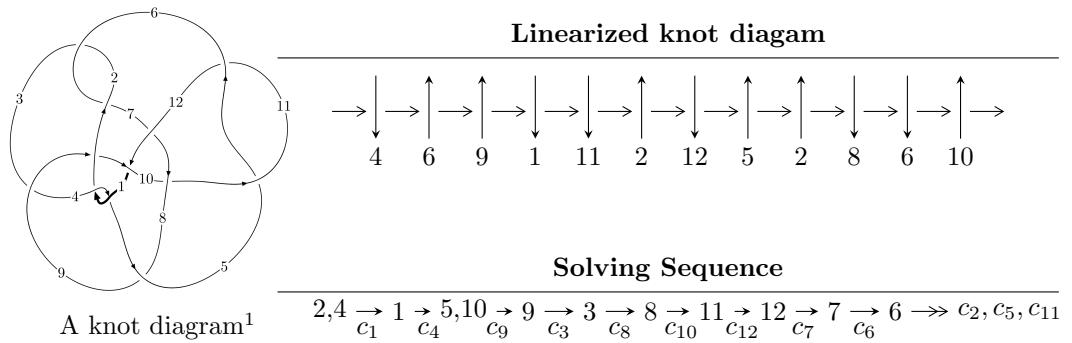


## 12n<sub>0859</sub> (K12n<sub>0859</sub>)



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u = & \langle 2.50974 \times 10^{289} u^{110} + 9.45965 \times 10^{289} u^{109} + \dots + 4.90170 \times 10^{288} b + 2.02264 \times 10^{290}, \\
 & 6.11196 \times 10^{290} u^{110} + 2.58646 \times 10^{291} u^{109} + \dots + 9.31323 \times 10^{289} a + 9.60207 \times 10^{291}, \\
 & u^{111} + 4u^{110} + \dots + 75u + 19 \rangle \\
 I_2^u = & \langle -6.13493 \times 10^{24} u^{36} + 8.28914 \times 10^{25} u^{35} + \dots + 1.90673 \times 10^{25} b + 8.11899 \times 10^{26}, \\
 & 8.06792 \times 10^{26} u^{36} - 5.25168 \times 10^{27} u^{35} + \dots + 2.09740 \times 10^{26} a + 5.96222 \times 10^{27}, u^{37} - 7u^{36} + \dots - 14u + 
 \end{aligned}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 148 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew([http://www.layer8.co.uk/math\(draw/index.htm#Running-draw](http://www.layer8.co.uk/math(draw/index.htm#Running-draw)), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.



**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{111} - 4u^{110} + \cdots + 75u - 19$
$c_2, c_6$	$u^{111} - 3u^{110} + \cdots + 11u + 1$
$c_3$	$u^{111} + u^{110} + \cdots - 11375608u + 498668$
$c_5, c_{11}$	$u^{111} - u^{110} + \cdots + 25708u + 2404$
$c_7$	$u^{111} + 8u^{110} + \cdots - 3750361u + 280259$
$c_8$	$u^{111} - 5u^{110} + \cdots + 1057226u + 206759$
$c_9$	$u^{111} - 2u^{110} + \cdots - 11878814u - 708719$
$c_{10}$	$u^{111} + 11u^{110} + \cdots - 13685u - 1355$
$c_{12}$	$u^{111} + 8u^{110} + \cdots - 59598u - 25569$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{111} + 68y^{110} + \dots - 21507y - 361$
$c_2, c_6$	$y^{111} - 75y^{110} + \dots - 235y - 1$
$c_3$	$y^{111} - 15y^{110} + \dots + 14994491642816y - 248669774224$
$c_5, c_{11}$	$y^{111} - 61y^{110} + \dots + 397749808y - 5779216$
$c_7$	$y^{111} + 10y^{110} + \dots - 12572239397577y - 78545107081$
$c_8$	$y^{111} - 3y^{110} + \dots - 601815422274y - 42749284081$
$c_9$	$y^{111} - 24y^{110} + \dots + 75899128605414y - 502282620961$
$c_{10}$	$y^{111} - 41y^{110} + \dots + 78323675y - 1836025$
$c_{12}$	$y^{111} - 32y^{110} + \dots + 18684218322y - 653773761$























Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.33469 - 1.10518I$		
$a = -0.0009648 + 0.1055420I$	$-7.01760 + 4.66538I$	0
$b = 0.0978189 - 0.0356464I$		



**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{37} - 7u^{36} + \cdots - 14u + 11$
$c_2$	$u^{37} - 2u^{36} + \cdots + 2u - 1$
$c_3$	$u^{37} + 10u^{35} + \cdots + 24u - 4$
$c_4$	$u^{37} + 7u^{36} + \cdots - 14u - 11$
$c_5$	$u^{37} - 13u^{35} + \cdots + 12u + 4$
$c_6$	$u^{37} + 2u^{36} + \cdots + 2u + 1$
$c_7$	$u^{37} + 7u^{36} + \cdots + 54u + 53$
$c_8$	$u^{37} - 2u^{35} + \cdots + 95u + 25$
$c_9$	$u^{37} - u^{36} + \cdots - 3u - 1$
$c_{10}$	$u^{37} + 22u^{36} + \cdots + 18u + 1$
$c_{11}$	$u^{37} - 13u^{35} + \cdots + 12u - 4$
$c_{12}$	$u^{37} - 3u^{36} + \cdots + 7u + 1$



