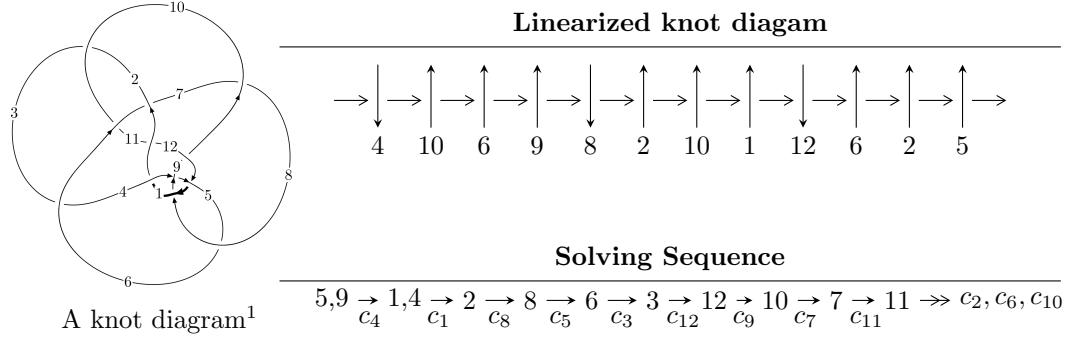


## $12n_{0839}$ ( $K12n_{0839}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle b - u, a - 1, u^9 - 5u^8 + 12u^7 - 16u^6 + 13u^5 - 6u^4 + 2u^3 - u^2 + 2u - 1 \rangle \\
 I_2^u &= \langle b + u, a + 1, u^9 - 3u^8 + 4u^7 - 2u^6 + u^5 - 2u^4 + 2u^3 - u^2 - 1 \rangle \\
 I_3^u &= \langle b - u, 4u^{17} + 8u^{16} + \dots + 2a - 5, u^{18} + 5u^{17} + \dots + 5u + 1 \rangle \\
 I_4^u &= \langle -12u^{17} - 44u^{16} + \dots + 2b - 4, a - 1, u^{18} + 5u^{17} + \dots + 5u + 1 \rangle \\
 I_5^u &= \langle -582u^{17} + 8001u^{16} + \dots + 6236b + 10944, -342u^{17} + 5232u^{16} + \dots + 6236a - 30, \\
 &\quad u^{18} - 17u^{17} + \dots - 176u + 32 \rangle \\
 I_6^u &= \langle b + u, -2u^7 - 5u^6 - 8u^5 - 9u^4 - 10u^3 - 7u^2 + a - 7u - 3, \\
 &\quad u^8 + 3u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 5u^2 + 3u + 1 \rangle \\
 I_7^u &= \langle u^7 + 2u^6 + 3u^5 + 4u^4 + 5u^3 + 3u^2 + b + 3u + 2, a + 1, u^8 + 3u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 5u^2 + 3u + 1 \rangle \\
 I_8^u &= \langle -au + b, -u^3 + a^2 + au + 4u^2 - 2a - 6u + 4, u^4 - 3u^3 + 3u^2 - u - 1 \rangle \\
 I_9^u &= \langle -14u^{14} - 57u^{13} + \dots + 4b - 4, 4u^{14}a - 24u^{14} + \dots + 5a - 25, \\
 &\quad u^{15} + 5u^{14} + 11u^{13} + 10u^{12} - 9u^{11} - 36u^{10} - 42u^9 - 10u^8 + 31u^7 + 50u^6 + 38u^5 + 7u^4 - 11u^3 - 6u^2 + u + 1 \rangle
 \end{aligned}$$

\* 9 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 126 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b - u, a - 1, u^9 - 5u^8 + \cdots + 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned}
a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_1 &= \begin{pmatrix} 1 \\ u \end{pmatrix} \\
a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\
a_2 &= \begin{pmatrix} u^2 - u + 1 \\ u^4 - u^3 + u \end{pmatrix} \\
a_8 &= \begin{pmatrix} -u \\ -u^2 + u \end{pmatrix} \\
a_6 &= \begin{pmatrix} u^3 - u^2 + 1 \\ u^4 - 2u^3 + u^2 \end{pmatrix} \\
a_3 &= \begin{pmatrix} -u^8 + 3u^7 - 4u^6 + u^5 + 2u^4 - 2u^3 + 1 \\ -u^8 + 5u^7 - 10u^6 + 11u^5 - 6u^4 + 2u^3 + 2u - 1 \end{pmatrix} \\
a_{12} &= \begin{pmatrix} -u + 1 \\ u \end{pmatrix} \\
a_{10} &= \begin{pmatrix} -u^3 + 2u^2 - u \\ u^3 - u^2 + u \end{pmatrix} \\
a_7 &= \begin{pmatrix} u^8 - 4u^7 + 7u^6 - 6u^5 + 2u^4 - u \\ -u^8 + 3u^7 - 5u^6 + 4u^5 - 2u^4 - u^2 + u \end{pmatrix} \\
a_{11} &= \begin{pmatrix} -u^7 + 3u^6 - 5u^5 + 4u^4 - 2u^3 - u + 1 \\ -2u^8 + 8u^7 - 15u^6 + 15u^5 - 8u^4 + 2u^3 - u^2 + 3u - 1 \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $3u^8 - 15u^7 + 36u^6 - 45u^5 + 33u^4 - 15u^3 + 9u^2 - 3u + 12$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_9$	$u^9 - 4u^8 + 10u^7 - 15u^6 + 16u^5 - 14u^4 + 12u^3 - 10u^2 + 6u - 1$
$c_2, c_6, c_{10}$	$u^9 - 7u^8 + 18u^7 - 19u^6 + 4u^5 + 5u^4 - 2u^3 - u^2 + 3u - 1$
$c_3, c_7, c_{11}$	$u^9 + 6u^8 + 15u^7 + 16u^6 + 2u^5 - 9u^4 - 2u^3 + 6u^2 + 3u - 1$
$c_4, c_8, c_{12}$	$u^9 - 5u^8 + 12u^7 - 16u^6 + 13u^5 - 6u^4 + 2u^3 - u^2 + 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_9$	$y^9 + 4y^8 + 12y^7 + 7y^6 + 8y^5 + 26y^3 + 16y^2 + 16y - 1$
$c_2, c_6, c_{10}$	$y^9 - 13y^8 + 66y^7 - 151y^6 + 126y^5 + 15y^4 - 3y^2 + 7y - 1$
$c_3, c_7, c_{11}$	$y^9 - 6y^8 + 37y^7 - 92y^6 + 166y^5 - 179y^4 + 156y^3 - 66y^2 + 21y - 1$
$c_4, c_8, c_{12}$	$y^9 - y^8 + 10y^7 + 19y^5 + 22y^4 + 12y^3 - 5y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.286198 + 0.902700I$		
$a = 1.00000$	$3.22071 - 2.28420I$	$3.39173 + 1.61517I$
$b = 0.286198 + 0.902700I$		
$u = 0.286198 - 0.902700I$		
$a = 1.00000$	$3.22071 + 2.28420I$	$3.39173 - 1.61517I$
$b = 0.286198 - 0.902700I$		
$u = -0.447949 + 0.409095I$		
$a = 1.00000$	$0.58147 + 2.13776I$	$3.86167 - 3.88522I$
$b = -0.447949 + 0.409095I$		
$u = -0.447949 - 0.409095I$		
$a = 1.00000$	$0.58147 - 2.13776I$	$3.86167 + 3.88522I$
$b = -0.447949 - 0.409095I$		
$u = 1.128820 + 0.825655I$		
$a = 1.00000$	$4.45533 + 4.10271I$	$9.59034 - 1.40424I$
$b = 1.128820 + 0.825655I$		
$u = 1.128820 - 0.825655I$		
$a = 1.00000$	$4.45533 - 4.10271I$	$9.59034 + 1.40424I$
$b = 1.128820 - 0.825655I$		
$u = 0.587597$		
$a = 1.00000$	0.838784	12.2450
$b = 0.587597$		
$u = 1.23914 + 1.04927I$		
$a = 1.00000$	$12.7072 + 17.7651I$	$10.03383 - 8.20740I$
$b = 1.23914 + 1.04927I$		
$u = 1.23914 - 1.04927I$		
$a = 1.00000$	$12.7072 - 17.7651I$	$10.03383 + 8.20740I$
$b = 1.23914 - 1.04927I$		

