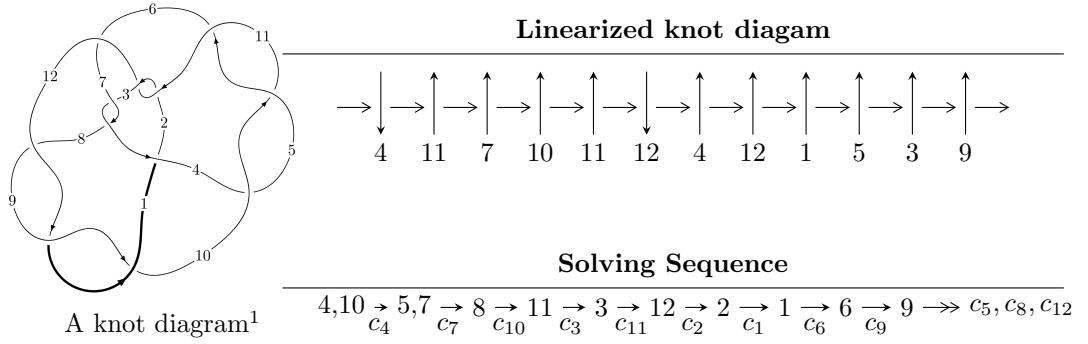


## $12n_{0882}$ ( $K12n_{0882}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 4u^{12} - 8u^{11} - 26u^{10} + 41u^9 + 59u^8 - 69u^7 - 42u^6 + 9u^5 - 10u^4 + 56u^3 + u^2 + 13b - 5u + 10, \\
 &\quad - 4u^{12} + 8u^{11} + 26u^{10} - 41u^9 - 59u^8 + 69u^7 + 42u^6 - 9u^5 + 10u^4 - 69u^3 - u^2 + 13a + 31u - 10, \\
 &\quad u^{13} + u^{12} - 6u^{11} - 6u^{10} + 13u^9 + 14u^8 - 7u^7 - 13u^6 - 12u^5 + 13u^3 + 6u^2 + 2u + 1 \rangle \\
 I_2^u &= \langle -5.18174 \times 10^{46}u^{47} - 1.01683 \times 10^{47}u^{46} + \dots + 3.77343 \times 10^{47}b - 4.53377 \times 10^{47}, \\
 &\quad 2.81502 \times 10^{47}u^{47} + 3.21473 \times 10^{47}u^{46} + \dots + 1.25781 \times 10^{47}a + 4.62967 \times 10^{48}, u^{48} + u^{47} + \dots + 20u + 1 \rangle \\
 I_3^u &= \langle -u^2 + b + 1, -u^3 + u^2 + a + 2u - 1, u^5 - 3u^3 + 2u + 1 \rangle \\
 I_4^u &= \langle -u^2 + b + 1, -2u^7 - u^6 + 11u^5 + 3u^4 - 18u^3 + 3u^2 + a + 8u - 9, \\
 &\quad u^8 - 5u^6 + u^5 + 7u^4 - 4u^3 - 2u^2 + 4u - 1 \rangle \\
 I_5^u &= \langle b + 1, a, u - 1 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 75 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 4u^{12} - 8u^{11} + \dots + 13b + 10, -4u^{12} + 8u^{11} + \dots + 13a - 10, u^{13} + u^{12} + \dots + 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.307692u^{12} - 0.615385u^{11} + \dots - 2.38462u + 0.769231 \\ -0.307692u^{12} + 0.615385u^{11} + \dots + 0.384615u - 0.769231 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 - 2u \\ -0.307692u^{12} + 0.615385u^{11} + \dots + 0.384615u - 0.769231 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.538462u^{12} - 0.0769231u^{11} + \dots + 3.07692u + 1.84615 \\ -1.07692u^{12} + 0.153846u^{11} + \dots - 2.15385u - 0.692308 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 - 1 \\ -0.692308u^{12} + 0.384615u^{11} + \dots + 1.61538u - 0.230769 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.46154u^{12} + 0.0769231u^{11} + \dots + 2.92308u + 2.15385 \\ -1.46154u^{12} - 0.0769231u^{11} + \dots - 2.92308u - 1.15385 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1.46154u^{12} - 0.0769231u^{11} + \dots - 2.92308u - 1.15385 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -1.38462u^{12} + 0.769231u^{11} + \dots - 0.769231u - 1.46154 \end{pmatrix}$$

(ii) **Obstruction class** = -1

