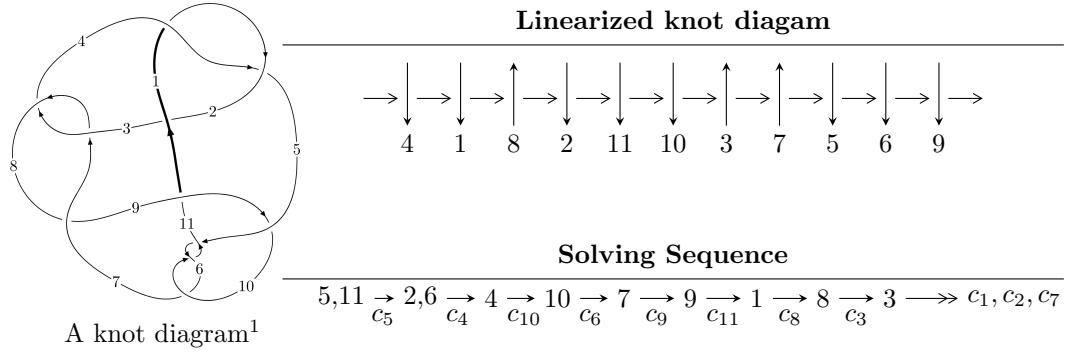


## $11a_{41}$ ( $K11a_{41}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$I_1^u = \langle u^{57} - u^{56} + \dots + b + 1, u^{59} - 2u^{58} + \dots + a + 3, u^{60} - 2u^{59} + \dots + 3u - 1 \rangle$$

$$I_2^u = \langle b + 1, u^2 + a - u + 3, u^3 - u^2 + 2u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 63 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{57} - u^{56} + \cdots + b + 1, \ u^{59} - 2u^{58} + \cdots + a + 3, \ u^{60} - 2u^{59} + \cdots + 3u - 1 \rangle^{\text{I.}}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{59} + 2u^{58} + \cdots + u - 3 \\ -u^{57} + u^{56} + \cdots + u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{59} + 2u^{58} + \cdots + 2u - 3 \\ -u^{57} + u^{56} + \cdots - 3u^3 - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^7 - 4u^5 - 4u^3 \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^9 + 4u^7 + 5u^5 + 2u^3 + u \\ u^{11} + 5u^9 + 8u^7 + 3u^5 - u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{59} + 2u^{58} + \cdots - u^2 - 2 \\ -u^{57} + u^{56} + \cdots + u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{59} + 2u^{58} + \cdots - u^2 - 2 \\ -u^{57} + u^{56} + \cdots + u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $u^{59} - 2u^{58} + \cdots + 8u - 3$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{60} - 4u^{59} + \cdots + 4u - 1$
$c_2$	$u^{60} + 32u^{59} + \cdots + 4u + 1$
$c_3, c_7$	$u^{60} + u^{59} + \cdots + 4u + 8$
$c_5, c_6, c_{10}$	$u^{60} - 2u^{59} + \cdots + 3u - 1$
$c_8$	$u^{60} - 21u^{59} + \cdots - 1040u + 64$
$c_9$	$u^{60} + 2u^{59} + \cdots + 3u - 1$
$c_{11}$	$u^{60} - 14u^{59} + \cdots - 1087u + 131$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{60} - 32y^{59} + \cdots - 4y + 1$
$c_2$	$y^{60} - 4y^{59} + \cdots - 32y + 1$
$c_3, c_7$	$y^{60} - 21y^{59} + \cdots - 1040y + 64$
$c_5, c_6, c_{10}$	$y^{60} + 54y^{59} + \cdots - 7y + 1$
$c_8$	$y^{60} + 31y^{59} + \cdots - 118016y + 4096$
$c_9$	$y^{60} - 2y^{59} + \cdots - 7y + 1$
$c_{11}$	$y^{60} + 10y^{59} + \cdots + 159609y + 17161$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.272258 + 1.012540I$		
$a = 1.93515 + 0.62774I$	$-2.04150 + 6.75419I$	$-6.05975 - 7.03761I$
$b = 1.147190 - 0.478763I$		
$u = -0.272258 - 1.012540I$		
$a = 1.93515 - 0.62774I$	$-2.04150 - 6.75419I$	$-6.05975 + 7.03761I$
$b = 1.147190 + 0.478763I$		
$u = -0.156290 + 1.052030I$		
$a = 0.095451 + 0.296346I$	$0.89236 + 2.41054I$	$-2.85789 - 3.50583I$
$b = 0.098316 + 0.688037I$		
$u = -0.156290 - 1.052030I$		
$a = 0.095451 - 0.296346I$	$0.89236 - 2.41054I$	$-2.85789 + 3.50583I$
$b = 0.098316 - 0.688037I$		
$u = 0.102597 + 0.926022I$		
$a = -1.92726 + 0.84189I$	$-2.71127 - 1.29749I$	$-7.32877 + 0.87949I$
$b = -1.169680 - 0.370214I$		
$u = 0.102597 - 0.926022I$		
$a = -1.92726 - 0.84189I$	$-2.71127 + 1.29749I$	$-7.32877 - 0.87949I$
$b = -1.169680 + 0.370214I$		
$u = 0.362204 + 0.739680I$		