$$\text{II. } I_2^u = \langle b + u, a + 1, u^9 - 3u^8 + 4u^7 - 2u^6 + u^5 - 2u^4 + 2u^3 - u^2 - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1 \\ -u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^2 + u - 1 \\ -u^4 + u^3 - u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ -u^2 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^3 - u^2 + 1 \\ u^4 - 2u^3 + u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^8 + 3u^7 - 4u^6 + u^5 + 2u^4 - 2u^3 + 1 \\ u^8 - 3u^7 + 4u^6 - u^5 - 2u^4 + 2u^3 - 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u - 1 \\ -u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^3 + 2u^2 - u \\ u^3 - u^2 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^8 - 4u^7 + 7u^6 - 6u^5 + 2u^4 - u \\ -u^8 + 3u^7 - 5u^6 + 4u^5 - 2u^4 - u^2 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^7 - 3u^6 + 5u^5 - 4u^4 + 2u^3 + u - 1 \\ u^6 - 3u^5 + 4u^4 - 2u^3 + u^2 - u + 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-3u^8 + 15u^7 - 24u^6 + 15u^5 + 3u^4 + 3u^3 - 9u^2 + 3u + 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_9$	$u^9 - 2u^8 + 4u^7 - 5u^6 + 8u^5 - 10u^4 + 8u^3 - 6u^2 + 2u + 1$
$c_2, c_6, c_{10}$	$u^9 + 5u^8 + 8u^7 + 5u^6 + 4u^5 + 3u^4 + 3u^2 - u + 1$
$c_3, c_7, c_{11}$	$u^9 + 4u^8 + 5u^7 - 2u^5 + u^4 + 4u^2 + u + 5$
$c_4, c_8, c_{12}$	$u^9 - 3u^8 + 4u^7 - 2u^6 + u^5 - 2u^4 + 2u^3 - u^2 - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_9$	$y^9 + 4y^8 + 12y^7 + 15y^6 + 8y^5 - 12y^4 - 14y^3 + 16y^2 + 16y - 1$
$c_2, c_6, c_{10}$	$y^9 - 9y^8 + 22y^7 + 9y^6 - 46y^5 - 65y^4 - 36y^3 - 15y^2 - 5y - 1$
$c_3, c_7, c_{11}$	$y^9 - 6y^8 + 21y^7 - 28y^6 - 26y^5 - 31y^4 - 12y^3 - 26y^2 - 39y - 25$
$c_4, c_8, c_{12}$	$y^9 - y^8 + 6y^7 - 4y^6 + 3y^5 - 10y^4 - 4y^3 - 5y^2 - 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.640457 + 0.839014I$		
$a = -1.00000$	$-3.41503 + 2.80054I$	$-2.62634 - 4.93597I$
$b = -0.640457 - 0.839014I$		
$u = 0.640457 - 0.839014I$		
$a = -1.00000$	$-3.41503 - 2.80054I$	$-2.62634 + 4.93597I$
$b = -0.640457 + 0.839014I$		
$u = -0.611257 + 0.526811I$		
$a = -1.00000$	$10.77880 + 7.66911I$	$9.14267 - 3.23917I$
$b = 0.611257 - 0.526811I$		
$u = -0.611257 - 0.526811I$		
$a = -1.00000$	$10.77880 - 7.66911I$	$9.14267 + 3.23917I$
$b = 0.611257 + 0.526811I$		
$u = 1.20234$		
$a = -1.00000$	11.2685	14.6480
$b = -1.20234$		
$u = -0.274779 + 0.650965I$		
$a = -1.00000$	$1.42494 - 3.44509I$	$5.30781 + 7.71847I$
$b = 0.274779 - 0.650965I$		
$u = -0.274779 - 0.650965I$		
$a = -1.00000$	$1.42494 + 3.44509I$	$5.30781 - 7.71847I$
$b = 0.274779 + 0.650965I$		
$u = 1.14441 + 0.99327I$		
$a = -1.00000$	$2.02642 + 11.00000I$	$4.85190 - 8.60523I$
$b = -1.14441 - 0.99327I$		
$u = 1.14441 - 0.99327I$		
$a = -1.00000$	$2.02642 - 11.00000I$	$4.85190 + 8.60523I$
$b = -1.14441 + 0.99327I$		

$$\text{III. } I_3^u = \langle b - u, 4u^{17} + 8u^{16} + \cdots + 2a - 5, u^{18} + 5u^{17} + \cdots + 5u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -2u^{17} - 4u^{16} + \cdots + 8u + \frac{5}{2} \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -10u^{17} - 36u^{16} + \cdots - 21u - \frac{7}{2} \\ -\frac{13}{2}u^{17} - 28u^{16} + \cdots - 31u - 8 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -3u^{17} - 31u^{16} + \cdots - 98u - 36 \\ 8u^{17} + 32u^{16} + \cdots + 29u + 6 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{3}{2}u^{17} - \frac{21}{2}u^{16} + \cdots - \frac{75}{2}u - \frac{37}{2} \\ \frac{11}{2}u^{17} + 24u^{16} + \cdots + \frac{57}{2}u + \frac{13}{2} \end{pmatrix} \\ a_3 &= \begin{pmatrix} -10.5000u^{17} - 46.5000u^{16} + \cdots - 59.5000u - 21.5000 \\ 6u^{17} + 25u^{16} + \cdots + \frac{57}{2}u + \frac{15}{2} \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -2u^{17} - 4u^{16} + \cdots + 7u + \frac{5}{2} \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -19u^{17} - 95u^{16} + \cdots - 154u - 48 \\ 8u^{17} + 32u^{16} + \cdots + 29u + 6 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -\frac{77}{2}u^{17} - \frac{327}{2}u^{16} + \cdots - 181u - \frac{85}{2} \\ -\frac{27}{2}u^{17} - \frac{121}{2}u^{16} + \cdots - 78u - \frac{43}{2} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 48u^{17} + \frac{413}{2}u^{16} + \cdots + 234u + 60 \\ 7u^{17} + \frac{65}{2}u^{16} + \cdots + \frac{91}{2}u + 13 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = 37u^{17} + 174u^{16} + 393u^{15} + 512u^{14} + 582u^{13} + 849u^{12} + 1180u^{11} + 897u^{10} + 226u^9 - 106u^8 - 125u^7 - 507u^6 - 919u^5 - 725u^4 - 89u^3 + 317u^2 + 285u + 100$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{18} + 2u^{17} + \cdots + 11u + 7$
$c_2, c_{10}$	$u^{18} + 6u^{17} + \cdots + 2u + 1$
$c_3$	$u^{18} + 18u^{17} + \cdots + 5632u + 1024$
$c_4, c_{12}$	$u^{18} + 5u^{17} + \cdots + 5u + 1$
$c_6$	$u^{18} - 12u^{17} + \cdots - 1552u + 352$
$c_7, c_{11}$	$u^{18} - 7u^{17} + \cdots - 40u + 7$
$c_8$	$u^{18} - 17u^{17} + \cdots - 176u + 32$
$c_9$	$u^{18} - 16u^{17} + \cdots - 240u + 32$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{18} + 10y^{17} + \cdots + 313y + 49$
$c_2, c_{10}$	$y^{18} - 30y^{17} + \cdots - 8y + 1$
$c_3$	$y^{18} - 10y^{17} + \cdots + 1572864y + 1048576$
$c_4, c_{12}$	$y^{18} - y^{17} + \cdots - 5y + 1$
$c_6$	$y^{18} - 12y^{17} + \cdots + 401664y + 123904$
$c_7, c_{11}$	$y^{18} - 15y^{17} + \cdots - 634y + 49$
$c_8$	$y^{18} - 7y^{17} + \cdots - 1792y + 1024$
$c_9$	$y^{18} + 2y^{17} + \cdots + 15616y + 1024$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.768042 + 0.719269I$		
$a = -0.875237 + 0.270339I$	$-2.27200 - 2.57043I$	$6.54941 + 3.50069I$
$b = -0.768042 + 0.719269I$		
$u = -0.768042 - 0.719269I$		
$a = -0.875237 - 0.270339I$	$-2.27200 + 2.57043I$	$6.54941 - 3.50069I$
$b = -0.768042 - 0.719269I$		
$u = 0.535137 + 0.962955I$		
$a = 1.40580 - 0.92249I$	$7.73898 + 8.44090I$	$7.63933 - 9.24995I$
$b = 0.535137 + 0.962955I$		
$u = 0.535137 - 0.962955I$		
$a = 1.40580 + 0.92249I$	$7.73898 - 8.44090I$	$7.63933 + 9.24995I$
$b = 0.535137 - 0.962955I$		
$u = 0.782103 + 0.053724I$		
$a = 1.91617 + 1.26164I$	$3.58305 - 1.24938I$	$17.0632 + 1.0174I$
$b = 0.782103 + 0.053724I$		
$u = 0.782103 - 0.053724I$		
$a = 1.91617 - 1.26164I$	$3.58305 + 1.24938I$	$17.0632 - 1.0174I$
$b = 0.782103 - 0.053724I$		
$u = -0.262844 + 0.715699I$		
$a = 0.165375 + 0.643986I$	$0.72242 + 2.18469I$	$2.93233 - 4.07670I$
$b = -0.262844 + 0.715699I$		
$u = -0.262844 - 0.715699I$		
$a = 0.165375 - 0.643986I$	$0.72242 - 2.18469I$	$2.93233 + 4.07670I$
$b = -0.262844 - 0.715699I$		
$u = 0.777809 + 0.987076I$		
$a = 0.288479 + 0.024311I$	$5.99338 + 3.58170I$	$6.02957 - 2.59118I$
$b = 0.777809 + 0.987076I$		
$u = 0.777809 - 0.987076I$		
$a = 0.288479 - 0.024311I$	$5.99338 - 3.58170I$	$6.02957 + 2.59118I$
$b = 0.777809 - 0.987076I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.695734 + 0.191789I$		
$a = -1.21725 - 2.62700I$	$11.7749 - 8.5337I$	$15.3206 + 8.5140I$
$b = -0.695734 + 0.191789I$		
$u = -0.695734 - 0.191789I$		
$a = -1.21725 + 2.62700I$	$11.7749 + 8.5337I$	$15.3206 - 8.5140I$
$b = -0.695734 - 0.191789I$		
$u = -0.594298 + 0.360810I$		
$a = -2.76005 + 0.70415I$	$2.40603 - 4.20864I$	$12.3347 + 11.0008I$
$b = -0.594298 + 0.360810I$		
$u = -0.594298 - 0.360810I$		
$a = -2.76005 - 0.70415I$	$2.40603 + 4.20864I$	$12.3347 - 11.0008I$
$b = -0.594298 - 0.360810I$		
$u = -1.18514 + 0.90997I$		
$a = -1.051240 + 0.105286I$	$3.54942 - 10.06710I$	$10.59088 + 5.55087I$
$b = -1.18514 + 0.90997I$		
$u = -1.18514 - 0.90997I$		
$a = -1.051240 - 0.105286I$	$3.54942 + 10.06710I$	$10.59088 - 5.55087I$
$b = -1.18514 - 0.90997I$		
$u = -1.08899 + 1.07733I$		
$a = -0.872048 - 0.388084I$	$10.91700 - 4.65632I$	$14.5399 + 2.8811I$
$b = -1.08899 + 1.07733I$		
$u = -1.08899 - 1.07733I$		
$a = -0.872048 + 0.388084I$	$10.91700 + 4.65632I$	$14.5399 - 2.8811I$
$b = -1.08899 - 1.07733I$		