$$(iii) \text{ Cusp Shapes} = \frac{42}{13}u^{12} + \frac{20}{13}u^{11} - 18u^{10} - \frac{122}{13}u^9 + \frac{483}{13}u^8 + \frac{309}{13}u^7 - \frac{285}{13}u^6 - \frac{367}{13}u^5 - \frac{300}{13}u^4 + \frac{94}{13}u^3 + \frac{394}{13}u^2 + \frac{162}{13}u + \frac{157}{13}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{13} - 12u^{12} + \cdots + 352u - 32$
$c_2, c_3, c_7$ $c_{11}$	$u^{13} - 3u^{11} + 9u^9 + u^8 - 12u^7 + u^6 + 16u^5 - u^4 - 11u^3 + 3u^2 + 4u - 1$
$c_4, c_5, c_8$ $c_9, c_{10}, c_{12}$	$u^{13} - u^{12} + \cdots + 2u - 1$
$c_6$	$u^{13} + 11u^{12} + \cdots - 208u - 56$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{13} + 8y^{12} + \cdots + 42496y - 1024$
$c_2, c_3, c_7$ $c_{11}$	$y^{13} - 6y^{12} + \cdots + 22y - 1$
$c_4, c_5, c_8$ $c_9, c_{10}, c_{12}$	$y^{13} - 13y^{12} + \cdots - 8y - 1$
$c_6$	$y^{13} + y^{12} + \cdots + 5408y - 3136$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.171620 + 0.859681I$		
$a = -0.34697 - 1.56070I$	$-2.17962 - 5.84511I$	$7.45794 + 6.04290I$
$b = 1.065670 - 0.718049I$		
$u = -0.171620 - 0.859681I$		
$a = -0.34697 + 1.56070I$	$-2.17962 + 5.84511I$	$7.45794 - 6.04290I$
$b = 1.065670 + 0.718049I$		
$u = -1.309140 + 0.064534I$		
$a = -0.581299 - 0.674191I$	$8.82263 + 2.58229I$	$16.9820 - 3.0015I$
$b = 0.972284 + 0.876654I$		
$u = -1.309140 - 0.064534I$		
$a = -0.581299 + 0.674191I$	$8.82263 - 2.58229I$	$16.9820 + 3.0015I$
$b = 0.972284 - 0.876654I$		
$u = 1.356440 + 0.275517I$		
$a = 0.256447 + 0.156488I$	$5.13873 + 2.17385I$	$13.57691 - 0.52106I$
$b = -0.782477 + 0.792358I$		
$u = 1.356440 - 0.275517I$		
$a = 0.256447 - 0.156488I$	$5.13873 - 2.17385I$	$13.57691 + 0.52106I$
$b = -0.782477 - 0.792358I$		
$u = 1.356860 + 0.395151I$		
$a = -1.72651 + 1.21374I$	$9.39305 + 5.41911I$	$19.2364 - 4.1129I$
$b = 0.875267 + 0.116755I$		
$u = 1.356860 - 0.395151I$		
$a = -1.72651 - 1.21374I$	$9.39305 - 5.41911I$	$19.2364 + 4.1129I$
$b = 0.875267 - 0.116755I$		
$u = -0.537178$		
$a = 1.16207$	0.805138	11.7720
$b = -0.242725$		
$u = -1.48836 + 0.39264I$		
$a = 1.67676 + 0.98279I$	$8.6054 - 15.1865I$	$15.2811 + 7.9689I$
$b = -1.30871 + 0.78070I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.48836 - 0.39264I$		
$a = 1.67676 - 0.98279I$	$8.6054 + 15.1865I$	$15.2811 - 7.9689I$
$b = -1.30871 - 0.78070I$		
$u = 0.024401 + 0.393610I$		
$a = 0.640545 - 1.244220I$	$1.07099 - 1.38837I$	$7.07977 + 4.85651I$
$b = -0.700673 + 0.396722I$		
$u = 0.024401 - 0.393610I$		
$a = 0.640545 + 1.244220I$	$1.07099 + 1.38837I$	$7.07977 - 4.85651I$
$b = -0.700673 - 0.396722I$		

