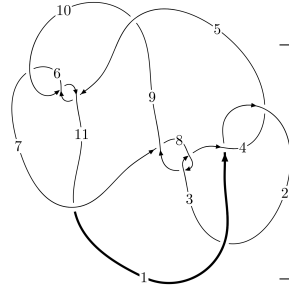
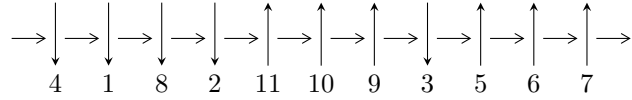


11a<sub>56</sub> (K11a<sub>56</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,11 \xrightarrow{c_5} 6 \xrightarrow{c_{10}} 10 \xrightarrow{c_6} 7 \xrightarrow{c_{11}} 1,3 \xrightarrow{c_2} 2 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \longrightarrow c_1, c_3, c_7$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{54} - u^{53} + \dots + b + 1, -u^{56} + 2u^{55} + \dots + a - 4, u^{57} - 2u^{56} + \dots + 3u - 1 \rangle$$

$$I_2^u = \langle b + 1, -u^2 + a - u - 2, u^3 + u^2 + 2u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 60 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{54} - u^{53} + \dots + b + 1, -u^{56} + 2u^{55} + \dots + a - 4, u^{57} - 2u^{56} + \dots + 3u - 1 \rangle$$

I.

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{56} - 2u^{55} + \dots + 2u + 4 \\ -u^{54} + u^{53} + \dots - u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{56} - 2u^{55} + \dots + 3u + 3 \\ -u^{54} + u^{53} + \dots - u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{56} - 2u^{55} + \dots + 4u + 3 \\ -u^{54} + u^{53} + \dots + 2u^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{10} - 5u^8 - 8u^6 - 3u^4 + 3u^2 + 1 \\ u^{10} + 4u^8 + 5u^6 - 3u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{10} - 5u^8 - 8u^6 - 3u^4 + 3u^2 + 1 \\ u^{10} + 4u^8 + 5u^6 - 3u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-u^{56} + 2u^{55} + \dots - 8u - 9$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{57} - 4u^{56} + \dots - 4u + 1$
$c_2$	$u^{57} + 30u^{56} + \dots + 4u + 1$
$c_3, c_8$	$u^{57} - u^{56} + \dots + 4u + 8$
$c_5, c_6, c_{10}$	$u^{57} + 2u^{56} + \dots + 3u + 1$
$c_7$	$u^{57} - 21u^{56} + \dots - 496u + 64$
$c_9, c_{11}$	$u^{57} - 2u^{56} + \dots - 3u + 9$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{57} - 30y^{56} + \dots + 4y - 1$
$c_2$	$y^{57} - 2y^{56} + \dots - 24y - 1$
$c_3, c_8$	$y^{57} + 21y^{56} + \dots - 496y - 64$
$c_5, c_6, c_{10}$	$y^{57} + 48y^{56} + \dots + 23y - 1$
$c_7$	$y^{57} + 25y^{56} + \dots + 134400y - 4096$
$c_9, c_{11}$	$y^{57} - 32y^{56} + \dots + 1719y - 81$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.339361 + 1.049480I$ $a = 0.50854 - 1.48654I$ $b = -1.48903 + 0.96739I$	$-1.26618 - 6.23330I$	0
$u = 0.339361 - 1.049480I$ $a = 0.50854 + 1.48654I$ $b = -1.48903 - 0.96739I$	$-1.26618 + 6.23330I$	0
$u = -0.245002 + 1.131380I$ $a = -0.32304 - 1.42186I$ $b = 0.208942 + 0.592370I$	$-3.18295 + 0.59460I$	0
$u = -0.245002 - 1.131380I$ $a = -0.32304 + 1.42186I$ $b = 0.208942 - 0.592370I$	$-3.18295 - 0.59460I$	0
$u = 0.317804 + 1.113660I$ $a = -0.301756 + 1.180030I$ $b = 1.38215 - 0.87035I$	$1.12994 - 1.12326I$	0