$$\text{IV. } I_4^u = \langle -12u^{17} - 44u^{16} + \dots + 2b - 4, a - 1, u^{18} + 5u^{17} + \dots + 5u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ 6u^{17} + 22u^{16} + \dots + \frac{25}{2}u + 2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -6u^{17} - 22u^{16} + \dots - \frac{25}{2}u - 1 \\ -2u^{17} - \frac{23}{2}u^{16} + \dots - \frac{43}{2}u - 6 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ 8u^{17} + 32u^{16} + \dots + 29u + 6 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 8u^{17} + \frac{67}{2}u^{16} + \dots + 34u + 9 \\ \frac{11}{2}u^{17} + 24u^{16} + \dots + \frac{57}{2}u + \frac{13}{2} \end{pmatrix} \\ a_3 &= \begin{pmatrix} -13u^{17} - 58u^{16} + \dots - 72u - \frac{39}{2} \\ -\frac{25}{2}u^{17} - 54u^{16} + \dots - 65u - 17 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -6u^{17} - 22u^{16} + \dots - \frac{25}{2}u - 1 \\ 6u^{17} + 22u^{16} + \dots + \frac{25}{2}u + 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{13}{2}u^{17} + 27u^{16} + \dots + 26u + 4 \\ -\frac{29}{2}u^{17} - 59u^{16} + \dots - 54u - 10 \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{15}{2}u^{17} + \frac{63}{2}u^{16} + \dots + 38u + 9 \\ -24u^{17} - 105u^{16} + \dots - \frac{255}{2}u - \frac{65}{2} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{43}{2}u^{17} + 94u^{16} + \dots + 112u + \frac{59}{2} \\ -\frac{11}{2}u^{17} - 24u^{16} + \dots - 28u - 7 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = 37u^{17} + 174u^{16} + 393u^{15} + 512u^{14} + 582u^{13} + 849u^{12} + 1180u^{11} + 897u^{10} + 226u^9 - 106u^8 - 125u^7 - 507u^6 - 919u^5 - 725u^4 - 89u^3 + 317u^2 + 285u + 100$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{18} - 16u^{17} + \cdots - 240u + 32$
$c_2, c_6$	$u^{18} + 6u^{17} + \cdots + 2u + 1$
$c_3, c_{11}$	$u^{18} - 7u^{17} + \cdots - 40u + 7$
$c_4, c_8$	$u^{18} + 5u^{17} + \cdots + 5u + 1$
$c_5, c_9$	$u^{18} + 2u^{17} + \cdots + 11u + 7$
$c_7$	$u^{18} + 18u^{17} + \cdots + 5632u + 1024$
$c_{10}$	$u^{18} - 12u^{17} + \cdots - 1552u + 352$
$c_{12}$	$u^{18} - 17u^{17} + \cdots - 176u + 32$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{18} + 2y^{17} + \cdots + 15616y + 1024$
$c_2, c_6$	$y^{18} - 30y^{17} + \cdots - 8y + 1$
$c_3, c_{11}$	$y^{18} - 15y^{17} + \cdots - 634y + 49$
$c_4, c_8$	$y^{18} - y^{17} + \cdots - 5y + 1$
$c_5, c_9$	$y^{18} + 10y^{17} + \cdots + 313y + 49$
$c_7$	$y^{18} - 10y^{17} + \cdots + 1572864y + 1048576$
$c_{10}$	$y^{18} - 12y^{17} + \cdots + 401664y + 123904$
$c_{12}$	$y^{18} - 7y^{17} + \cdots - 1792y + 1024$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.768042 + 0.719269I$		
$a = 1.00000$	$-2.27200 - 2.57043I$	$6.54941 + 3.50069I$
$b = 0.477772 - 0.837163I$		
$u = -0.768042 - 0.719269I$		
$a = 1.00000$	$-2.27200 + 2.57043I$	$6.54941 - 3.50069I$
$b = 0.477772 + 0.837163I$		
$u = 0.535137 + 0.962955I$		
$a = 1.00000$	$7.73898 + 8.44090I$	$7.63933 - 9.24995I$
$b = 1.64061 + 0.86007I$		
$u = 0.535137 - 0.962955I$		
$a = 1.00000$	$7.73898 - 8.44090I$	$7.63933 + 9.24995I$
$b = 1.64061 - 0.86007I$		
$u = 0.782103 + 0.053724I$		
$a = 1.00000$	$3.58305 - 1.24938I$	$17.0632 + 1.0174I$
$b = 1.43086 + 1.08968I$		
$u = 0.782103 - 0.053724I$		
$a = 1.00000$	$3.58305 + 1.24938I$	$17.0632 - 1.0174I$
$b = 1.43086 - 1.08968I$		
$u = -0.262844 + 0.715699I$		
$a = 1.00000$	$0.72242 + 2.18469I$	$2.93233 - 4.07670I$
$b = -0.504368 - 0.050909I$		
$u = -0.262844 - 0.715699I$		
$a = 1.00000$	$0.72242 - 2.18469I$	$2.93233 + 4.07670I$
$b = -0.504368 + 0.050909I$		
$u = 0.777809 + 0.987076I$		
$a = 1.00000$	$5.99338 + 3.58170I$	$6.02957 - 2.59118I$
$b = 0.200384 + 0.303660I$		
$u = 0.777809 - 0.987076I$		
$a = 1.00000$	$5.99338 - 3.58170I$	$6.02957 + 2.59118I$
$b = 0.200384 - 0.303660I$		

