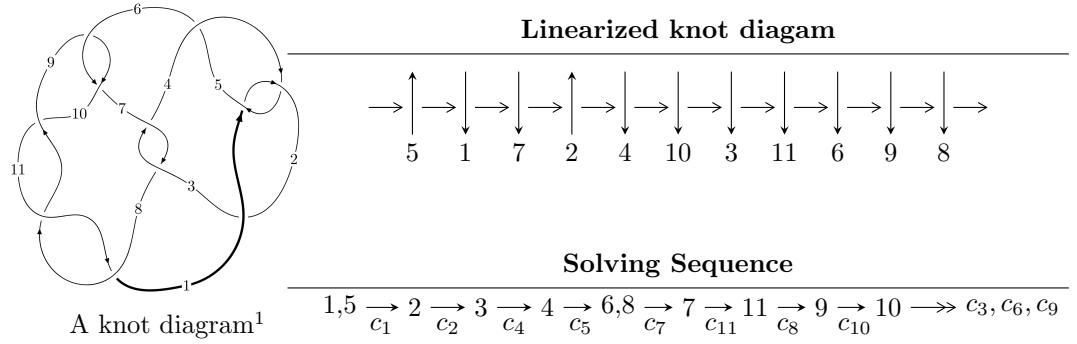


## $11a_{50}$ ( $K11a_{50}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned} I_1^u &= \langle -2u^{46} + 9u^{45} + \cdots + 4b + 5, -u^{46} + 18u^{45} + \cdots + 4a - 25, u^{47} - 4u^{46} + \cdots + 6u - 1 \rangle \\ I_2^u &= \langle -au + b, a^3 - a^2u - a^2 + 2au + 1, u^2 + u + 1 \rangle \end{aligned}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 53 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -2u^{46} + 9u^{45} + \dots + 4b + 5, -u^{46} + 18u^{45} + \dots + 4a - 25, u^{47} - 4u^{46} + \dots + 6u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} \frac{1}{4}u^{46} - \frac{9}{2}u^{45} + \dots - 17u + \frac{25}{4} \\ \frac{1}{2}u^{46} - \frac{9}{4}u^{45} + \dots + \frac{9}{4}u - \frac{5}{4} \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{7}{4}u^{46} - \frac{5}{2}u^{45} + \dots + 2u + \frac{7}{4} \\ -\frac{9}{2}u^{46} + \frac{41}{4}u^{45} + \dots + \frac{35}{4}u - \frac{7}{4} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -\frac{1}{4}u^{46} + \frac{3}{4}u^{45} + \dots + \frac{13}{4}u + 2 \\ \frac{1}{4}u^{46} - u^{45} + \dots - \frac{5}{2}u + \frac{1}{4} \end{pmatrix} \\ a_9 &= \begin{pmatrix} -2u^{46} + \frac{15}{2}u^{45} + \dots + 20u + 1 \\ -\frac{5}{4}u^{46} + \frac{13}{4}u^{45} + \dots - \frac{11}{4}u + \frac{1}{2} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -\frac{7}{4}u^{46} + \frac{33}{4}u^{45} + \dots + \frac{107}{4}u - \frac{1}{2} \\ -\frac{5}{4}u^{46} + \frac{9}{4}u^{45} + \dots - \frac{31}{4}u + \frac{3}{2} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -\frac{7}{4}u^{46} + \frac{33}{4}u^{45} + \dots + \frac{107}{4}u - \frac{1}{2} \\ -\frac{5}{4}u^{46} + \frac{9}{4}u^{45} + \dots - \frac{31}{4}u + \frac{3}{2} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-9u^{46} + \frac{33}{2}u^{45} + \dots - 27u - 4$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{47} + 4u^{46} + \cdots + 6u + 1$
$c_2, c_5$	$u^{47} + 14u^{46} + \cdots + 38u - 1$
$c_3, c_7$	$u^{47} - u^{46} + \cdots + 96u + 64$
$c_6, c_9$	$u^{47} + 3u^{46} + \cdots - u + 1$
$c_8, c_{10}, c_{11}$	$u^{47} + 11u^{46} + \cdots + u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{47} + 14y^{46} + \cdots + 38y - 1$
$c_2, c_5$	$y^{47} + 42y^{46} + \cdots + 2346y - 1$
$c_3, c_7$	$y^{47} + 35y^{46} + \cdots - 23552y - 4096$
$c_6, c_9$	$y^{47} - 11y^{46} + \cdots + y - 1$
$c_8, c_{10}, c_{11}$	$y^{47} + 53y^{46} + \cdots + 41y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.663428 + 0.780790I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-4.48198 - 0.15159I}$
$a = 1.00646 - 1.05901I$	$1.047100 - 0.807076I$	$-4.48198 - 0.15159I$
$b = -0.205400 + 0.577345I$		
$u = -0.663428 - 0.780790I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-4.48198 + 0.15159I}$
$a = 1.00646 + 1.05901I$	$1.047100 + 0.807076I$	$-4.48198 + 0.15159I$
$b = -0.205400 - 0.577345I$		
$u = -0.199822 + 1.009780I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-10.22284 + 8.38293I}$