### III.

$$I_2^u = \langle -5.18 \times 10^{46}u^{47} - 1.02 \times 10^{47}u^{46} + \dots + 3.77 \times 10^{47}b - 4.53 \times 10^{47}, 2.82 \times 10^{47}u^{47} + 3.21 \times 10^{47}u^{46} + \dots + 1.26 \times 10^{47}a + 4.63 \times 10^{48}, u^{48} + u^{47} + \dots + 20u + 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2.23803u^{47} - 2.55582u^{46} + \dots - 95.9559u - 36.8074 \\ 0.137322u^{47} + 0.269470u^{46} + \dots + 10.2860u + 1.20150 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2.10071u^{47} - 2.28635u^{46} + \dots - 85.6699u - 35.6059 \\ 0.137322u^{47} + 0.269470u^{46} + \dots + 10.2860u + 1.20150 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1.66504u^{47} - 1.59037u^{46} + \dots - 127.758u - 32.3177 \\ 0.0330654u^{47} + 0.122014u^{46} + \dots - 10.8225u + 0.0377011 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2.91125u^{47} - 2.61233u^{46} + \dots - 182.706u - 53.5737 \\ 0.168578u^{47} + 0.0577104u^{46} + \dots - 0.407278u + 0.897363 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.68717u^{47} - 1.75245u^{46} + \dots - 125.467u - 32.2876 \\ 0.0461378u^{47} + 0.188914u^{46} + \dots - 11.3519u - 0.0721935 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1.64103u^{47} - 1.56354u^{46} + \dots - 136.819u - 32.3598 \\ 0.0461378u^{47} + 0.188914u^{46} + \dots - 11.3519u - 0.0721935 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2.76666u^{47} + 2.69855u^{46} + \dots + 205.087u + 52.5080 \\ -0.111644u^{47} + 0.153944u^{46} + \dots + 8.10592u - 0.451941 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-2.00373u^{47} - 2.03203u^{46} + \dots - 42.9306u - 8.93702$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{24} + 2u^{23} + \dots - 20u - 1)^2$
$c_2, c_3, c_7$ $c_{11}$	$u^{48} - u^{47} + \dots - 197u + 73$
$c_4, c_5, c_8$ $c_9, c_{10}, c_{12}$	$u^{48} - u^{47} + \dots - 20u + 1$
$c_6$	$(u^{24} - 5u^{23} + \dots + 15u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{24} + 4y^{23} + \cdots - 522y + 1)^2$
$c_2, c_3, c_7$ $c_{11}$	$y^{48} - 23y^{47} + \cdots - 76039y + 5329$
$c_4, c_5, c_8$ $c_9, c_{10}, c_{12}$	$y^{48} - 43y^{47} + \cdots - 216y + 1$
$c_6$	$(y^{24} - 3y^{23} + \cdots - 135y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.379137 + 0.976493I$		
$a = -0.471549 + 1.157640I$	$2.67292 + 10.25690I$	$12.1975 - 7.6788I$
$b = 1.29469 + 0.67005I$		
$u = 0.379137 - 0.976493I$		
$a = -0.471549 - 1.157640I$	$2.67292 - 10.25690I$	$12.1975 + 7.6788I$
