$
$c_6$	$y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$
$c_8, c_{11}$	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.21774$ $a = -0.629714$ $b = -1.00000$	0.756147	-2.23020
$u = -0.309916 + 0.549911I$ $a = -0.871221 + 1.107660I$ $b = -1.00000$	$-1.31583 - 1.53058I$	$-6.94263 + 4.09764I$
$u = -0.309916 - 0.549911I$ $a = -0.871221 - 1.107660I$ $b = -1.00000$	$-1.31583 + 1.53058I$	$-6.94263 - 4.09764I$
$u = 1.41878 + 0.21917I$ $a = 0.186078 - 0.874646I$ $b = -1.00000$	$4.22763 + 4.40083I$	$-2.94226 - 4.18967I$
$u = 1.41878 - 0.21917I$ $a = 0.186078 + 0.874646I$ $b = -1.00000$	$4.22763 - 4.40083I$	$-2.94226 + 4.18967I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^5)(u^{55} - 6u^{54} + \dots - 8u + 1)$
$c_2$	$((u + 1)^5)(u^{55} + 24u^{54} + \dots + 8u + 1)$
$c_3, c_7$	$u^5(u^{55} + u^{54} + \dots + 64u + 32)$
$c_4$	$((u + 1)^5)(u^{55} - 6u^{54} + \dots - 8u + 1)$
$c_5$	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)(u^{55} - 2u^{54} + \dots + 2u + 1)$
$c_6$	$(u^5 + 3u^4 + 4u^3 + u^2 - u - 1)(u^{55} + 6u^{54} + \dots + 302u + 77)$
$c_8$	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)(u^{55} - 8u^{54} + \dots + 94u - 7)$
$c_9, c_{10}$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)(u^{55} - 2u^{54} + \dots + 2u + 1)$
$c_{11}$	$(u^5 - u^4 + 2u^3 - u^2 + u - 1)(u^{55} - 8u^{54} + \dots + 94u - 7)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y - 1)^5)(y^{55} - 24y^{54} + \dots + 8y - 1)$
$c_2$	$((y - 1)^5)(y^{55} + 20y^{54} + \dots - 220y - 1)$
$c_3, c_7$	$y^5(y^{55} + 33y^{54} + \dots - 14848y - 1024)$
$c_5, c_9, c_{10}$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)(y^{55} - 52y^{54} + \dots + 14y - 1)$
$c_6$	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)(y^{55} - 20y^{54} + \dots + 146490y - 5929)$
$c_8, c_{11}$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)(y^{55} + 48y^{54} + \dots + 4314y - 49)$