$a = -0.834043 - 0.291155I$	$-2.01497 - 4.25844I$	$-10.22284 + 8.38293I$
$b = -0.625995 - 0.626906I$		
$u = -0.199822 - 1.009780I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-10.22284 - 8.38293I}$
$a = -0.834043 + 0.291155I$	$-2.01497 + 4.25844I$	$-10.22284 - 8.38293I$
$b = -0.625995 + 0.626906I$		
$u = -0.461388 + 0.956277I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-2.14725 - 2.29266I}$
$a = 0.665200 + 0.526100I$	$-0.63663 - 1.64887I$	$-2.14725 - 2.29266I$
$b = -0.316069 + 0.253513I$		
$u = -0.461388 - 0.956277I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-2.14725 + 2.29266I}$
$a = 0.665200 - 0.526100I$	$-0.63663 + 1.64887I$	$-2.14725 + 2.29266I$
$b = -0.316069 - 0.253513I$		
$u = 0.810606 + 0.776375I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-3.05328 + 3.33895I}$
$a = 0.565835 + 0.632629I$	$4.58669 - 3.21526I$	$-3.05328 + 3.33895I$
$b = -0.750225 - 1.009350I$		
$u = 0.810606 - 0.776375I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-3.05328 - 3.33895I}$
$a = 0.565835 - 0.632629I$	$4.58669 + 3.21526I$	$-3.05328 - 3.33895I$
$b = -0.750225 + 1.009350I$		
$u = -0.656947 + 0.912090I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-6.53825 + 6.48689I}$
$a = -0.22666 + 1.51107I$	$0.63898 - 4.31334I$	$-6.53825 + 6.48689I$
$b = -0.392245 - 0.675540I$		
$u = -0.656947 - 0.912090I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$C_{-6.53825 - 6.48689I}$
$a = -0.22666 - 1.51107I$	$0.63898 + 4.31334I$	$-6.53825 - 6.48689I$
$b = -0.392245 + 0.675540I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.867038 + 0.019562I$		
$a = 0.12989 + 1.85582I$	$9.34836 - 3.22875I$	$0.48816 + 2.52460I$
$b = -0.08456 - 1.60423I$		
$u = -0.867038 - 0.019562I$		
$a = 0.12989 - 1.85582I$	$9.34836 + 3.22875I$	$0.48816 - 2.52460I$
$b = -0.08456 + 1.60423I$		
$u = -0.311898 + 0.787865I$		
$a = 0.956078 + 0.122134I$	$-0.33163 - 1.48922I$	$-3.21291 + 4.41196I$
$b = 0.1036160 + 0.0693880I$		
$u = -0.311898 - 0.787865I$		
$a = 0.956078 - 0.122134I$	$-0.33163 + 1.48922I$	$-3.21291 - 4.41196I$
$b = 0.1036160 - 0.0693880I$		
$u = 0.749711 + 0.881463I$		
$a = 0.133762 - 0.692661I$	$1.38780 + 2.84463I$	$-7.00000 - 2.87095I$
$b = -1.094820 - 0.057901I$		
$u = 0.749711 - 0.881463I$		
$a = 0.133762 + 0.692661I$	$1.38780 - 2.84463I$	$-7.00000 + 2.87095I$
$b = -1.094820 + 0.057901I$		
$u = -0.026264 + 0.834708I$		
$a = -1.139080 - 0.577019I$	$-2.87835 + 0.31776I$	$-14.00580 - 0.89851I$
$b = -0.739974 + 0.342805I$		
$u = -0.026264 - 0.834708I$		
$a = -1.139080 + 0.577019I$	$-2.87835 - 0.31776I$	$-14.00580 + 0.89851I$
$b = -0.739974 - 0.342805I$		
$u = 0.830386 + 0.839820I$		
$a = 0.137676 - 0.366174I$	$6.59048 + 1.40114I$	$0. - 2.24691I$
$b = 0.439191 + 0.593639I$		
$u = 0.830386 - 0.839820I$		
$a = 0.137676 + 0.366174I$	$6.59048 - 1.40114I$	$0. + 2.24691I$
$b = 0.439191 - 0.593639I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.927893 + 0.738669I$		
$a = 0.28332 + 1.95602I$	$13.7092 - 7.1190I$	$0. + 3.20529I$
$b = -0.22878 - 1.70233I$		
$u = 0.927893 - 0.738669I$		