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.695734 + 0.191789I$		
$a = 1.00000$	$11.7749 - 8.5337I$	$15.3206 + 8.5140I$
$b = 1.35071 + 1.59423I$		
$u = -0.695734 - 0.191789I$		
$a = 1.00000$	$11.7749 + 8.5337I$	$15.3206 - 8.5140I$
$b = 1.35071 - 1.59423I$		
$u = -0.594298 + 0.360810I$		
$a = 1.00000$	$2.40603 - 4.20864I$	$12.3347 + 11.0008I$
$b = 1.38623 - 1.41433I$		
$u = -0.594298 - 0.360810I$		
$a = 1.00000$	$2.40603 + 4.20864I$	$12.3347 - 11.0008I$
$b = 1.38623 + 1.41433I$		
$u = -1.18514 + 0.90997I$		
$a = 1.00000$	$3.54942 - 10.06710I$	$10.59088 + 5.55087I$
$b = 1.15005 - 1.08137I$		
$u = -1.18514 - 0.90997I$		
$a = 1.00000$	$3.54942 + 10.06710I$	$10.59088 - 5.55087I$
$b = 1.15005 + 1.08137I$		
$u = -1.08899 + 1.07733I$		
$a = 1.00000$	$10.91700 - 4.65632I$	$14.5399 + 2.8811I$
$b = 1.36775 - 0.51686I$		
$u = -1.08899 - 1.07733I$		
$a = 1.00000$	$10.91700 + 4.65632I$	$14.5399 - 2.8811I$
$b = 1.36775 + 0.51686I$		

$$\text{V. } I_5^u = \langle -582u^{17} + 8001u^{16} + \cdots + 6236b + 10944, -342u^{17} + 5232u^{16} + \cdots + 6236a - 30, u^{18} - 17u^{17} + \cdots - 176u + 32 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.0548428u^{17} - 0.838999u^{16} + \cdots + 14.0253u + 0.00481078 \\ 0.0933291u^{17} - 1.28303u^{16} + \cdots + 9.65715u - 1.75497 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.265074u^{17} - 4.05516u^{16} + \cdots + 19.0391u - 1.22675 \\ 0.381976u^{17} - 6.48829u^{16} + \cdots + 65.8958u - 13.2033 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.0831462u^{17} + 1.44524u^{16} + \cdots - 38.8754u + 6.77999 \\ 0.0317511u^{17} - 0.472579u^{16} + \cdots - 6.85375u + 2.66068 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.0383659u^{17} - 0.560616u^{16} + \cdots + 2.67672u - 5.61835 \\ 0.158796u^{17} - 2.55320u^{16} + \cdots + 8.38294u - 2.24375 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.377205u^{17} - 6.21685u^{16} + \cdots + 81.8435u - 10.5930 \\ 0.0953335u^{17} - 1.67335u^{16} + \cdots + 37.2421u - 9.11225 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.0384862u^{17} + 0.444035u^{16} + \cdots + 4.36818u + 1.75978 \\ 0.0933291u^{17} - 1.28303u^{16} + \cdots + 9.65715u - 1.75497 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.0794580u^{17} + 1.18706u^{16} + \cdots - 14.9190u + 0.442591 \\ -0.0354394u^{17} + 0.730757u^{16} + \cdots - 15.1026u + 3.67672 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.121572u^{17} - 2.10381u^{16} + \cdots + 19.2797u - 3.21905 \\ -0.435014u^{17} + 6.63851u^{16} + \cdots - 28.5946u + 5.07697 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.690186u^{17} - 10.8130u^{16} + \cdots + 61.6639u - 7.15876 \\ 0.967768u^{17} - 15.7437u^{16} + \cdots + 140.533u - 28.0949 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-\frac{741}{3118}u^{17} + \frac{7227}{1559}u^{16} + \cdots - \frac{161008}{1559}u + \frac{45958}{1559}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u^{18} + 2u^{17} + \cdots + 11u + 7$
$c_2$	$u^{18} - 12u^{17} + \cdots - 1552u + 352$
$c_3, c_7$	$u^{18} - 7u^{17} + \cdots - 40u + 7$
$c_4$	$u^{18} - 17u^{17} + \cdots - 176u + 32$
$c_5$	$u^{18} - 16u^{17} + \cdots - 240u + 32$
$c_6, c_{10}$	$u^{18} + 6u^{17} + \cdots + 2u + 1$
$c_8, c_{12}$	$u^{18} + 5u^{17} + \cdots + 5u + 1$
$c_{11}$	$u^{18} + 18u^{17} + \cdots + 5632u + 1024$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_9$	$y^{18} + 10y^{17} + \cdots + 313y + 49$
$c_2$	$y^{18} - 12y^{17} + \cdots + 401664y + 123904$
$c_3, c_7$	$y^{18} - 15y^{17} + \cdots - 634y + 49$
$c_4$	$y^{18} - 7y^{17} + \cdots - 1792y + 1024$
$c_5$	$y^{18} + 2y^{17} + \cdots + 15616y + 1024$
$c_6, c_{10}$	$y^{18} - 30y^{17} + \cdots - 8y + 1$
$c_8, c_{12}$	$y^{18} - y^{17} + \cdots - 5y + 1$
$c_{11}$	$y^{18} - 10y^{17} + \cdots + 1572864y + 1048576$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.477772 + 0.837163I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.043040 + 0.322168I$	$-2.27200 + 2.57043I$	$6.54941 - 3.50069I$
$b = -0.768042 - 0.719269I$		
$u = 0.477772 - 0.837163I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.043040 - 0.322168I$	$-2.27200 - 2.57043I$	$6.54941 + 3.50069I$
$b = -0.768042 + 0.719269I$		
$u = 1.36775 + 0.51686I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.957162 - 0.425962I$	$10.91700 + 4.65632I$	$14.5399 - 2.8811I$
$b = -1.08899 - 1.07733I$		
$u = 1.36775 - 0.51686I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.957162 + 0.425962I$	$10.91700 - 4.65632I$	$14.5399 + 2.8811I$
$b = -1.08899 + 1.07733I$		
$u = -0.504368 + 0.050909I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.37410 + 1.45676I$	$0.72242 - 2.18469I$	$2.93233 + 4.07670I$
$b = -0.262844 - 0.715699I$		
$u = -0.504368 - 0.050909I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.37410 - 1.45676I$	$0.72242 + 2.18469I$	$2.93233 - 4.07670I$
$b = -0.262844 + 0.715699I$		
$u = 1.15005 + 1.08137I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.941815 + 0.094327I$	$3.54942 + 10.06710I$	$10.59088 - 5.55087I$
$b = -1.18514 - 0.90997I$		
$u = 1.15005 - 1.08137I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.941815 - 0.094327I$	$3.54942 - 10.06710I$	$10.59088 + 5.55087I$
$b = -1.18514 + 0.90997I$		
$u = 0.200384 + 0.303660I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 3.44201 - 0.29007I$	$5.99338 + 3.58170I$	$6.02957 - 2.59118I$
$b = 0.777809 + 0.987076I$		
$u = 0.200384 - 0.303660I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 3.44201 + 0.29007I$	$5.99338 - 3.58170I$	$6.02957 + 2.59118I$
$b = 0.777809 - 0.987076I$		