$u = 0.317804 - 1.113660I$ $a = -0.301756 - 1.180030I$ $b = 1.38215 + 0.87035I$	$1.12994 + 1.12326I$	0
$u = 0.799224 + 0.161136I$ $a = 3.09156 + 0.85984I$ $b = -1.72076 - 1.24432I$	$1.44780 + 10.42440I$	$2.90383 - 7.96893I$
$u = 0.799224 - 0.161136I$ $a = 3.09156 - 0.85984I$ $b = -1.72076 + 1.24432I$	$1.44780 - 10.42440I$	$2.90383 + 7.96893I$
$u = 0.806026 + 0.024229I$ $a = -0.524270 - 0.510392I$ $b = 0.297226 + 0.891673I$	$7.00743 + 2.64990I$	$8.23772 - 3.33458I$
$u = 0.806026 - 0.024229I$ $a = -0.524270 + 0.510392I$ $b = 0.297226 - 0.891673I$	$7.00743 - 2.64990I$	$8.23772 + 3.33458I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.787966 + 0.130536I$ $a = -2.57577 - 0.95104I$ $b = 1.42239 + 1.23954I$	$4.10218 + 5.18574I$	$6.42318 - 4.39381I$
$u = 0.787966 - 0.130536I$ $a = -2.57577 + 0.95104I$ $b = 1.42239 - 1.23954I$	$4.10218 - 5.18574I$	$6.42318 + 4.39381I$
$u = 0.226143 + 1.198470I$ $a = -0.29741 - 1.54674I$ $b = -1.71216 + 1.04442I$	$-3.91254 + 1.67555I$	0
$u = 0.226143 - 1.198470I$ $a = -0.29741 + 1.54674I$ $b = -1.71216 - 1.04442I$	$-3.91254 - 1.67555I$	0
$u = -0.754570 + 0.135098I$ $a = -1.92141 + 1.62306I$ $b = 0.580662 - 0.892200I$	$-0.25463 - 4.33211I$	$1.62345 + 4.63416I$
$u = -0.754570 - 0.135098I$ $a = -1.92141 - 1.62306I$ $b = 0.580662 + 0.892200I$	$-0.25463 + 4.33211I$	$1.62345 - 4.63416I$
$u = -0.338013 + 0.681571I$ $a = 0.642106 - 0.604854I$ $b = -0.849512 + 0.966860I$	$-2.04198 - 6.13465I$	$-0.96110 + 7.52026I$
$u = -0.338013 - 0.681571I$ $a = 0.642106 + 0.604854I$ $b = -0.849512 - 0.966860I$	$-2.04198 + 6.13465I$	$-0.96110 - 7.52026I$
$u = 0.722838 + 0.126778I$ $a = 2.54617 + 1.95088I$ $b = -1.31528 - 1.75485I$	$-0.80005 + 1.75324I$	$2.03009 - 4.15615I$
$u = 0.722838 - 0.126778I$ $a = 2.54617 - 1.95088I$ $b = -1.31528 + 1.75485I$	$-0.80005 - 1.75324I$	$2.03009 + 4.15615I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.275696 + 1.237520I$ $a = 0.808387 + 0.975749I$ $b = -0.556151 - 0.097923I$	$-1.78635 - 3.24178I$	0
$u = -0.275696 - 1.237520I$ $a = 0.808387 - 0.975749I$ $b = -0.556151 + 0.097923I$	$-1.78635 + 3.24178I$	0
$u = 0.353003 + 1.235470I$ $a = 0.259194 + 0.074469I$ $b = 0.608563 - 0.823394I$	$3.27082 + 1.52614I$	0
$u = 0.353003 - 1.235470I$ $a = 0.259194 - 0.074469I$ $b = 0.608563 + 0.823394I$	$3.27082 - 1.52614I$	0
$u = -0.664926 + 0.248231I$ $a = -0.53582 + 1.91639I$ $b = -0.321007 - 0.845457I$	$-0.56153 + 2.51315I$	$1.83697 - 2.48665I$
$u = -0.664926 - 0.248231I$ $a = -0.53582 - 1.91639I$ $b = -0.321007 + 0.845457I$	$-0.56153 - 2.51315I$	$1.83697 + 2.48665I$
$u = -0.704230 + 0.061019I$ $a = 1.64700 - 0.65736I$ $b = -0.525612 + 0.326561I$	$1.82968 - 0.29846I$	$5.16983 - 0.57329I$