$a = 0.28332 - 1.95602I$	$13.7092 + 7.1190I$	$0. - 3.20529I$
$b = -0.22878 + 1.70233I$		
$u = -0.294048 + 1.158780I$		
$a = -1.041500 - 0.000140I$	$5.33133 - 7.16658I$	$-4.32444 + 6.19083I$
$b = -0.17743 - 1.57625I$		
$u = -0.294048 - 1.158780I$		
$a = -1.041500 + 0.000140I$	$5.33133 + 7.16658I$	$-4.32444 - 6.19083I$
$b = -0.17743 + 1.57625I$		
$u = -0.322894 + 1.152850I$		
$a = 1.126820 + 0.062685I$	$5.51392 - 0.84918I$	$-3.71085 + 0.I$
$b = -0.03457 + 1.51727I$		
$u = -0.322894 - 1.152850I$		
$a = 1.126820 - 0.062685I$	$5.51392 + 0.84918I$	$-3.71085 + 0.I$
$b = -0.03457 - 1.51727I$		
$u = -0.810352 + 0.881677I$		
$a = 1.20304 - 2.40238I$	$8.49103 + 0.19218I$	$-2.01859 + 0.I$
$b = -0.06174 + 1.58029I$		
$u = -0.810352 - 0.881677I$		
$a = 1.20304 + 2.40238I$	$8.49103 - 0.19218I$	$-2.01859 + 0.I$
$b = -0.06174 - 1.58029I$		
$u = 0.928006 + 0.759035I$		
$a = -0.06191 - 1.86044I$	$14.10940 - 0.53726I$	$0. - 1.50138I$
$b = 0.10905 + 1.59219I$		
$u = 0.928006 - 0.759035I$		
$a = -0.06191 + 1.86044I$	$14.10940 + 0.53726I$	$0. + 1.50138I$
$b = 0.10905 - 1.59219I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.803055 + 0.903733I$		
$a = -0.99990 + 2.49478I$	$8.42204 - 6.23223I$	$0. + 5.02146I$
$b = -0.11755 - 1.60103I$		
$u = -0.803055 - 0.903733I$		
$a = -0.99990 - 2.49478I$	$8.42204 + 6.23223I$	$0. - 5.02146I$
$b = -0.11755 + 1.60103I$		
$u = 0.797400 + 0.942409I$		
$a = 0.817901 + 0.783072I$	$6.27252 + 4.67969I$	$0$
$b = 0.484733 - 0.494859I$		
$u = 0.797400 - 0.942409I$		
$a = 0.817901 - 0.783072I$	$6.27252 - 4.67969I$	$0$
$b = 0.484733 + 0.494859I$		
$u = 0.760355 + 0.975109I$		
$a = -0.78027 - 1.38920I$	$3.97968 + 9.12021I$	$-7.00000 - 8.49829I$
$b = -0.832040 + 0.941509I$		
$u = 0.760355 - 0.975109I$		
$a = -0.78027 + 1.38920I$	$3.97968 - 9.12021I$	$-7.00000 + 8.49829I$
$b = -0.832040 - 0.941509I$		
$u = 0.236667 + 0.699953I$		
$a = -2.00141 - 0.89361I$	$2.56997 + 3.95764I$	$-7.31001 - 0.68586I$
$b = -0.27531 + 1.39228I$		
$u = 0.236667 - 0.699953I$		
$a = -2.00141 + 0.89361I$	$2.56997 - 3.95764I$	$-7.31001 + 0.68586I$
$b = -0.27531 - 1.39228I$		
$u = 0.807992 + 1.034530I$		
$a = 1.69856 + 1.55368I$	$13.2416 + 6.9328I$	$0$
$b = 0.14248 - 1.55761I$		
$u = 0.807992 - 1.034530I$		
$a = 1.69856 - 1.55368I$	$13.2416 - 6.9328I$	$0$
$b = 0.14248 + 1.55761I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.796590 + 1.043640I$		
$a = -1.65368 - 1.73183I$	$12.7501 + 13.4737I$	0
$b = -0.26885 + 1.69481I$		
$u = 0.796590 - 1.043640I$		
$a = -1.65368 + 1.73183I$	$12.7501 - 13.4737I$	0
$b = -0.26885 - 1.69481I$		
$u = 0.262896 + 0.609439I$		
$a = 2.19053 + 0.65507I$	$2.83383 - 1.80935I$	$-5.60137 + 4.89150I$
$b = -0.102273 - 1.283390I$		
$u = 0.262896 - 0.609439I$		
$a = 2.19053 - 0.65507I$	$2.83383 + 1.80935I$	$-5.60137 - 4.89150I$
$b = -0.102273 + 1.283390I$		
$u = -0.563257 + 0.159760I$		
$a = 0.608331 + 0.292239I$	$1.45889 - 1.89863I$	$-0.82802 + 4.86862I$
$b = -0.248810 - 0.689997I$		
$u = -0.563257 - 0.159760I$		