$b = 1.29469 - 0.67005I$		
$u = -0.021423 + 0.948358I$		
$a = 0.401732 + 0.737665I$	$4.94291 - 0.58720I$	$16.0412 - 0.8168I$
$b = -0.856499 + 0.135005I$		
$u = -0.021423 - 0.948358I$		
$a = 0.401732 - 0.737665I$	$4.94291 + 0.58720I$	$16.0412 + 0.8168I$
$b = -0.856499 - 0.135005I$		
$u = -1.023260 + 0.490646I$		
$a = 0.476231 + 0.027830I$	$0.464120 + 1.081590I$	$8.00000 - 2.00672I$
$b = -1.044720 - 0.584882I$		
$u = -1.023260 - 0.490646I$		
$a = 0.476231 - 0.027830I$	$0.464120 - 1.081590I$	$8.00000 + 2.00672I$
$b = -1.044720 + 0.584882I$		
$u = -0.379291 + 0.739173I$		
$a = 0.316811 + 0.748267I$	$-0.51929 - 4.00862I$	$8.65058 + 5.80685I$
$b = 0.248462 + 1.064600I$		
$u = -0.379291 - 0.739173I$		
$a = 0.316811 - 0.748267I$	$-0.51929 + 4.00862I$	$8.65058 - 5.80685I$
$b = 0.248462 - 1.064600I$		
$u = 1.135680 + 0.336882I$		
$a = 0.864140 - 0.699527I$	$-0.51929 + 4.00862I$	$8.00000 - 5.80685I$
$b = -0.713544 - 0.730081I$		
$u = 1.135680 - 0.336882I$		
$a = 0.864140 + 0.699527I$	$-0.51929 - 4.00862I$	$8.00000 + 5.80685I$
$b = -0.713544 + 0.730081I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.750478 + 0.292577I$		
$a = 1.176600 + 0.468222I$	0.664158	$9.39053 + 0.I$
$b = -0.319389 + 0.477318I$		
$u = -0.750478 - 0.292577I$		
$a = 1.176600 - 0.468222I$	0.664158	$9.39053 + 0.I$
$b = -0.319389 - 0.477318I$		
$u = 1.163220 + 0.303346I$		
$a = -0.223618 - 0.467491I$	4.64466	$15.0647 + 0.I$
$b = -1.004700 + 0.471049I$		
$u = 1.163220 - 0.303346I$		
$a = -0.223618 + 0.467491I$	4.64466	$15.0647 + 0.I$
$b = -1.004700 - 0.471049I$		
$u = 0.141459 + 0.765036I$		
$a = 0.561104 - 0.769052I$	-3.53422	$4.26168 + 0.I$
$b = 0.623240 - 0.846147I$		
$u = 0.141459 - 0.765036I$		
$a = 0.561104 + 0.769052I$	-3.53422	$4.26168 + 0.I$
$b = 0.623240 + 0.846147I$		
$u = 0.068175 + 0.762824I$		
$a = 0.696604 + 1.029800I$	1.27885 + 3.92180I	$9.29302 - 3.73808I$
$b = 0.970507 + 0.650047I$		
$u = 0.068175 - 0.762824I$		
$a = 0.696604 - 1.029800I$	1.27885 - 3.92180I	$9.29302 + 3.73808I$
$b = 0.970507 - 0.650047I$		
$u = 1.235930 + 0.167013I$		
$a = -0.657445 - 0.412560I$	4.65694 + 3.47868I	0
$b = 0.705420 + 0.391760I$		
$u = 1.235930 - 0.167013I$		
$a = -0.657445 + 0.412560I$	4.65694 - 3.47868I	0
$b = 0.705420 - 0.391760I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.916403 + 0.885493I$		
$a = 0.391708 - 0.248635I$	$4.14619 - 4.10761I$	0
$b = -1.329710 + 0.460814I$		
$u = 0.916403 - 0.885493I$		