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.43086 + 1.08968I$		
$a = 0.364052 - 0.239699I$	$3.58305 - 1.24938I$	$17.0632 + 1.0174I$
$b = 0.782103 + 0.053724I$		
$u = 1.43086 - 1.08968I$		
$a = 0.364052 + 0.239699I$	$3.58305 + 1.24938I$	$17.0632 - 1.0174I$
$b = 0.782103 - 0.053724I$		
$u = 1.64061 + 0.86007I$		
$a = 0.497231 + 0.326283I$	$7.73898 + 8.44090I$	$7.63933 - 9.24995I$
$b = 0.535137 + 0.962955I$		
$u = 1.64061 - 0.86007I$		
$a = 0.497231 - 0.326283I$	$7.73898 - 8.44090I$	$7.63933 + 9.24995I$
$b = 0.535137 - 0.962955I$		
$u = 1.38623 + 1.41433I$		
$a = -0.340171 + 0.086786I$	$2.40603 + 4.20864I$	$12.3347 - 11.0008I$
$b = -0.594298 - 0.360810I$		
$u = 1.38623 - 1.41433I$		
$a = -0.340171 - 0.086786I$	$2.40603 - 4.20864I$	$12.3347 + 11.0008I$
$b = -0.594298 + 0.360810I$		
$u = 1.35071 + 1.59423I$		
$a = -0.145208 + 0.313379I$	$11.7749 - 8.5337I$	$15.3206 + 8.5140I$
$b = -0.695734 + 0.191789I$		
$u = 1.35071 - 1.59423I$		
$a = -0.145208 - 0.313379I$	$11.7749 + 8.5337I$	$15.3206 - 8.5140I$
$b = -0.695734 - 0.191789I$		

$$\text{VI. } I_6^u = \langle b + u, -2u^7 - 5u^6 + \dots + a - 3, u^8 + 3u^7 + \dots + 3u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 2u^7 + 5u^6 + 8u^5 + 9u^4 + 10u^3 + 7u^2 + 7u + 3 \\ -u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 3u^7 + 7u^6 + 10u^5 + 11u^4 + 13u^3 + 9u^2 + 9u + 4 \\ u^6 + 2u^5 + 3u^4 + 3u^3 + 3u^2 + u + 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^7 + 2u^6 + 4u^5 + 5u^4 + 5u^3 + 3u^2 + 5u + 1 \\ u^7 + 2u^6 + 2u^5 + 2u^4 + 3u^3 + 2u^2 + 2u + 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -2u^7 - 6u^6 - 9u^5 - 9u^4 - 10u^3 - 9u^2 - 6u - 2 \\ u^3 + u^2 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -4u^7 - 12u^6 - 16u^5 - 13u^4 - 15u^3 - 14u^2 - 7u \\ u^7 + 3u^6 + 4u^5 + 4u^4 + 4u^3 + 4u^2 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 2u^7 + 5u^6 + 8u^5 + 9u^4 + 10u^3 + 7u^2 + 8u + 3 \\ -u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^7 - 2u^6 + u^4 - 2u^3 - u^2 + 3u - 1 \\ u^7 + 2u^6 + 2u^5 + 2u^4 + 4u^3 + 2u^2 + 2u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -3u^7 - 8u^6 - 11u^5 - 10u^4 - 12u^3 - 9u^2 - 7u - 2 \\ -u^5 - 2u^4 - 2u^3 - 2u^2 - u - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^6 - u^5 - u^4 - 2u^3 - 3u^2 - 2 \\ u^7 + 2u^6 + 2u^5 + 2u^4 + 3u^3 + 2u^2 + 2u + 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $15u^7 + 35u^6 + 47u^5 + 47u^4 + 60u^3 + 37u^2 + 32u + 19$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^8 + 2u^6 + u^5 + 4u^4 - u^3 + 4u^2 - u + 1$
$c_2, c_{10}$	$u^8 - 4u^7 + 8u^6 - 14u^5 + 19u^4 - 17u^3 + 11u^2 - 4u + 1$
$c_3$	$u^8 - 3u^7 - 2u^6 + 3u^5 + 22u^4 + 24u^3 + 18u^2 + 3u + 1$
$c_4, c_{12}$	$u^8 + 3u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 5u^2 + 3u + 1$
$c_6$	$u^8 + 3u^7 + u^6 + 8u^4 + 6u^3 - 2u^2 - u + 1$
$c_7, c_{11}$	$u^8 + u^7 - 2u^6 - 5u^5 - u^4 + 6u^3 + 8u^2 + 4u + 1$
$c_8$	$(u^4 - 3u^3 + 3u^2 - u - 1)^2$
$c_9$	$u^8 - 7u^7 + 20u^6 - 37u^5 + 52u^4 - 48u^3 + 44u^2 - 19u + 11$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^8 + 4y^7 + 12y^6 + 23y^5 + 36y^4 + 37y^3 + 22y^2 + 7y + 1$
$c_2, c_{10}$	$y^8 - 10y^6 - 6y^5 + 31y^4 + 33y^3 + 23y^2 + 6y + 1$
$c_3$	$y^8 - 13y^7 + 66y^6 + 83y^5 + 288y^4 + 194y^3 + 224y^2 + 27y + 1$
$c_4, c_{12}$	$y^8 + y^7 + 3y^6 + 8y^5 + 11y^4 + 8y^3 + 3y^2 + y + 1$
$c_6$	$y^8 - 7y^7 + 17y^6 - 24y^5 + 68y^4 - 66y^3 + 32y^2 - 5y + 1$
$c_7, c_{11}$	$y^8 - 5y^7 + 12y^6 - 17y^5 + 23y^4 - 16y^3 + 14y^2 + 1$
$c_8$	$(y^4 - 3y^3 + y^2 - 7y + 1)^2$
$c_9$	$y^8 - 9y^7 - 14y^6 + 127y^5 + 668y^4 + 1306y^3 + 1256y^2 + 607y + 121$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.164478 + 0.986381I$		
$a = 0.29921 + 1.79440I$	$-0.891430 + 0.808282I$	$4.38747 - 7.84089I$
$b = 0.164478 - 0.986381I$		
$u = -0.164478 - 0.986381I$		
$a = 0.29921 - 1.79440I$	$-0.891430 - 0.808282I$	$4.38747 + 7.84089I$
$b = 0.164478 + 0.986381I$		
$u = 0.452583 + 0.891722I$		
$a = 0.172107 - 0.339102I$	$1.13995 - 1.35977I$	$7.04382 - 3.05706I$
$b = -0.452583 - 0.891722I$		
$u = 0.452583 - 0.891722I$		
$a = 0.172107 + 0.339102I$	$1.13995 + 1.35977I$	$7.04382 + 3.05706I$
$b = -0.452583 + 0.891722I$		
$u = -0.584796 + 0.379478I$		
$a = 0.22519 + 1.70988I$	$1.15941 - 3.26530I$	$7.76010 + 9.86097I$
$b = 0.584796 - 0.379478I$		
$u = -0.584796 - 0.379478I$		
$a = 0.22519 - 1.70988I$	$1.15941 + 3.26530I$	$7.76010 - 9.86097I$
$b = 0.584796 + 0.379478I$		
$u = -1.20331 + 0.78084I$		
$a = 0.803486 - 0.238578I$	$8.46167 - 5.22804I$	$9.80861 + 4.92233I$
$b = 1.20331 - 0.78084I$		
$u = -1.20331 - 0.78084I$		
$a = 0.803486 + 0.238578I$	$8.46167 + 5.22804I$	$9.80861 - 4.92233I$
$b = 1.20331 + 0.78084I$		

VII.