$u = -0.704230 - 0.061019I$ $a = 1.64700 + 0.65736I$ $b = -0.525612 - 0.326561I$	$1.82968 + 0.29846I$	$5.16983 + 0.57329I$
$u = 0.355735 + 1.276270I$ $a = -0.681670 + 0.406147I$ $b = -0.007104 + 0.903876I$	$2.96572 + 6.83199I$	0
$u = 0.355735 - 1.276270I$ $a = -0.681670 - 0.406147I$ $b = -0.007104 - 0.903876I$	$2.96572 - 6.83199I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.294328 + 1.319490I$ $a = 1.338980 + 0.220264I$ $b = -0.580535 + 0.617472I$	$-2.52174 - 3.91370I$	0
$u = -0.294328 - 1.319490I$ $a = 1.338980 - 0.220264I$ $b = -0.580535 - 0.617472I$	$-2.52174 + 3.91370I$	0
$u = -0.181659 + 1.350590I$ $a = 0.400207 - 0.673731I$ $b = 0.475022 + 0.135856I$	$-3.91953 - 3.45367I$	0
$u = -0.181659 - 1.350590I$ $a = 0.400207 + 0.673731I$ $b = 0.475022 - 0.135856I$	$-3.91953 + 3.45367I$	0
$u = 0.308057 + 1.342450I$ $a = 2.07004 - 0.68307I$ $b = -1.21623 - 2.16373I$	$-5.43045 + 5.50488I$	0
$u = 0.308057 - 1.342450I$ $a = 2.07004 + 0.68307I$ $b = -1.21623 + 2.16373I$	$-5.43045 - 5.50488I$	0
$u = -0.040540 + 1.380290I$ $a = 0.437295 - 0.786403I$ $b = 0.388863 - 1.268110I$	$-5.57754 - 2.56020I$	0
$u = -0.040540 - 1.380290I$ $a = 0.437295 + 0.786403I$ $b = 0.388863 + 1.268110I$	$-5.57754 + 2.56020I$	0
$u = -0.321142 + 1.347280I$ $a = -1.81984 - 0.00606I$ $b = 0.797242 - 1.062560I$	$-4.92507 - 8.23091I$	0
$u = -0.321142 - 1.347280I$ $a = -1.81984 + 0.00606I$ $b = 0.797242 + 1.062560I$	$-4.92507 + 8.23091I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.010128 + 1.388520I$ $a = -0.665649 + 0.739671I$ $b = 0.02872 + 1.83602I$	$-9.28405 + 1.35733I$	0
$u = 0.010128 - 1.388520I$ $a = -0.665649 - 0.739671I$ $b = 0.02872 - 1.83602I$	$-9.28405 - 1.35733I$	0
$u = 0.337618 + 1.347450I$ $a = -1.76632 + 1.05829I$ $b = 1.40418 + 1.48266I$	$-0.55115 + 9.25140I$	0
$u = 0.337618 - 1.347450I$ $a = -1.76632 - 1.05829I$ $b = 1.40418 - 1.48266I$	$-0.55115 - 9.25140I$	0
$u = 0.086152 + 0.593036I$ $a = -0.86026 - 1.12969I$ $b = -0.349711 + 1.132030I$	$-3.25990 + 1.13842I$	$-4.67839 - 1.12304I$
$u = 0.086152 - 0.593036I$ $a = -0.86026 + 1.12969I$ $b = -0.349711 - 1.132030I$	$-3.25990 - 1.13842I$	$-4.67839 + 1.12304I$
$u = -0.268783 + 1.376140I$ $a = -1.251340 + 0.579944I$ $b = -0.053457 - 1.081820I$	$-5.67983 - 0.88312I$	0
$u = -0.268783 - 1.376140I$ $a = -1.251340 - 0.579944I$ $b = -0.053457 + 1.081820I$	$-5.67983 + 0.88312I$	0
$u = 0.340495 + 1.364500I$ $a = 1.93564 - 1.27843I$ $b = -1.80297 - 1.45511I$	$-3.3664 + 14.5406I$	0
$u = 0.340495 - 1.364500I$ $a = 1.93564 + 1.27843I$ $b = -1.80297 + 1.45511I$	$-3.3664 - 14.5406I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.279491 + 0.522898I$		