$a = 0.391708 + 0.248635I$	$4.14619 + 4.10761I$	0
$b = -1.329710 - 0.460814I$		
$u = -1.265470 + 0.153865I$		
$a = -2.80490 - 0.73050I$	$4.94291 - 0.58720I$	0
$b = 0.791562 + 0.363762I$		
$u = -1.265470 - 0.153865I$		
$a = -2.80490 + 0.73050I$	$4.94291 + 0.58720I$	0
$b = 0.791562 - 0.363762I$		
$u = -1.263720 + 0.231617I$		
$a = 2.48042 + 2.19572I$	$4.14619 - 4.10761I$	0
$b = -0.811085 + 0.535687I$		
$u = -1.263720 - 0.231617I$		
$a = 2.48042 - 2.19572I$	$4.14619 + 4.10761I$	0
$b = -0.811085 - 0.535687I$		
$u = -1.28856$		
$a = -0.869778$	14.0810	25.5770
$b = -0.755603$		
$u = 1.32785$		
$a = 4.15788$	14.6478	0
$b = -0.885530$		
$u = 1.330000 + 0.048649I$		
$a = -2.39749 + 0.12309I$	$9.08685 + 4.24572I$	0
$b = 1.065850 + 0.841425I$		
$u = 1.330000 - 0.048649I$		
$a = -2.39749 - 0.12309I$	$9.08685 - 4.24572I$	0
$b = 1.065850 - 0.841425I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.309300 + 0.318007I$		
$a = 0.889440 + 0.821935I$	$5.58448 - 7.81589I$	0
$b = -0.928244 + 0.711653I$		
$u = -1.309300 - 0.318007I$		
$a = 0.889440 - 0.821935I$	$5.58448 + 7.81589I$	0
$b = -0.928244 - 0.711653I$		
$u = -1.316980 + 0.405826I$		
$a = -0.548637 + 0.081279I$	$9.08685 - 4.24572I$	0
$b = 0.803853 + 0.148006I$		
$u = -1.316980 - 0.405826I$		
$a = -0.548637 - 0.081279I$	$9.08685 + 4.24572I$	0
$b = 0.803853 - 0.148006I$		
$u = -0.087131 + 0.611347I$		
$a = 0.35264 + 2.45893I$	$0.464120 + 1.081590I$	$8.16075 - 2.00672I$
$b = 0.721176 + 0.611639I$		
$u = -0.087131 - 0.611347I$		
$a = 0.35264 - 2.45893I$	$0.464120 - 1.081590I$	$8.16075 + 2.00672I$
$b = 0.721176 - 0.611639I$		
$u = -1.373810 + 0.321857I$		
$a = -0.344264 + 0.528075I$	$1.27885 - 3.92180I$	0
$b = -0.621802 - 0.993232I$		
$u = -1.373810 - 0.321857I$		
$a = -0.344264 - 0.528075I$	$1.27885 + 3.92180I$	0
$b = -0.621802 + 0.993232I$		
$u = 1.36990 + 0.36882I$		
$a = 1.75795 - 1.37725I$	$2.67292 + 10.25690I$	0
$b = -1.073560 - 0.763448I$		
$u = 1.36990 - 0.36882I$		
$a = 1.75795 + 1.37725I$	$2.67292 - 10.25690I$	0
$b = -1.073560 + 0.763448I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.49633 + 0.29266I$		
$a = -0.376487 - 0.561865I$	$5.58448 + 7.81589I$	0
$b = -0.34302 + 1.38502I$		
$u = 1.49633 - 0.29266I$		
$a = -0.376487 + 0.561865I$	$5.58448 - 7.81589I$	0
$b = -0.34302 - 1.38502I$		
$u = 1.65947$		
$a = -1.72670$	10.1445	0
$b = 1.72233$		
$u = -1.66105$		
$a = -1.80640$	14.0810	0
$b = 2.14588$		
$u = -1.81988$		