$$I_7^u = \langle u^7 + 2u^6 + 3u^5 + 4u^4 + 5u^3 + 3u^2 + b + 3u + 2, a + 1, u^8 + 3u^7 + \dots + 3u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1 \\ -u^7 - 2u^6 - 3u^5 - 4u^4 - 5u^3 - 3u^2 - 3u - 2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^7 + 2u^6 + 3u^5 + 4u^4 + 5u^3 + 2u^2 + 3u + 1 \\ u^6 + u^5 - u^4 - u^3 + u^2 - u - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ u^7 + 2u^6 + 2u^5 + 2u^4 + 3u^3 + 2u^2 + 2u + 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^7 + 3u^6 + 4u^5 + 4u^4 + 4u^3 + 3u^2 + 2u + 2 \\ u^3 + u^2 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^7 + 2u^6 + 3u^5 + 4u^4 + 5u^3 + 3u^2 + 3u + 1 \\ -u^7 - 2u^6 - 3u^5 - 4u^4 - 5u^3 - 3u^2 - 3u - 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^7 + 2u^6 + 3u^5 + 4u^4 + 5u^3 + 3u^2 + 3u + 1 \\ -u^7 - 2u^6 - 3u^5 - 4u^4 - 5u^3 - 3u^2 - 3u - 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^2 - u - 1 \\ -u^7 - 2u^6 - 2u^5 - 2u^4 - 3u^3 - u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^6 - 3u^5 - 4u^4 - 4u^3 - 4u^2 - 4u - 1 \\ u^7 + 5u^6 + 10u^5 + 12u^4 + 11u^3 + 12u^2 + 10u + 4 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^7 - 3u^6 - 5u^5 - 5u^4 - 5u^3 - 4u^2 - 3u - 2 \\ -u^7 - u^6 - u^3 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $15u^7 + 35u^6 + 47u^5 + 47u^4 + 60u^3 + 37u^2 + 32u + 19$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^8 - 7u^7 + 20u^6 - 37u^5 + 52u^4 - 48u^3 + 44u^2 - 19u + 11$
$c_2, c_6$	$u^8 - 4u^7 + 8u^6 - 14u^5 + 19u^4 - 17u^3 + 11u^2 - 4u + 1$
$c_3, c_{11}$	$u^8 + u^7 - 2u^6 - 5u^5 - u^4 + 6u^3 + 8u^2 + 4u + 1$
$c_4, c_8$	$u^8 + 3u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 5u^2 + 3u + 1$
$c_5, c_9$	$u^8 + 2u^6 + u^5 + 4u^4 - u^3 + 4u^2 - u + 1$
$c_7$	$u^8 - 3u^7 - 2u^6 + 3u^5 + 22u^4 + 24u^3 + 18u^2 + 3u + 1$
$c_{10}$	$u^8 + 3u^7 + u^6 + 8u^4 + 6u^3 - 2u^2 - u + 1$
$c_{12}$	$(u^4 - 3u^3 + 3u^2 - u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^8 - 9y^7 - 14y^6 + 127y^5 + 668y^4 + 1306y^3 + 1256y^2 + 607y + 121$
$c_2, c_6$	$y^8 - 10y^6 - 6y^5 + 31y^4 + 33y^3 + 23y^2 + 6y + 1$
$c_3, c_{11}$	$y^8 - 5y^7 + 12y^6 - 17y^5 + 23y^4 - 16y^3 + 14y^2 + 1$
$c_4, c_8$	$y^8 + y^7 + 3y^6 + 8y^5 + 11y^4 + 8y^3 + 3y^2 + y + 1$
$c_5, c_9$	$y^8 + 4y^7 + 12y^6 + 23y^5 + 36y^4 + 37y^3 + 22y^2 + 7y + 1$
$c_7$	$y^8 - 13y^7 + 66y^6 + 83y^5 + 288y^4 + 194y^3 + 224y^2 + 27y + 1$
$c_{10}$	$y^8 - 7y^7 + 17y^6 - 24y^5 + 68y^4 - 66y^3 + 32y^2 - 5y + 1$
$c_{12}$	$(y^4 - 3y^3 + y^2 - 7y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_7^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.164478 + 0.986381I$		
$a = -1.00000$	$-0.891430 + 0.808282I$	$4.38747 - 7.84089I$
$b = -1.81917$		
$u = -0.164478 - 0.986381I$		
$a = -1.00000$	$-0.891430 - 0.808282I$	$4.38747 + 7.84089I$
$b = -1.81917$		
$u = 0.452583 + 0.891722I$		
$a = -1.00000$	$1.13995 - 1.35977I$	$7.04382 - 3.05706I$
$b = 0.380278$		
$u = 0.452583 - 0.891722I$		
$a = -1.00000$	$1.13995 + 1.35977I$	$7.04382 + 3.05706I$
$b = 0.380278$		
$u = -0.584796 + 0.379478I$		
$a = -1.00000$	$1.15941 - 3.26530I$	$7.76010 + 9.86097I$
$b = -0.780553 - 0.914474I$		
$u = -0.584796 - 0.379478I$		
$a = -1.00000$	$1.15941 + 3.26530I$	$7.76010 - 9.86097I$
$b = -0.780553 + 0.914474I$		
$u = -1.20331 + 0.78084I$		
$a = -1.00000$	$8.46167 - 5.22804I$	$9.80861 + 4.92233I$
$b = -0.780553 + 0.914474I$		
$u = -1.20331 - 0.78084I$		
$a = -1.00000$	$8.46167 + 5.22804I$	$9.80861 - 4.92233I$
$b = -0.780553 - 0.914474I$		

### VIII.

$$I_8^u = \langle -au + b, -u^3 + a^2 + au + 4u^2 - 2a - 6u + 4, u^4 - 3u^3 + 3u^2 - u - 1 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ au \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2a - au + a \\ 2u^3a - 3u^2a + 2au + a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2a + u^3 - 2au - 3u^2 + 3u - 1 \\ u^3a - 2u^2a + u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3a + 2u^2a - au + u^2 - u + 1 \\ -u^2a + u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2a - u^3 + 3au + 3u^2 - 2u \\ 2u^2a + u^3 - u^2 - u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -au + a \\ au \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3a + 2u^2a + u^3 - au - 3u^2 + a + 4u - 3 \\ u^2a - au - a + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 + 3u^2 - 3u + 2 \\ u^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2u^3a - 3u^2a + u^3 + au - 3u^2 + 2a + 4u - 2 \\ 4u^3a - 4u^2a + u^3 + 4au - u^2 + 2a + 1 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $11u^3a - 21u^2a - 7u^3 + 7au + 11u^2 + 5a + u + 7$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u^8 + 2u^6 + u^5 + 4u^4 - u^3 + 4u^2 - u + 1$
$c_2$	$u^8 + 3u^7 + u^6 + 8u^4 + 6u^3 - 2u^2 - u + 1$
$c_3, c_7$	$u^8 + u^7 - 2u^6 - 5u^5 - u^4 + 6u^3 + 8u^2 + 4u + 1$
$c_4$	$(u^4 - 3u^3 + 3u^2 - u - 1)^2$
$c_5$	$u^8 - 7u^7 + 20u^6 - 37u^5 + 52u^4 - 48u^3 + 44u^2 - 19u + 11$
$c_6, c_{10}$	$u^8 - 4u^7 + 8u^6 - 14u^5 + 19u^4 - 17u^3 + 11u^2 - 4u + 1$
$c_8, c_{12}$	$u^8 + 3u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 5u^2 + 3u + 1$
$c_{11}$	$u^8 - 3u^7 - 2u^6 + 3u^5 + 22u^4 + 24u^3 + 18u^2 + 3u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_9$	$y^8 + 4y^7 + 12y^6 + 23y^5 + 36y^4 + 37y^3 + 22y^2 + 7y + 1$
$c_2$	$y^8 - 7y^7 + 17y^6 - 24y^5 + 68y^4 - 66y^3 + 32y^2 - 5y + 1$
$c_3, c_7$	$y^8 - 5y^7 + 12y^6 - 17y^5 + 23y^4 - 16y^3 + 14y^2 + 1$
$c_4$	$(y^4 - 3y^3 + y^2 - 7y + 1)^2$
$c_5$	$y^8 - 9y^7 - 14y^6 + 127y^5 + 668y^4 + 1306y^3 + 1256y^2 + 607y + 121$
$c_6, c_{10}$	$y^8 - 10y^6 - 6y^5 + 31y^4 + 33y^3 + 23y^2 + 6y + 1$
$c_8, c_{12}$	$y^8 + y^7 + 3y^6 + 8y^5 + 11y^4 + 8y^3 + 3y^2 + y + 1$
$c_{11}$	$y^8 - 13y^7 + 66y^6 + 83y^5 + 288y^4 + 194y^3 + 224y^2 + 27y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_8^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.780553 + 0.914474I$		
$a = 1.143740 - 0.339608I$	$8.46167 + 5.22804I$	$9.80861 - 4.92233I$
$b = 1.20331 + 0.78084I$		
$u = 0.780553 + 0.914474I$		
$a = 0.075710 - 0.574866I$	$1.15941 - 3.26530I$	$7.76010 + 9.86097I$
$b = 0.584796 - 0.379478I$		
$u = 0.780553 - 0.914474I$		
$a = 1.143740 + 0.339608I$	$8.46167 - 5.22804I$	$9.80861 + 4.92233I$
$b = 1.20331 - 0.78084I$		
$u = 0.780553 - 0.914474I$		
$a = 0.075710 + 0.574866I$	$1.15941 + 3.26530I$	$7.76010 - 9.86097I$
$b = 0.584796 + 0.379478I$		
$u = -0.380278$		
$a = 1.19014 + 2.34492I$	$1.13995 - 1.35977I$	$7.04382 - 3.05706I$
$b = -0.452583 - 0.891722I$		
$u = -0.380278$		
$a = 1.19014 - 2.34492I$	$1.13995 + 1.35977I$	$7.04382 + 3.05706I$
$b = -0.452583 + 0.891722I$		
$u = 1.81917$		
$a = 0.090414 + 0.542214I$	$-0.891430 - 0.808282I$	$4.38747 + 7.84089I$
$b = 0.164478 + 0.986381I$		
$u = 1.81917$		
$a = 0.090414 - 0.542214I$	$-0.891430 + 0.808282I$	$4.38747 - 7.84089I$
$b = 0.164478 - 0.986381I$		