$a = 1.398890 + 0.042352I$	$-1.51448 + 6.91671I$	$-4.99151 - 4.33152I$
$b = 1.157070 - 0.528981I$		
$u = 0.362204 - 0.739680I$		
$a = 1.398890 - 0.042352I$	$-1.51448 - 6.91671I$	$-4.99151 + 4.33152I$
$b = 1.157070 + 0.528981I$		
$u = 0.739190 + 0.273449I$		
$a = 2.83377 - 1.12471I$	$-3.14550 - 10.93560I$	$-7.60991 + 8.98761I$
$b = 1.183660 + 0.548618I$		
$u = 0.739190 - 0.273449I$		
$a = 2.83377 + 1.12471I$	$-3.14550 + 10.93560I$	$-7.60991 - 8.98761I$
$b = 1.183660 - 0.548618I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.705650 + 0.274949I$		
$a = -0.556763 - 0.943620I$	$-0.27172 - 5.84779I$	$-4.34743 + 6.06110I$
$b = 0.216325 - 0.833418I$		
$u = 0.705650 - 0.274949I$		
$a = -0.556763 + 0.943620I$	$-0.27172 + 5.84779I$	$-4.34743 - 6.06110I$
$b = 0.216325 + 0.833418I$		
$u = -0.739469 + 0.157117I$		
$a = 2.42529 + 0.98016I$	$-4.64706 - 2.94332I$	$-9.69548 + 3.11009I$
$b = 1.123680 + 0.435823I$		
$u = -0.739469 - 0.157117I$		
$a = 2.42529 - 0.98016I$	$-4.64706 + 2.94332I$	$-9.69548 - 3.11009I$
$b = 1.123680 - 0.435823I$		
$u = -0.701322 + 0.243359I$		
$a = -2.80040 - 1.59166I$	$-4.44900 + 4.80272I$	$-9.53100 - 5.34375I$
$b = -1.129360 + 0.462569I$		
$u = -0.701322 - 0.243359I$		
$a = -2.80040 + 1.59166I$	$-4.44900 - 4.80272I$	$-9.53100 + 5.34375I$
$b = -1.129360 - 0.462569I$		
$u = 0.691544 + 0.218830I$		
$a = -2.61676 + 0.96703I$	$-4.78959 - 2.10958I$	$-9.89618 + 4.41005I$
$b = -1.228960 + 0.314277I$		
$u = 0.691544 - 0.218830I$		
$a = -2.61676 - 0.96703I$	$-4.78959 + 2.10958I$	$-9.89618 - 4.41005I$
$b = -1.228960 - 0.314277I$		
$u = -0.150600 + 0.704962I$		
$a = -1.51108 + 0.72061I$	$-2.66735 - 1.26395I$	$-6.69853 + 0.15559I$
$b = -1.130100 - 0.383816I$		
$u = -0.150600 - 0.704962I$		
$a = -1.51108 - 0.72061I$	$-2.66735 + 1.26395I$	$-6.69853 - 0.15559I$
$b = -1.130100 + 0.383816I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.245563 + 1.262290I$		
$a = 1.207160 + 0.477268I$	$2.15190 + 3.30985I$	0
$b = 0.712663 - 0.173753I$		
$u = -0.245563 - 1.262290I$		
$a = 1.207160 - 0.477268I$	$2.15190 - 3.30985I$	0
$b = 0.712663 + 0.173753I$		
$u = 0.313312 + 0.634127I$		
$a = 0.406095 + 0.033528I$	$1.19086 + 2.11650I$	$-1.10142 - 0.94504I$
$b = 0.231815 + 0.743223I$		
$u = 0.313312 - 0.634127I$		
$a = 0.406095 - 0.033528I$	$1.19086 - 2.11650I$	$-1.10142 + 0.94504I$
$b = 0.231815 - 0.743223I$		
$u = 0.593362 + 0.375996I$		
$a = 1.44574 - 0.93956I$	$3.02257 - 4.24450I$	$-1.33904 + 7.25011I$
$b = 0.826187 + 0.623051I$		
$u = 0.593362 - 0.375996I$		
$a = 1.44574 + 0.93956I$	$3.02257 + 4.24450I$	$-1.33904 - 7.25011I$
$b = 0.826187 - 0.623051I$		
$u = -0.651026 + 0.178717I$		
$a = 0.833384 - 0.653334I$	$-1.64038 + 0.76431I$	$-6.82050 - 1.17334I$
$b = -0.075209 - 0.564522I$		
$u = -0.651026 - 0.178717I$		
$a = 0.833384 + 0.653334I$	$-1.64038 - 0.76431I$	$-6.82050 + 1.17334I$
$b = -0.075209 + 0.564522I$		
$u = 0.514134 + 0.433646I$		
$a = 0.120502 - 0.319390I$	$3.31167 + 0.60747I$	$0.058994 + 0.358835I$