$a = -1.44716$	14.6478	0
$b = 1.67660$		
$u = -0.024167 + 0.177554I$		
$a = -0.54655 + 4.54825I$	$4.65694 - 3.47868I$	$16.3031 + 8.4838I$
$b = -1.041510 + 0.853951I$		
$u = -0.024167 - 0.177554I$		
$a = -0.54655 - 4.54825I$	$4.65694 + 3.47868I$	$16.3031 - 8.4838I$
$b = -1.041510 - 0.853951I$		
$u = -0.0602179$		
$a = -35.2967$	10.1445	-9.41450
$b = 0.822371$		

$$\text{III. } I_3^u = \langle -u^2 + b + 1, -u^3 + u^2 + a + 2u - 1, u^5 - 3u^3 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 - u^2 - 2u + 1 \\ u^2 - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 - 2u \\ u^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^4 + 2u^2 - 1 \\ u^4 - 2u^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 - 1 \\ -u^3 - u^2 + 2u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4 - u^3 + 2u^2 + u - 1 \\ u^4 + u^3 - 2u^2 - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ u^4 + u^3 - 2u^2 - u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^4 + u^3 - u^2 - u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-2u^4 - 3u^3 + 3u^2 + 2u + 17$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^5 - 2u^4 + 5u^3 - 4u^2 - 1$
$c_2, c_7$	$u^5 + u^4 - u^3 - u^2 + 1$
$c_3, c_{11}$	$u^5 - u^4 - u^3 + u^2 - 1$
$c_4, c_5, c_8$ $c_9$	$u^5 - 3u^3 + 2u + 1$
$c_6$	$u^5 + 2u^4 + 3u^3 + 3u^2 + 3u + 1$
$c_{10}, c_{12}$	$u^5 - 3u^3 + 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^5 + 6y^4 + 9y^3 - 20y^2 - 8y - 1$
$c_2, c_3, c_7$ $c_{11}$	$y^5 - 3y^4 + 3y^3 - 3y^2 + 2y - 1$
$c_4, c_5, c_8$ $c_9, c_{10}, c_{12}$	$y^5 - 6y^4 + 13y^3 - 12y^2 + 4y - 1$
$c_6$	$y^5 + 2y^4 + 3y^3 + 5y^2 + 3y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.297630 + 0.272489I$		
$a = -1.308900 + 0.104091I$	$7.56155 + 5.69445I$	$14.5549 - 5.9553I$
$b = 0.609585 + 0.707177I$		
$u = 1.297630 - 0.272489I$		
$a = -1.308900 - 0.104091I$	$7.56155 - 5.69445I$	$14.5549 + 5.9553I$
$b = 0.609585 - 0.707177I$		
$u = -0.516079 + 0.312340I$		
$a = 1.87697 - 0.08320I$	$2.00050 + 0.85728I$	$16.5843 - 0.7821I$
$b = -0.831219 - 0.322384I$		
$u = -0.516079 - 0.312340I$		
$a = 1.87697 + 0.08320I$	$2.00050 - 0.85728I$	$16.5843 + 0.7821I$
$b = -0.831219 + 0.322384I$		
$u = -1.56310$		
$a = -2.13614$	17.0644	20.7220
$b = 1.44327$		