$$\text{IX. } I_9^u = \langle -14u^{14} - 57u^{13} + \cdots + 4b - 4, 4u^{14}a - 24u^{14} + \cdots + 5a - 25, u^{15} + 5u^{14} + \cdots + u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} a \\ \frac{7}{2}u^{14} + \frac{57}{4}u^{13} + \cdots - \frac{1}{4}u + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{7}{2}u^{14} - \frac{57}{4}u^{13} + \cdots + a - 1 \\ \frac{1}{2}u^{14} + \frac{3}{2}u^{13} + \cdots - au - \frac{9}{4} \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{7}{2}u^{14}a + u^{14} + \cdots - a + 6 \\ \frac{5}{4}u^{13} + \frac{19}{4}u^{12} + \cdots - 4u + 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^{14}a - \frac{3}{2}u^{14} + \cdots - \frac{5}{2}a - \frac{7}{2}u \\ -\frac{7}{4}u^{14} - \frac{29}{4}u^{13} + \cdots + \frac{1}{2}u - \frac{3}{2} \end{pmatrix} \\ a_3 &= \begin{pmatrix} \frac{3}{4}u^{14}a - \frac{13}{4}u^{14} + \cdots + \frac{5}{4}a - \frac{19}{4} \\ -\frac{3}{2}u^{14}a + \frac{7}{4}u^{14} + \cdots - a + \frac{7}{4} \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -\frac{7}{2}u^{14} - \frac{57}{4}u^{13} + \cdots + a - 1 \\ \frac{7}{2}u^{14} + \frac{57}{4}u^{13} + \cdots - \frac{1}{4}u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -\frac{1}{2}u^{14}a + \frac{3}{4}u^{14} + \cdots + \frac{9}{4}a + \frac{19}{4} \\ -3u^{14}a + \frac{1}{4}u^{14} + \cdots - \frac{13}{4}a + \frac{1}{4} \end{pmatrix} \\ a_7 &= \begin{pmatrix} -\frac{7}{4}u^{14}a + \frac{13}{2}u^{14} + \cdots - \frac{3}{2}a + \frac{19}{2} \\ \frac{1}{4}u^{14}a + 2u^{14} + \cdots + \frac{1}{2}a + \frac{13}{4} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^{14}a + 7u^{14} + \cdots + a + \frac{41}{4} \\ u^{14}a - \frac{9}{4}u^{14} + \cdots + a - 3 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = 4u^{14} + 18u^{13} + 34u^{12} + 18u^{11} - 56u^{10} - 126u^9 - 96u^8 + 44u^7 + 144u^6 + 138u^5 + 52u^4 - 46u^3 - 56u^2 - 2u + 24$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_9$	$(u^{15} + 3u^{14} + \cdots + 13u + 11)^2$
$c_2, c_6, c_{10}$	$(u^{15} + 3u^{14} + \cdots + 23u + 1)^2$
$c_3, c_7, c_{11}$	$(u^{15} - 5u^{14} + \cdots - 205u + 61)^2$
$c_4, c_8, c_{12}$	$(u^{15} + 5u^{14} + \cdots + u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_9$	$(y^{15} + 5y^{14} + \dots - 1107y - 121)^2$
$c_2, c_6, c_{10}$	$(y^{15} - 15y^{14} + \dots + 201y - 1)^2$
$c_3, c_7, c_{11}$	$(y^{15} - 19y^{14} + \dots + 9085y - 3721)^2$
$c_4, c_8, c_{12}$	$(y^{15} - 3y^{14} + \dots + 13y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_g^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.046733 + 1.000910I$		
$a = -0.995650 + 0.093177I$	-0.882183	$4.39116 + 0.I$
$b = -1.81124$		
$u = -0.046733 + 1.000910I$		
$a = 0.08431 + 1.80566I$	-0.882183	$4.39116 + 0.I$
$b = -0.046733 - 1.000910I$		
$u = -0.046733 - 1.000910I$		
$a = -0.995650 - 0.093177I$	-0.882183	$4.39116 + 0.I$
$b = -1.81124$		
$u = -0.046733 - 1.000910I$		
$a = 0.08431 - 1.80566I$	-0.882183	$4.39116 + 0.I$
$b = -0.046733 + 1.000910I$		
$u = 1.217660 + 0.183120I$		
$a = -0.751696 + 0.987223I$	10.95830 - 3.33174I	$13.91874 + 2.36228I$
$b = -0.738859 + 0.190472I$		
$u = 1.217660 + 0.183120I$		
$a = -0.570362 + 0.242199I$	10.95830 - 3.33174I	$13.91874 + 2.36228I$
$b = -1.09609 + 1.06445I$		
$u = 1.217660 - 0.183120I$		
$a = -0.751696 - 0.987223I$	10.95830 + 3.33174I	$13.91874 - 2.36228I$
$b = -0.738859 - 0.190472I$		
$u = 1.217660 - 0.183120I$		
$a = -0.570362 - 0.242199I$	10.95830 + 3.33174I	$13.91874 - 2.36228I$
$b = -1.09609 - 1.06445I$		
$u = -0.738859 + 0.190472I$		
$a = -1.48542 - 0.63077I$	10.95830 - 3.33174I	$13.91874 + 2.36228I$
$b = -1.09609 + 1.06445I$		
$u = -0.738859 + 0.190472I$		
$a = 1.73930 - 0.99229I$	10.95830 - 3.33174I	$13.91874 + 2.36228I$
$b = 1.217660 + 0.183120I$		

Solutions to $I_9^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.738859 - 0.190472I$		
$a = -1.48542 + 0.63077I$	$10.95830 + 3.33174I$	$13.91874 - 2.36228I$
$b = -1.09609 - 1.06445I$		
$u = -0.738859 - 0.190472I$		
$a = 1.73930 + 0.99229I$	$10.95830 + 3.33174I$	$13.91874 - 2.36228I$
$b = 1.217660 - 0.183120I$		
$u = -0.652116 + 0.353801I$		
$a = -0.571565 - 0.118668I$	$1.81981 - 2.21397I$	$12.88568 + 4.22289I$
$b = -0.69295 - 1.45068I$		
$u = -0.652116 + 0.353801I$		
$a = -0.11149 + 2.16409I$	$1.81981 - 2.21397I$	$12.88568 + 4.22289I$
$b = 0.414711 - 0.124835I$		
$u = -0.652116 - 0.353801I$		
$a = -0.571565 + 0.118668I$	$1.81981 + 2.21397I$	$12.88568 - 4.22289I$
$b = -0.69295 + 1.45068I$		
$u = -0.652116 - 0.353801I$		
$a = -0.11149 - 2.16409I$	$1.81981 + 2.21397I$	$12.88568 - 4.22289I$
$b = 0.414711 + 0.124835I$		
$u = -1.09609 + 1.06445I$		
$a = -0.488224 - 0.641197I$	$10.95830 - 3.33174I$	$13.91874 + 2.36228I$
$b = -0.738859 + 0.190472I$		
$u = -1.09609 + 1.06445I$		
$a = 0.433762 + 0.247467I$	$10.95830 - 3.33174I$	$13.91874 + 2.36228I$
$b = 1.217660 + 0.183120I$		
$u = -1.09609 - 1.06445I$		
$a = -0.488224 + 0.641197I$	$10.95830 + 3.33174I$	$13.91874 - 2.36228I$
$b = -0.738859 - 0.190472I$		
$u = -1.09609 - 1.06445I$		
$a = 0.433762 - 0.247467I$	$10.95830 + 3.33174I$	$13.91874 - 2.36228I$
$b = 1.217660 - 0.183120I$		

