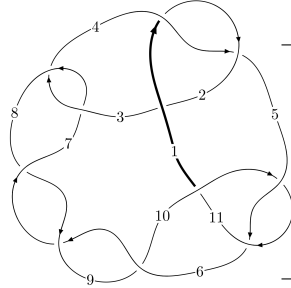
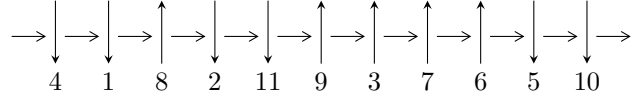


11a<sub>46</sub> (K11a<sub>46</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$6,11 \xrightarrow{c_5} 2,5 \xrightarrow{c_4} 4 \xrightarrow{c_{10}} 10 \xrightarrow{c_{11}} 1 \xrightarrow{c_2} 3 \xrightarrow{c_9} 9 \xrightarrow{c_6} 7 \xrightarrow{c_8} 8 \rightsquigarrow c_1, c_3, c_7$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$\begin{aligned}
 I_1^u &= \langle -u^{15} - u^{14} + 3u^{13} + 4u^{12} - 4u^{11} - 7u^{10} - u^9 + 4u^8 + 4u^7 + 2u^6 - 4u^5 - 4u^4 - u^3 + u^2 + b, \\
 &\quad u^{15} + u^{14} - 3u^{13} - 4u^{12} + 4u^{11} + 7u^{10} + u^9 - 4u^8 - 4u^7 - 2u^6 + 4u^5 + 4u^4 + 2u^3 - u^2 + a, \\
 &\quad u^{16} + u^{15} - 4u^{14} - 5u^{13} + 7u^{12} + 11u^{11} - 3u^{10} - 11u^9 - 5u^8 + 2u^7 + 8u^6 + 6u^5 - 2u^4 - 5u^3 - u^2 + u + 1 \rangle \\
 I_2^u &= \langle -u^{26} + 8u^{24} + \dots + 3u^2 + b, 2u^{27} + u^{26} + \dots + a - 3, u^{28} + u^{27} + \dots - 2u - 1 \rangle \\
 I_3^u &= \langle b - 1, a + 2, u - 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{15} - u^{14} + \dots + u^2 + b, u^{15} + u^{14} + \dots - u^2 + a, u^{16} + u^{15} + \dots + u + 1 \rangle \quad \mathbf{I.}$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{15} - u^{14} + \dots - 2u^3 + u^2 \\ u^{15} + u^{14} + \dots + u^3 - u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{14} + u^{13} + \dots + u^2 - u \\ -u^{14} - u^{13} + \dots + u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{15} - u^{14} + \dots - 2u^3 + u^2 \\ u^{15} + u^{14} + \dots + 4u^4 - u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^6 - u^4 + 1 \\ -u^6 + 2u^4 - u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^9 - 2u^7 + u^5 + 2u^3 - u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^9 - 2u^7 + u^5 + 2u^3 - u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 2u^{15} + 6u^{14} - 6u^{13} - 24u^{12} + 4u^{11} + 46u^{10} + 14u^9 - 32u^8 - 28u^7 - 4u^6 + 16u^5 + 32u^4 + 4u^3 - 10u^2 - 10u + 2$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}$	$u^{16} - u^{15} + \dots - u + 1$
$c_2, c_{11}$	$u^{16} + 9u^{15} + \dots + 3u + 1$
$c_3, c_7$	$u^{16} + 3u^{15} + \dots + 2u + 2$
$c_6, c_8, c_9$	$u^{16} - 3u^{15} + \dots - 11u^2 + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}$	$y^{16} - 9y^{15} + \dots - 3y + 1$
$c_2, c_{11}$	$y^{16} - y^{15} + \dots + 5y + 1$
$c_3, c_7$	$y^{16} - 3y^{15} + \dots - 11y^2 + 4$
$c_6, c_8, c_9$	$y^{16} + 17y^{15} + \dots - 88y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.807171 + 0.504072I$ $a = -0.65855 - 1.36972I$ $b = 0.569167 + 0.512553I$	$1.82651 + 4.13679I$	$2.56414 - 7.87070I$
$u = -0.807171 - 0.504072I$ $a = -0.65855 + 1.36972I$ $b = 0.569167 - 0.512553I$	$1.82651 - 4.13679I$	$2.56414 + 7.87070I$
$u = 1.048260 + 0.400216I$ $a = 1.81547 - 2.15452I$ $b = -2.46363 + 0.89931I$	$-4.21490 - 4.31562I$	$-7.10271 + 5.64590I$
$u = 1.048260 - 0.400216I$ $a = 1.81547 + 2.15452I$ $b = -2.46363 - 0.89931I$	$-4.21490 + 4.31562I$	$-7.10271 - 5.64590I$
$u = -0.034491 + 0.874872I$ $a = -0.0293241 - 0.1171040I$ $b = -0.049834 + 0.783610I$	$-5.17406 - 3.14776I$	$-1.28039 + 2.42611I$
$u = -0.034491 - 0.874872I$ $a = -0.0293241 + 0.1171040I$ $b = -0.049834 - 0.783610I$	$-5.17406 + 3.14776I$	$-1.28039 - 2.42611I$
$u = -1.079150 + 0.504952I$ $a = -1.83629 - 1.53825I$ $b = 2.26756 - 0.09714I$	$-2.62432 + 9.39287I$	$-3.86862 - 9.95391I$
$u = -1.079150 - 0.504952I$ $a = -1.83629 + 1.53825I$ $b = 2.26756 + 0.09714I$	$-2.62432 - 9.39287I$	$-3.86862 + 9.95391I$
$u = 0.735290 + 0.237976I$ $a = -0.78828 - 1.71780I$ $b = 0.51567 + 1.34529I$	$-1.32039 - 1.29101I$	$-3.35201 + 4.88471I$
$u = 0.735290 - 0.237976I$ $a = -0.78828 + 1.71780I$ $b = 0.51567 - 1.34529I$	$-1.32039 + 1.29101I$	$-3.35201 - 4.88471I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.255070 + 0.472625I$		
$a = 2.56417 - 1.25500I$	$-12.8673 - 6.3576I$	$-8.01117 + 3.79413I$
$b = -3.70009 - 0.87285I$		
$u = 1.255070 - 0.472625I$		
$a = 2.56417 + 1.25500I$	$-12.8673 + 6.3576I$	$-8.01117 - 3.79413I$
$b = -3.70009 + 0.87285I$		
$u = -1.258180 + 0.499599I$		
$a = -2.49673 - 1.17352I$	$-12.4913 + 13.0634I$	$-7.30770 - 8.20106I$
$b = 3.54634 - 1.07442I$		
$u = -1.258180 - 0.499599I$		
$a = -2.49673 + 1.17352I$	$-12.4913 - 13.0634I$	$-7.30770 + 8.20106I$
$b = 3.54634 + 1.07442I$		
$u = -0.359617 + 0.529211I$		
$a = -0.070464 - 0.486206I$	$1.49968 - 0.85752I$	$4.35846 + 1.06718I$
$b = -0.185176 + 0.429100I$		
$u = -0.359617 - 0.529211I$		
$a = -0.070464 + 0.486206I$	$1.49968 + 0.85752I$	$4.35846 - 1.06718I$
$b = -0.185176 - 0.429100I$		