**IV.**

$$I_4^u = \langle -u^2 + b + 1, -2u^7 - u^6 + \dots + a - 9, u^8 - 5u^6 + u^5 + 7u^4 - 4u^3 - 2u^2 + 4u - 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2u^7 + u^6 - 11u^5 - 3u^4 + 18u^3 - 3u^2 - 8u + 9 \\ u^2 - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 2u^7 + u^6 - 11u^5 - 3u^4 + 18u^3 - 2u^2 - 8u + 8 \\ u^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -3u^7 - u^6 + 14u^5 + u^4 - 18u^3 + 6u^2 + 6u - 7 \\ u^4 - 2u^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 4u^7 + 2u^6 - 19u^5 - 5u^4 + 26u^3 - 5u^2 - 11u + 12 \\ u^5 - 4u^3 + u^2 + 3u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -3u^7 + 14u^5 - 2u^4 - 17u^3 + 7u^2 + 4u - 7 \\ -u^6 + 4u^4 - u^3 - 3u^2 + 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -3u^7 - u^6 + 14u^5 + 2u^4 - 18u^3 + 4u^2 + 6u - 7 \\ -u^6 + 4u^4 - u^3 - 3u^2 + 2u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -3u^7 + 15u^5 - 2u^4 - 21u^3 + 9u^2 + 7u - 11 \\ u^7 + u^6 - 4u^5 - 3u^4 + 4u^3 + u^2 - u + 1 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $10u^7 + 5u^6 - 45u^5 - 10u^4 + 60u^3 - 15u^2 - 25u + 42$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^4 + 3u^3 + 4u^2 + 4u + 1)^2$
$c_2, c_7$	$u^8 + 2u^7 - 3u^6 - 5u^5 + 5u^4 + 6u^3 - u^2 - 3u - 1$
$c_3, c_{11}$	$u^8 - 2u^7 - 3u^6 + 5u^5 + 5u^4 - 6u^3 - u^2 + 3u - 1$
$c_4, c_5, c_8$ $c_9$	$u^8 - 5u^6 + u^5 + 7u^4 - 4u^3 - 2u^2 + 4u - 1$
$c_6$	$(u^4 - u^3 + u^2 + u - 1)^2$
$c_{10}, c_{12}$	$u^8 - 5u^6 - u^5 + 7u^4 + 4u^3 - 2u^2 - 4u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^4 - y^3 - 6y^2 - 8y + 1)^2$
$c_2, c_3, c_7$ $c_{11}$	$y^8 - 10y^7 + 39y^6 - 81y^5 + 101y^4 - 70y^3 + 27y^2 - 7y + 1$
$c_4, c_5, c_8$ $c_9, c_{10}, c_{12}$	$y^8 - 10y^7 + 39y^6 - 75y^5 + 75y^4 - 42y^3 + 22y^2 - 12y + 1$
$c_6$	$(y^4 + y^3 + y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.220530 + 0.143929I$		
$a = -0.57045 + 1.41533I$	$4.50609 - 2.52742I$	$14.9376 + 0.3938I$
$b = 0.468985 - 0.351339I$		
$u = -1.220530 - 0.143929I$		
$a = -0.57045 - 1.41533I$	$4.50609 + 2.52742I$	$14.9376 - 0.3938I$
$b = 0.468985 + 0.351339I$		
$u = 0.475131 + 0.605600I$		
$a = 0.0796516 + 0.0837240I$	$4.50609 - 2.52742I$	$14.9376 + 0.3938I$
$b = -1.141000 + 0.575478I$		
$u = 0.475131 - 0.605600I$		
$a = 0.0796516 - 0.0837240I$	$4.50609 + 2.52742I$	$14.9376 - 0.3938I$
$b = -1.141000 - 0.575478I$		
$u = 1.26429$		
$a = 1.67924$	13.5577	8.81150
$b = 0.598434$		
$u = 1.63636$		
$a = -1.79185$	10.3288	34.3130
$b = 1.67768$		
$u = 0.313425$		
$a = 6.69143$	10.3288	34.3130
$b = -0.901765$		
$u = -1.72328$		
$a = -1.59721$	13.5577	8.81150
$b = 1.96968$		