Solutions to $I_9^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.414711 + 0.124835I$		
$a = -1.67728 - 0.34824I$	$1.81981 + 2.21397I$	$12.88568 - 4.22289I$
$b = -0.69295 + 1.45068I$		
$u = 0.414711 + 0.124835I$		
$a = -0.56662 + 3.66862I$	$1.81981 + 2.21397I$	$12.88568 - 4.22289I$
$b = -0.652116 - 0.353801I$		
$u = 0.414711 - 0.124835I$		
$a = -1.67728 + 0.34824I$	$1.81981 - 2.21397I$	$12.88568 + 4.22289I$
$b = -0.69295 - 1.45068I$		
$u = 0.414711 - 0.124835I$		
$a = -0.56662 - 3.66862I$	$1.81981 - 2.21397I$	$12.88568 + 4.22289I$
$b = -0.652116 + 0.353801I$		
$u = -0.69295 + 1.45068I$		
$a = -0.023743 + 0.460864I$	$1.81981 + 2.21397I$	$12.88568 - 4.22289I$
$b = 0.414711 + 0.124835I$		
$u = -0.69295 + 1.45068I$		
$a = -0.041119 - 0.266231I$	$1.81981 + 2.21397I$	$12.88568 - 4.22289I$
$b = -0.652116 - 0.353801I$		
$u = -0.69295 - 1.45068I$		
$a = -0.023743 - 0.460864I$	$1.81981 - 2.21397I$	$12.88568 + 4.22289I$
$b = 0.414711 - 0.124835I$		
$u = -0.69295 - 1.45068I$		
$a = -0.041119 + 0.266231I$	$1.81981 - 2.21397I$	$12.88568 + 4.22289I$
$b = -0.652116 + 0.353801I$		
$u = -1.81124$		
$a = 0.025801 + 0.552610I$	-0.882183	4.39120
$b = -0.046733 + 1.000910I$		
$u = -1.81124$		
$a = 0.025801 - 0.552610I$	-0.882183	4.39120
$b = -0.046733 - 1.000910I$		

## X. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_9$	$(u^8 + 2u^6 + u^5 + 4u^4 - u^3 + 4u^2 - u + 1)^2$ $\cdot (u^8 - 7u^7 + 20u^6 - 37u^5 + 52u^4 - 48u^3 + 44u^2 - 19u + 11)$ $\cdot (u^9 - 4u^8 + 10u^7 - 15u^6 + 16u^5 - 14u^4 + 12u^3 - 10u^2 + 6u - 1)$ $\cdot (u^9 - 2u^8 + 4u^7 - 5u^6 + 8u^5 - 10u^4 + 8u^3 - 6u^2 + 2u + 1)$ $\cdot ((u^{15} + 3u^{14} + \dots + 13u + 11)^2)(u^{18} - 16u^{17} + \dots - 240u + 32)$ $\cdot (u^{18} + 2u^{17} + \dots + 11u + 7)^2$
$c_2, c_6, c_{10}$	$(u^8 - 4u^7 + 8u^6 - 14u^5 + 19u^4 - 17u^3 + 11u^2 - 4u + 1)^2$ $\cdot (u^8 + 3u^7 + u^6 + 8u^4 + 6u^3 - 2u^2 - u + 1)$ $\cdot (u^9 - 7u^8 + 18u^7 - 19u^6 + 4u^5 + 5u^4 - 2u^3 - u^2 + 3u - 1)$ $\cdot (u^9 + 5u^8 + 8u^7 + 5u^6 + 4u^5 + 3u^4 + 3u^2 - u + 1)$ $\cdot ((u^{15} + 3u^{14} + \dots + 23u + 1)^2)(u^{18} - 12u^{17} + \dots - 1552u + 352)$ $\cdot (u^{18} + 6u^{17} + \dots + 2u + 1)^2$
$c_3, c_7, c_{11}$	$(u^8 - 3u^7 - 2u^6 + 3u^5 + 22u^4 + 24u^3 + 18u^2 + 3u + 1)$ $\cdot (u^8 + u^7 - 2u^6 - 5u^5 - u^4 + 6u^3 + 8u^2 + 4u + 1)^2$ $\cdot (u^9 + 4u^8 + 5u^7 - 2u^5 + u^4 + 4u^2 + u + 5)$ $\cdot (u^9 + 6u^8 + 15u^7 + 16u^6 + 2u^5 - 9u^4 - 2u^3 + 6u^2 + 3u - 1)$ $\cdot ((u^{15} - 5u^{14} + \dots - 205u + 61)^2)(u^{18} - 7u^{17} + \dots - 40u + 7)^2$ $\cdot (u^{18} + 18u^{17} + \dots + 5632u + 1024)$
$c_4, c_8, c_{12}$	$(u^4 - 3u^3 + 3u^2 - u - 1)^2$ $\cdot (u^8 + 3u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 5u^2 + 3u + 1)^2$ $\cdot (u^9 - 5u^8 + 12u^7 - 16u^6 + 13u^5 - 6u^4 + 2u^3 - u^2 + 2u - 1)$ $\cdot (u^9 - 3u^8 + 4u^7 - 2u^6 + u^5 - 2u^4 + 2u^3 - u^2 - 1)$ $\cdot ((u^{15} + 5u^{14} + \dots + u + 1)^2)(u^{18} - 17u^{17} + \dots - 176u + 32)$ $\cdot (u^{18} + 5u^{17} + \dots + 5u + 1)^2$

## XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_9$	$(y^8 - 9y^7 - 14y^6 + 127y^5 + 668y^4 + 1306y^3 + 1256y^2 + 607y + 121)$ $\cdot (y^8 + 4y^7 + 12y^6 + 23y^5 + 36y^4 + 37y^3 + 22y^2 + 7y + 1)^2$ $\cdot (y^9 + 4y^8 + 12y^7 + 7y^6 + 8y^5 + 26y^3 + 16y^2 + 16y - 1)$ $\cdot (y^9 + 4y^8 + 12y^7 + 15y^6 + 8y^5 - 12y^4 - 14y^3 + 16y^2 + 16y - 1)$ $\cdot (y^{15} + 5y^{14} + \dots - 1107y - 121)^2$ $\cdot (y^{18} + 2y^{17} + \dots + 15616y + 1024)(y^{18} + 10y^{17} + \dots + 313y + 49)^2$
$c_2, c_6, c_{10}$	$(y^8 - 10y^6 - 6y^5 + 31y^4 + 33y^3 + 23y^2 + 6y + 1)^2$ $\cdot (y^8 - 7y^7 + 17y^6 - 24y^5 + 68y^4 - 66y^3 + 32y^2 - 5y + 1)$ $\cdot (y^9 - 13y^8 + 66y^7 - 151y^6 + 126y^5 + 15y^4 - 3y^2 + 7y - 1)$ $\cdot (y^9 - 9y^8 + 22y^7 + 9y^6 - 46y^5 - 65y^4 - 36y^3 - 15y^2 - 5y - 1)$ $\cdot ((y^{15} - 15y^{14} + \dots + 201y - 1)^2)(y^{18} - 30y^{17} + \dots - 8y + 1)^2$ $\cdot (y^{18} - 12y^{17} + \dots + 401664y + 123904)$
$c_3, c_7, c_{11}$	$(y^8 - 13y^7 + 66y^6 + 83y^5 + 288y^4 + 194y^3 + 224y^2 + 27y + 1)$ $\cdot (y^8 - 5y^7 + 12y^6 - 17y^5 + 23y^4 - 16y^3 + 14y^2 + 1)^2$ $\cdot (y^9 - 6y^8 + 21y^7 - 28y^6 - 26y^5 - 31y^4 - 12y^3 - 26y^2 - 39y - 25)$ $\cdot (y^9 - 6y^8 + 37y^7 - 92y^6 + 166y^5 - 179y^4 + 156y^3 - 66y^2 + 21y - 1)$ $\cdot (y^{15} - 19y^{14} + \dots + 9085y - 3721)^2$ $\cdot (y^{18} - 15y^{17} + \dots - 634y + 49)^2$ $\cdot (y^{18} - 10y^{17} + \dots + 1572864y + 1048576)$
$c_4, c_8, c_{12}$	$(y^4 - 3y^3 + y^2 - 7y + 1)^2$ $\cdot (y^8 + y^7 + 3y^6 + 8y^5 + 11y^4 + 8y^3 + 3y^2 + y + 1)^2$ $\cdot (y^9 - y^8 + 6y^7 - 4y^6 + 3y^5 - 10y^4 - 4y^3 - 5y^2 - 2y - 1)$ $\cdot (y^9 - y^8 + 10y^7 + 19y^5 + 22y^4 + 12y^3 - 5y^2 + 2y - 1)$ $\cdot ((y^{15} - 3y^{14} + \dots + 13y - 1)^2)(y^{18} - 7y^{17} + \dots - 1792y + 1024)$ $\cdot (y^{18} - y^{17} + \dots - 5y + 1)^2$