**II.**

$$I_2^u = \langle -u^{26} + 8u^{24} + \dots + 3u^2 + b, 2u^{27} + u^{26} + \dots + a - 3, u^{28} + u^{27} + \dots - 2u - 1 \rangle$$

**(i) Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^{27} - u^{26} + \dots + 4u + 3 \\ u^{26} - 8u^{24} + \dots - 4u^3 - 3u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2u^{27} - 17u^{25} + \dots - 5u - 3 \\ u^{25} - 7u^{23} + \dots + 4u^2 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2u^{27} + 16u^{25} + \dots + 5u + 3 \\ u^{22} - 6u^{20} + \dots - 3u^2 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^6 - u^4 + 1 \\ -u^6 + 2u^4 - u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^9 - 2u^7 + u^5 + 2u^3 - u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^9 - 2u^7 + u^5 + 2u^3 - u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes**

$$= 4u^{24} - 28u^{22} - 4u^{21} + 88u^{20} + 24u^{19} - 140u^{18} - 64u^{17} + 80u^{16} + 80u^{15} + 96u^{14} - 20u^{13} - 188u^{12} - 72u^{11} + 80u^{10} + 76u^9 + 60u^8 - 8u^7 - 56u^6 - 28u^5 + 4u^4 + 8u^3 + 8u^2 - 2$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}$	$u^{28} - u^{27} + \dots + 2u - 1$
$c_2, c_{11}$	$u^{28} + 17u^{27} + \dots - 4u + 1$
$c_3, c_7$	$(u^{14} - u^{13} + \dots - u - 1)^2$
$c_6, c_8, c_9$	$(u^{14} - 3u^{13} + \dots - 5u + 1)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}$	$y^{28} - 17y^{27} + \dots + 4y + 1$
$c_2, c_{11}$	$y^{28} - 13y^{27} + \dots - 28y + 1$
$c_3, c_7$	$(y^{14} - 3y^{13} + \dots - 5y + 1)^2$
$c_6, c_8, c_9$	$(y^{14} + 17y^{13} + \dots - y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.997731 + 0.254321I$ $a = -0.812406 - 0.190507I$ $b = 0.788217 + 0.159208I$	$-1.87700 - 0.85224I$	$-4.40198 + 0.38712I$
$u = 0.997731 - 0.254321I$ $a = -0.812406 + 0.190507I$ $b = 0.788217 - 0.159208I$	$-1.87700 + 0.85224I$	$-4.40198 - 0.38712I$
$u = -0.053235 + 0.909759I$ $a = -1.181850 + 0.612019I$ $b = -2.28006 - 0.09309I$	$-8.82756 - 8.01486I$	$-4.36796 + 5.37427I$
$u = -0.053235 - 0.909759I$ $a = -1.181850 - 0.612019I$ $b = -2.28006 + 0.09309I$	$-8.82756 + 8.01486I$	$-4.36796 - 5.37427I$
$u = -1.051200 + 0.342720I$ $a = 2.04075 + 0.52134I$ $b = -1.21015 + 1.19657I$	$-4.64212 + 1.98638I$	$-7.34408 - 5.08636I$
$u = -1.051200 - 0.342720I$ $a = 2.04075 - 0.52134I$ $b = -1.21015 - 1.19657I$	$-4.64212 - 1.98638I$	$-7.34408 + 5.08636I$
$u = -1.013550 + 0.462956I$ $a = 0.550084 - 0.313876I$ $b = -0.418870 + 0.084661I$	$-0.31026 + 4.88256I$	$-0.31401 - 6.44337I$