$$\mathbf{V} \cdot I_5^u = \langle b+1, a, u-1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 18

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_7, c_{11}$	$u - 1$
$c_4, c_5, c_8$ $c_9, c_{10}, c_{12}$	$u + 1$
$c_6$	$u$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$	
$c_4, c_5, c_7$	$y - 1$
$c_8, c_9, c_{10}$	
$c_{11}, c_{12}$	
$c_6$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$	4.93480	18.0000
$b = -1.00000$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)(u^4 + 3u^3 + 4u^2 + 4u + 1)^2(u^5 - 2u^4 + 5u^3 - 4u^2 - 1) \\ \cdot (u^{13} - 12u^{12} + \dots + 352u - 32)(u^{24} + 2u^{23} + \dots - 20u - 1)^2$
$c_2, c_7$	$(u - 1)(u^5 + u^4 - u^3 - u^2 + 1) \\ \cdot (u^8 + 2u^7 - 3u^6 - 5u^5 + 5u^4 + 6u^3 - u^2 - 3u - 1) \\ \cdot (u^{13} - 3u^{11} + 9u^9 + u^8 - 12u^7 + u^6 + 16u^5 - u^4 - 11u^3 + 3u^2 + 4u - 1) \\ \cdot (u^{48} - u^{47} + \dots - 197u + 73)$
$c_3, c_{11}$	$(u - 1)(u^5 - u^4 - u^3 + u^2 - 1) \\ \cdot (u^8 - 2u^7 - 3u^6 + 5u^5 + 5u^4 - 6u^3 - u^2 + 3u - 1) \\ \cdot (u^{13} - 3u^{11} + 9u^9 + u^8 - 12u^7 + u^6 + 16u^5 - u^4 - 11u^3 + 3u^2 + 4u - 1) \\ \cdot (u^{48} - u^{47} + \dots - 197u + 73)$
$c_4, c_5, c_8$ $c_9$	$(u + 1)(u^5 - 3u^3 + 2u + 1)(u^8 - 5u^6 + \dots + 4u - 1) \\ \cdot (u^{13} - u^{12} + \dots + 2u - 1)(u^{48} - u^{47} + \dots - 20u + 1)$
$c_6$	$u(u^4 - u^3 + u^2 + u - 1)^2(u^5 + 2u^4 + 3u^3 + 3u^2 + 3u + 1) \\ \cdot (u^{13} + 11u^{12} + \dots - 208u - 56)(u^{24} - 5u^{23} + \dots + 15u - 1)^2$
$c_{10}, c_{12}$	$(u + 1)(u^5 - 3u^3 + 2u - 1)(u^8 - 5u^6 + \dots - 4u - 1) \\ \cdot (u^{13} - u^{12} + \dots + 2u - 1)(u^{48} - u^{47} + \dots - 20u + 1)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)(y^4 - y^3 - 6y^2 - 8y + 1)^2(y^5 + 6y^4 + 9y^3 - 20y^2 - 8y - 1) \\ \cdot (y^{13} + 8y^{12} + \dots + 42496y - 1024)(y^{24} + 4y^{23} + \dots - 522y + 1)^2$
$c_2, c_3, c_7$ $c_{11}$	$(y - 1)(y^5 - 3y^4 + 3y^3 - 3y^2 + 2y - 1) \\ \cdot (y^8 - 10y^7 + 39y^6 - 81y^5 + 101y^4 - 70y^3 + 27y^2 - 7y + 1) \\ \cdot (y^{13} - 6y^{12} + \dots + 22y - 1)(y^{48} - 23y^{47} + \dots - 76039y + 5329)$
$c_4, c_5, c_8$ $c_9, c_{10}, c_{12}$	$(y - 1)(y^5 - 6y^4 + 13y^3 - 12y^2 + 4y - 1) \\ \cdot (y^8 - 10y^7 + 39y^6 - 75y^5 + 75y^4 - 42y^3 + 22y^2 - 12y + 1) \\ \cdot (y^{13} - 13y^{12} + \dots - 8y - 1)(y^{48} - 43y^{47} + \dots - 216y + 1)$
$c_6$	$y(y^4 + y^3 + y^2 - 3y + 1)^2(y^5 + 2y^4 + 3y^3 + 5y^2 + 3y - 1) \\ \cdot (y^{13} + y^{12} + \dots + 5408y - 3136)(y^{24} - 3y^{23} + \dots - 135y + 1)^2$