$b = 0.725195 - 0.626130I$		
$u = 0.514134 - 0.433646I$		
$a = 0.120502 + 0.319390I$	$3.31167 - 0.60747I$	$0.058994 - 0.358835I$
$b = 0.725195 + 0.626130I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.667151$		
$a = 1.87106$	-1.74355	-3.65290
$b = 0.617384$		
$u = 0.146423 + 1.356920I$		
$a = -1.11641 + 0.87341I$	2.27680 - 1.86506I	0
$b = -1.211750 - 0.122488I$		
$u = 0.146423 - 1.356920I$		
$a = -1.11641 - 0.87341I$	2.27680 + 1.86506I	0
$b = -1.211750 + 0.122488I$		
$u = -0.298418 + 1.347350I$		
$a = 0.950662 + 0.883761I$	0.089664 + 0.805813I	0
$b = 1.102840 + 0.401160I$		
$u = -0.298418 - 1.347350I$		
$a = 0.950662 - 0.883761I$	0.089664 - 0.805813I	0
$b = 1.102840 - 0.401160I$		
$u = -0.112811 + 1.380760I$		
$a = 0.088761 + 1.367980I$	3.11222 - 0.32948I	0
$b = -0.973157 - 0.442087I$		
$u = -0.112811 - 1.380760I$		
$a = 0.088761 - 1.367980I$	3.11222 + 0.32948I	0
$b = -0.973157 + 0.442087I$		
$u = -0.181790 + 1.380090I$		
$a = 0.51009 - 1.34681I$	4.27304 + 3.48079I	0
$b = -0.578631 + 0.449363I$		
$u = -0.181790 - 1.380090I$		
$a = 0.51009 + 1.34681I$	4.27304 - 3.48079I	0
$b = -0.578631 - 0.449363I$		
$u = -0.252426 + 1.375440I$		
$a = 1.054820 + 0.112572I$	3.31453 + 4.03685I	0
$b = -0.213723 - 0.598525I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.252426 - 1.375440I$		
$a = 1.054820 - 0.112572I$	$3.31453 - 4.03685I$	0
$b = -0.213723 + 0.598525I$		
$u = 0.272964 + 1.386080I$		
$a = -1.045560 + 0.896556I$	$0.31494 - 5.61200I$	0
$b = -1.260740 + 0.293725I$		
$u = 0.272964 - 1.386080I$		
$a = -1.045560 - 0.896556I$	$0.31494 + 5.61200I$	0
$b = -1.260740 - 0.293725I$		
$u = -0.27784 + 1.39711I$		
$a = -1.46445 - 2.26687I$	$0.77544 + 8.36220I$	0
$b = -1.121330 + 0.494109I$		
$u = -0.27784 - 1.39711I$		
$a = -1.46445 + 2.26687I$	$0.77544 - 8.36220I$	0
$b = -1.121330 - 0.494109I$		
$u = 0.11177 + 1.42352I$		
$a = 0.003244 - 0.724114I$	$7.44712 + 0.69473I$	0
$b = 0.361594 + 0.782628I$		
$u = 0.11177 - 1.42352I$		
$a = 0.003244 + 0.724114I$	$7.44712 - 0.69473I$	0
$b = 0.361594 - 0.782628I$		
$u = 0.27859 + 1.41128I$		
$a = -0.929433 - 0.027526I$	$5.10898 - 9.43023I$	0
$b = 0.233048 - 0.870544I$		
$u = 0.27859 - 1.41128I$		
$a = -0.929433 + 0.027526I$	$5.10898 + 9.43023I$	0
$b = 0.233048 + 0.870544I$		
$u = 0.07750 + 1.43810I$		
$a = 0.274235 + 0.847102I$	$5.22134 + 5.76496I$	0
$b = 1.113070 - 0.571356I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.07750 - 1.43810I$		
$a = 0.274235 - 0.847102I$	$5.22134 - 5.76496I$	0
$b = 1.113070 + 0.571356I$		
$u = 0.29362 + 1.41349I$		
$a = 1.61836 - 1.90667I$	$2.2343 - 14.6854I$	0
$b = 1.192200 + 0.565015I$		
$u = 0.29362 - 1.41349I$		
$a = 1.61836 + 1.90667I$	$2.2343 + 14.6854I$	0
$b = 1.192200 - 0.565015I$		
$u = 0.19005 + 1.43268I$		
$a = -0.563532 + 0.432636I$	$9.23623 - 1.96231I$	0
$b = 0.708476 - 0.712296I$		
$u = 0.19005 - 1.43268I$		
$a = -0.563532 - 0.432636I$	$9.23623 + 1.96231I$	0
$b = 0.708476 + 0.712296I$		
$u = 0.22072 + 1.43184I$		