$u = -1.013550 - 0.462956I$ $a = 0.550084 + 0.313876I$ $b = -0.418870 - 0.084661I$	$-0.31026 - 4.88256I$	$-0.31401 + 6.44337I$
$u = 0.009396 + 0.884908I$ $a = 1.24317 + 0.68253I$ $b = 2.23988 + 0.06633I$	$-9.09089 + 1.51934I$	$-4.87778 - 0.64840I$
$u = 0.009396 - 0.884908I$ $a = 1.24317 - 0.68253I$ $b = 2.23988 - 0.06633I$	$-9.09089 - 1.51934I$	$-4.87778 + 0.64840I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.13074$ $a = -1.65240$ $b = 1.34469$	-2.55923	2.09270
$u = -0.644858 + 0.497518I$ $a = 0.327243 + 0.252473I$ $b = -0.861939 - 0.330036I$	2.27008	$4.70520 + 0.I$
$u = -0.644858 - 0.497518I$ $a = 0.327243 - 0.252473I$ $b = -0.861939 + 0.330036I$	2.27008	$4.70520 + 0.I$
$u = 1.180860 + 0.240994I$ $a = -1.86418 + 0.50864I$ $b = 1.72950 + 0.72402I$	$-4.64212 + 1.98638I$	$-7.34408 - 5.08636I$
$u = 1.180860 - 0.240994I$ $a = -1.86418 - 0.50864I$ $b = 1.72950 - 0.72402I$	$-4.64212 - 1.98638I$	$-7.34408 + 5.08636I$
$u = -0.768027$ $a = 2.43278$ $b = -0.304273$	-2.55923	2.09270
$u = -0.266232 + 0.686741I$ $a = -0.522796 + 0.802943I$ $b = -1.51666 - 0.33236I$	$-0.31026 - 4.88256I$	$-0.31401 + 6.44337I$
$u = -0.266232 - 0.686741I$ $a = -0.522796 - 0.802943I$ $b = -1.51666 + 0.33236I$	$-0.31026 + 4.88256I$	$-0.31401 - 6.44337I$
$u = 1.255170 + 0.447404I$ $a = -0.697496 - 0.632935I$ $b = 0.257772 + 0.768928I$	$-9.09089 - 1.51934I$	$-4.87778 + 0.64840I$
$u = 1.255170 - 0.447404I$ $a = -0.697496 + 0.632935I$ $b = 0.257772 - 0.768928I$	$-9.09089 + 1.51934I$	$-4.87778 - 0.64840I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.245950 + 0.483423I$ $a = 0.644350 - 0.639100I$ $b = -0.133052 + 0.709234I$	$-8.82756 + 8.01486I$	$-4.36796 - 5.37427I$
$u = -1.245950 - 0.483423I$ $a = 0.644350 + 0.639100I$ $b = -0.133052 - 0.709234I$	$-8.82756 - 8.01486I$	$-4.36796 + 5.37427I$
$u = -1.257930 + 0.462599I$ $a = 1.97998 + 0.69687I$ $b = -2.24068 + 1.79013I$	$-12.94110 + 3.26499I$	$-8.09314 - 2.49004I$
$u = -1.257930 - 0.462599I$ $a = 1.97998 - 0.69687I$ $b = -2.24068 - 1.79013I$	$-12.94110 - 3.26499I$	$-8.09314 + 2.49004I$
$u = 1.279730 + 0.439354I$ $a = -1.95695 + 0.70259I$ $b = 2.35927 + 1.64819I$	$-12.94110 + 3.26499I$	$-8.09314 - 2.49004I$
$u = 1.279730 - 0.439354I$ $a = -1.95695 - 0.70259I$ $b = 2.35927 - 1.64819I$	$-12.94110 - 3.26499I$	$-8.09314 + 2.49004I$
$u = 0.128720 + 0.430400I$ $a = 0.35991 + 1.87835I$ $b = 1.266560 + 0.022630I$	$-1.87700 + 0.85224I$	$-4.40198 - 0.38712I$
$u = 0.128720 - 0.430400I$ $a = 0.35991 - 1.87835I$ $b = 1.266560 - 0.022630I$	$-1.87700 - 0.85224I$	$-4.40198 + 0.38712I$