$a = -0.1114230 + 0.0411162I$	$0.29336 - 1.71892I$	$2.35747 + 4.28522I$
$b = 0.664100 - 0.647028I$		
$u = -0.279491 - 0.522898I$		
$a = -0.1114230 - 0.0411162I$	$0.29336 + 1.71892I$	$2.35747 - 4.28522I$
$b = 0.664100 + 0.647028I$		
$u = -0.04491 + 1.42071I$		
$a = -0.362172 + 0.648626I$	$-8.60971 - 7.06322I$	0
$b = -0.88717 + 1.55692I$		
$u = -0.04491 - 1.42071I$		
$a = -0.362172 - 0.648626I$	$-8.60971 + 7.06322I$	0
$b = -0.88717 - 1.55692I$		
$u = -0.475182 + 0.281427I$		
$a = 0.033922 - 1.111620I$	$1.12264 - 1.10520I$	$5.95384 + 5.07623I$
$b = 0.503597 + 0.110254I$		
$u = -0.475182 - 0.281427I$		
$a = 0.033922 + 1.111620I$	$1.12264 + 1.10520I$	$5.95384 - 5.07623I$
$b = 0.503597 - 0.110254I$		
$u = 0.195845$		
$a = 3.55820$	$-1.30246$	$-9.05740$
$b = -0.749956$		

$$\text{II. } I_2^u = \langle b + 1, -u^2 + a - u - 2, u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + u + 2 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + u + 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + u + 2 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $5u^2 + 4u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^3$
$c_2, c_4$	$(u + 1)^3$
$c_3, c_7, c_8$	$u^3$
$c_5, c_6$	$u^3 + u^2 + 2u + 1$
$c_9, c_{11}$	$u^3 + u^2 - 1$
$c_{10}$	$u^3 - u^2 + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^3$
$c_3, c_7, c_8$	$y^3$
$c_5, c_6, c_{10}$	$y^3 + 3y^2 + 2y - 1$
$c_9, c_{11}$	$y^3 - y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215080 + 1.307140I$ $a = 0.122561 + 0.744862I$ $b = -1.00000$	$-4.66906 - 2.82812I$	$-5.17211 + 2.41717I$
$u = -0.215080 - 1.307140I$ $a = 0.122561 - 0.744862I$ $b = -1.00000$	$-4.66906 + 2.82812I$	$-5.17211 - 2.41717I$
$u = -0.569840$ $a = 1.75488$ $b = -1.00000$	$-0.531480$	$3.34420$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^3)(u^{57} - 4u^{56} + \dots - 4u + 1)$
$c_2$	$((u + 1)^3)(u^{57} + 30u^{56} + \dots + 4u + 1)$
$c_3, c_8$	$u^3(u^{57} - u^{56} + \dots + 4u + 8)$
$c_4$	$((u + 1)^3)(u^{57} - 4u^{56} + \dots - 4u + 1)$
$c_5, c_6$	$(u^3 + u^2 + 2u + 1)(u^{57} + 2u^{56} + \dots + 3u + 1)$
$c_7$	$u^3(u^{57} - 21u^{56} + \dots - 496u + 64)$
$c_9, c_{11}$	$(u^3 + u^2 - 1)(u^{57} - 2u^{56} + \dots - 3u + 9)$
$c_{10}$	$(u^3 - u^2 + 2u - 1)(u^{57} + 2u^{56} + \dots + 3u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y - 1)^3)(y^{57} - 30y^{56} + \dots + 4y - 1)$
$c_2$	$((y - 1)^3)(y^{57} - 2y^{56} + \dots - 24y - 1)$
$c_3, c_8$	$y^3(y^{57} + 21y^{56} + \dots - 496y - 64)$
$c_5, c_6, c_{10}$	$(y^3 + 3y^2 + 2y - 1)(y^{57} + 48y^{56} + \dots + 23y - 1)$
$c_7$	$y^3(y^{57} + 25y^{56} + \dots + 134400y - 4096)$
$c_9, c_{11}$	$(y^3 - y^2 + 2y - 1)(y^{57} - 32y^{56} + \dots + 1719y - 81)$