$a = 0.55993 - 1.54260I$	$8.80345 - 7.21631I$	0
$b = 0.857884 + 0.678909I$		
$u = 0.22072 - 1.43184I$		
$a = 0.55993 + 1.54260I$	$8.80345 + 7.21631I$	0
$b = 0.857884 - 0.678909I$		
$u = -0.434286 + 0.236524I$		
$a = 0.227567 - 1.379360I$	$-0.85637 + 1.13107I$	$-6.00125 - 6.01444I$
$b = -0.654919 + 0.246891I$		
$u = -0.434286 - 0.236524I$		
$a = 0.227567 + 1.379360I$	$-0.85637 - 1.13107I$	$-6.00125 + 6.01444I$
$b = -0.654919 - 0.246891I$		
$u = 0.388108$		
$a = -3.78596$	$-2.19031$	0.722320
$b = -1.10470$		

$$\text{II. } I_2^u = \langle b+1, u^2 + a - u + 3, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^2 + u - 3 \\ -1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^2 + u - 2 \\ -1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u^2 - u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^2 + 1 \\ u^2 - u + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^2 + 1 \\ u^2 - u + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^2 + 1 \\ u^2 - u + 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^2 + u - 2 \\ -1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^2 + u - 2 \\ -1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5u^2 + 4u - 16$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^3$
$c_2, c_4$	$(u + 1)^3$
$c_3, c_7, c_8$	$u^3$
$c_5, c_6$	$u^3 - u^2 + 2u - 1$
$c_9, c_{11}$	$u^3 - u^2 + 1$
$c_{10}$	$u^3 + u^2 + 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^3$
$c_3, c_7, c_8$	$y^3$
$c_5, c_6, c_{10}$	$y^3 + 3y^2 + 2y - 1$
$c_9, c_{11}$	$y^3 - y^2 + 2y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.215080 + 1.307140I$		
$a = -1.122560 + 0.744862I$	$1.37919 - 2.82812I$	$-6.82789 + 2.41717I$
$b = -1.00000$		
$u = 0.215080 - 1.307140I$		
$a = -1.122560 - 0.744862I$	$1.37919 + 2.82812I$	$-6.82789 - 2.41717I$
$b = -1.00000$		
$u = 0.569840$		
$a = -2.75488$	$-2.75839$	$-15.3440$
$b = -1.00000$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^3)(u^{60} - 4u^{59} + \cdots + 4u - 1)$
$c_2$	$((u + 1)^3)(u^{60} + 32u^{59} + \cdots + 4u + 1)$
$c_3, c_7$	$u^3(u^{60} + u^{59} + \cdots + 4u + 8)$
$c_4$	$((u + 1)^3)(u^{60} - 4u^{59} + \cdots + 4u - 1)$
$c_5, c_6$	$(u^3 - u^2 + 2u - 1)(u^{60} - 2u^{59} + \cdots + 3u - 1)$
$c_8$	$u^3(u^{60} - 21u^{59} + \cdots - 1040u + 64)$
$c_9$	$(u^3 - u^2 + 1)(u^{60} + 2u^{59} + \cdots + 3u - 1)$
$c_{10}$	$(u^3 + u^2 + 2u + 1)(u^{60} - 2u^{59} + \cdots + 3u - 1)$
$c_{11}$	$(u^3 - u^2 + 1)(u^{60} - 14u^{59} + \cdots - 1087u + 131)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y - 1)^3)(y^{60} - 32y^{59} + \dots - 4y + 1)$
$c_2$	$((y - 1)^3)(y^{60} - 4y^{59} + \dots - 32y + 1)$
$c_3, c_7$	$y^3(y^{60} - 21y^{59} + \dots - 1040y + 64)$
$c_5, c_6, c_{10}$	$(y^3 + 3y^2 + 2y - 1)(y^{60} + 54y^{59} + \dots - 7y + 1)$
$c_8$	$y^3(y^{60} + 31y^{59} + \dots - 118016y + 4096)$
$c_9$	$(y^3 - y^2 + 2y - 1)(y^{60} - 2y^{59} + \dots - 7y + 1)$
$c_{11}$	$(y^3 - y^2 + 2y - 1)(y^{60} + 10y^{59} + \dots + 159609y + 17161)$