$$\text{III. } I_3^u = \langle b - 1, a + 2, u - 1 \rangle$$

**(i) Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -12**

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_5$	$u - 1$
$c_2, c_4, c_{10}$ $c_{11}$	$u + 1$
$c_3, c_6, c_7$ $c_8, c_9$	$u$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_{10}, c_{11}$	$y - 1$
$c_3, c_6, c_7$ $c_8, c_9$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -2.00000$	-3.28987	-12.0000
$b = 1.00000$		



#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u - 1)(u^{16} - u^{15} + \dots - u + 1)(u^{28} - u^{27} + \dots + 2u - 1)$
$c_2, c_{11}$	$(u + 1)(u^{16} + 9u^{15} + \dots + 3u + 1)(u^{28} + 17u^{27} + \dots - 4u + 1)$
$c_3, c_7$	$u(u^{14} - u^{13} + \dots - u - 1)^2(u^{16} + 3u^{15} + \dots + 2u + 2)$
$c_4, c_{10}$	$(u + 1)(u^{16} - u^{15} + \dots - u + 1)(u^{28} - u^{27} + \dots + 2u - 1)$
$c_6, c_8, c_9$	$u(u^{14} - 3u^{13} + \dots - 5u + 1)^2(u^{16} - 3u^{15} + \dots - 11u^2 + 4)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}$	$(y - 1)(y^{16} - 9y^{15} + \dots - 3y + 1)(y^{28} - 17y^{27} + \dots + 4y + 1)$
$c_2, c_{11}$	$(y - 1)(y^{16} - y^{15} + \dots + 5y + 1)(y^{28} - 13y^{27} + \dots - 28y + 1)$
$c_3, c_7$	$y(y^{14} - 3y^{13} + \dots - 5y + 1)^2(y^{16} - 3y^{15} + \dots - 11y^2 + 4)$
$c_6, c_8, c_9$	$y(y^{14} + 17y^{13} + \dots - y + 1)^2(y^{16} + 17y^{15} + \dots - 88y + 16)$