$a = 0.608331 - 0.292239I$	$1.45889 + 1.89863I$	$-0.82802 - 4.86862I$
$b = -0.248810 + 0.689997I$		
$u = 0.143780$		
$a = 3.43014$	$-0.906933$	$-11.3950$
$b = -0.444877$		

$$\text{II. } I_2^u = \langle -au + b, a^3 - a^2u - a^2 + 2au + 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u+1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ u+1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a \\ au \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ au \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -a^2u + 1 \\ a^2u + a^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -a^2u - au - a + u + 1 \\ a^2u + a^2 - au - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2a^2u - a^2 - a + u + 2 \\ a^2u + a^2 - au - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2a^2u - a^2 - a + u + 2 \\ a^2u + a^2 - au - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $5a^2u + 6a^2 - 5au - a + 7u - 10$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$(u^2 + u + 1)^3$
$c_3, c_7$	$u^6$
$c_4$	$(u^2 - u + 1)^3$
$c_6$	$(u^3 + u^2 - 1)^2$
$c_8$	$(u^3 - u^2 + 2u - 1)^2$
$c_9$	$(u^3 - u^2 + 1)^2$
$c_{10}, c_{11}$	$(u^3 + u^2 + 2u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5$	$(y^2 + y + 1)^3$
$c_3, c_7$	$y^6$
$c_6, c_9$	$(y^3 - y^2 + 2y - 1)^2$
$c_8, c_{10}, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 1.239560 - 0.467306I$	$3.02413 - 4.85801I$	$-2.74410 + 7.22587I$
$b = -0.215080 + 1.307140I$		
$u = -0.500000 + 0.866025I$		
$a = -1.024480 + 0.839835I$	$3.02413 + 0.79824I$	$-4.03424 + 1.64667I$
$b = -0.215080 - 1.307140I$		
$u = -0.500000 + 0.866025I$		
$a = 0.284920 + 0.493496I$	$-1.11345 - 2.02988I$	$-12.72167 + 5.84990I$
$b = -0.569840$		
$u = -0.500000 - 0.866025I$		
$a = 1.239560 + 0.467306I$	$3.02413 + 4.85801I$	$-2.74410 - 7.22587I$
$b = -0.215080 - 1.307140I$		
$u = -0.500000 - 0.866025I$		
$a = -1.024480 - 0.839835I$	$3.02413 - 0.79824I$	$-4.03424 - 1.64667I$
$b = -0.215080 + 1.307140I$		
$u = -0.500000 - 0.866025I$		
$a = 0.284920 - 0.493496I$	$-1.11345 + 2.02988I$	$-12.72167 - 5.84990I$
$b = -0.569840$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 + u + 1)^3)(u^{47} + 4u^{46} + \dots + 6u + 1)$
$c_2, c_5$	$((u^2 + u + 1)^3)(u^{47} + 14u^{46} + \dots + 38u - 1)$
$c_3, c_7$	$u^6(u^{47} - u^{46} + \dots + 96u + 64)$
$c_4$	$((u^2 - u + 1)^3)(u^{47} + 4u^{46} + \dots + 6u + 1)$
$c_6$	$((u^3 + u^2 - 1)^2)(u^{47} + 3u^{46} + \dots - u + 1)$
$c_8$	$((u^3 - u^2 + 2u - 1)^2)(u^{47} + 11u^{46} + \dots + u + 1)$
$c_9$	$((u^3 - u^2 + 1)^2)(u^{47} + 3u^{46} + \dots - u + 1)$
$c_{10}, c_{11}$	$((u^3 + u^2 + 2u + 1)^2)(u^{47} + 11u^{46} + \dots + u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y^2 + y + 1)^3)(y^{47} + 14y^{46} + \dots + 38y - 1)$
$c_2, c_5$	$((y^2 + y + 1)^3)(y^{47} + 42y^{46} + \dots + 2346y - 1)$
$c_3, c_7$	$y^6(y^{47} + 35y^{46} + \dots - 23552y - 4096)$
$c_6, c_9$	$((y^3 - y^2 + 2y - 1)^2)(y^{47} - 11y^{46} + \dots + y - 1)$
$c_8, c_{10}, c_{11}$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{47} + 53y^{46} + \dots + 41y - 1)$