**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{37} + 23y^{36} + \cdots - 970y - 121$
$c_2, c_6$	$y^{37} - 12y^{36} + \cdots - 18y - 1$
$c_3$	$y^{37} + 20y^{36} + \cdots + 2240y^2 - 16$
$c_5, c_{11}$	$y^{37} - 26y^{36} + \cdots + 16y - 16$
$c_7$	$y^{37} - 23y^{36} + \cdots - 197000y - 2809$
$c_8$	$y^{37} - 4y^{36} + \cdots - 13625y - 625$
$c_9$	$y^{37} + 15y^{36} + \cdots - 13y - 1$
$c_{10}$	$y^{37} - 22y^{36} + \cdots + 24y - 1$
$c_{12}$	$y^{37} - 13y^{36} + \cdots + 27y - 1$







Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.08131 - 1.45044I$		
$a = -1.72119 - 0.88843I$	$7.85531 + 1.16591I$	0
$b = -0.820310 - 0.305825I$		
$u = 0.61362 + 1.38794I$		
$a = -0.856322 + 0.234037I$	$-1.89505 - 7.33551I$	0
$b = -0.577930 + 0.946142I$		
$u = 0.61362 - 1.38794I$		
$a = -0.856322 - 0.234037I$	$-1.89505 + 7.33551I$	0
$b = -0.577930 - 0.946142I$		
$u = -0.452526 + 0.035117I$		
$a = -1.24367 - 1.43822I$	$2.70807 - 2.95640I$	$-0.93484 + 2.88220I$
$b = 0.967861 - 0.831701I$		
$u = -0.452526 - 0.035117I$		
$a = -1.24367 + 1.43822I$	$2.70807 + 2.95640I$	$-0.93484 - 2.88220I$
$b = 0.967861 + 0.831701I$		
$u = 1.32694 + 1.08802I$		
$a = -0.116548 + 0.093587I$	$-7.10745 - 4.64492I$	0
$b = 0.044971 + 0.286445I$		
$u = 1.32694 - 1.08802I$		
$a = -0.116548 - 0.093587I$	$-7.10745 + 4.64492I$	0
$b = 0.044971 - 0.286445I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{37} - 7u^{36} + \dots - 14u + 11)(u^{111} - 4u^{110} + \dots + 75u - 19)$
$c_2$	$(u^{37} - 2u^{36} + \dots + 2u - 1)(u^{111} - 3u^{110} + \dots + 11u + 1)$
$c_3$	$(u^{37} + 10u^{35} + \dots + 24u - 4)$ $\cdot (u^{111} + u^{110} + \dots - 11375608u + 498668)$
$c_4$	$(u^{37} + 7u^{36} + \dots - 14u - 11)(u^{111} - 4u^{110} + \dots + 75u - 19)$
$c_5$	$(u^{37} - 13u^{35} + \dots + 12u + 4)(u^{111} - u^{110} + \dots + 25708u + 2404)$
$c_6$	$(u^{37} + 2u^{36} + \dots + 2u + 1)(u^{111} - 3u^{110} + \dots + 11u + 1)$
$c_7$	$(u^{37} + 7u^{36} + \dots + 54u + 53)$ $\cdot (u^{111} + 8u^{110} + \dots - 3750361u + 280259)$
$c_8$	$(u^{37} - 2u^{35} + \dots + 95u + 25)$ $\cdot (u^{111} - 5u^{110} + \dots + 1057226u + 206759)$
$c_9$	$(u^{37} - u^{36} + \dots - 3u - 1)(u^{111} - 2u^{110} + \dots - 1.18788 \times 10^7 u - 708719)$
$c_{10}$	$(u^{37} + 22u^{36} + \dots + 18u + 1)(u^{111} + 11u^{110} + \dots - 13685u - 1355)$
$c_{11}$	$(u^{37} - 13u^{35} + \dots + 12u - 4)(u^{111} - u^{110} + \dots + 25708u + 2404)$
$c_{12}$	$(u^{37} - 3u^{36} + \dots + 7u + 1)(u^{111} + 8u^{110} + \dots - 59598u - 25569)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^{37} + 23y^{36} + \dots - 970y - 121)(y^{111} + 68y^{110} + \dots - 21507y - 361)$
$c_2, c_6$	$(y^{37} - 12y^{36} + \dots - 18y - 1)(y^{111} - 75y^{110} + \dots - 235y - 1)$
$c_3$	$(y^{37} + 20y^{36} + \dots + 2240y^2 - 16) \cdot (y^{111} - 15y^{110} + \dots + 14994491642816y - 248669774224)$
$c_5, c_{11}$	$(y^{37} - 26y^{36} + \dots + 16y - 16) \cdot (y^{111} - 61y^{110} + \dots + 397749808y - 5779216)$
$c_7$	$(y^{37} - 23y^{36} + \dots - 197000y - 2809) \cdot (y^{111} + 10y^{110} + \dots - 12572239397577y - 78545107081)$
$c_8$	$(y^{37} - 4y^{36} + \dots - 13625y - 625) \cdot (y^{111} - 3y^{110} + \dots - 601815422274y - 42749284081)$
$c_9$	$(y^{37} + 15y^{36} + \dots - 13y - 1) \cdot (y^{111} - 24y^{110} + \dots + 75899128605414y - 502282620961)$
$c_{10}$	$(y^{37} - 22y^{36} + \dots + 24y - 1) \cdot (y^{111} - 41y^{110} + \dots + 78323675y - 1836025)$
$c_{12}$	$(y^{37} - 13y^{36} + \dots + 27y - 1) \cdot (y^{111} - 32y^{110} + \dots + 18684218322y - 653773761)$