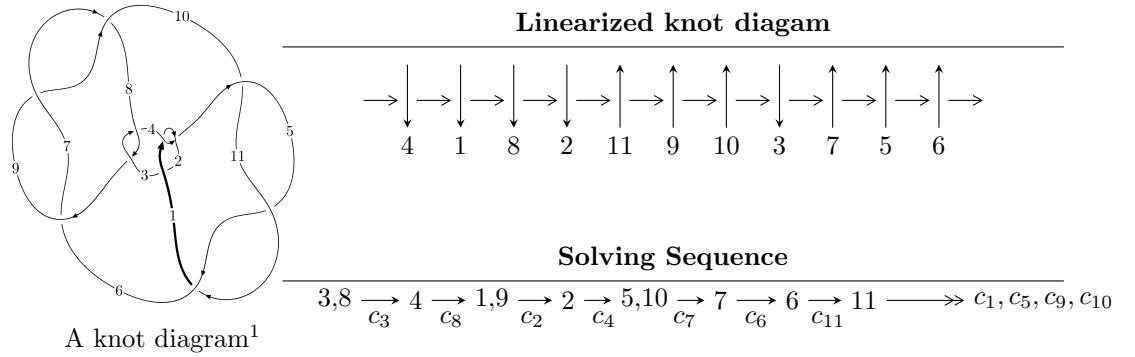


## $11a_{57}$ ( $K11a_{57}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\begin{aligned}
I_1^u &= \langle -68209745u^{16} + 103218620u^{15} + \dots + 6895752724d + 558230980, \\
&\quad - 117728333u^{16} + 37441650u^{15} + \dots + 13791505448c - 2779791176, \\
&\quad - 70376587u^{16} + 38764471u^{15} + \dots + 6895752724b + 3895994728, \\
&\quad - 327083412u^{16} + 276473252u^{15} + \dots + 6895752724a - 7902639380, u^{17} - 2u^{16} + \dots - 4u^2 + 8 \rangle \\
I_2^u &= \langle u^6c + 2u^5c + 3u^4c + 2u^3c - u^3 - cu - u^2 + d - u, \\
&\quad - u^6c - u^5c - 2u^4c - u^3c - u^2c + 2c^2 - cu - 2u^2 - 2u - 2, -u^4 - u^3 - u^2 + b + 1, \\
&\quad - u^6 - 3u^5 - 4u^4 - 3u^3 - u^2 + 2a + u, u^7 + 3u^6 + 6u^5 + 7u^4 + 5u^3 + u^2 - 2u - 2 \rangle \\
I_3^u &= \langle -u^4 + d, -u^2 + c - 1, -u^4a - 2u^2a + u^3 - au + b - a + u + 1, \\
&\quad u^3a - 2u^2a - u^3 + a^2 + 2au + u^2 - 2a - u + 1, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle \\
I_4^u &= \langle 2u^4a - 2u^4 + 4u^2a + 2u^3 + au - 6u^2 + d + 4a + 2u - 4, -u^4a + u^4 - 2u^2a - u^3 + 3u^2 + c - 2a - u + 2, \\
&\quad - u^4a - 2u^2a + u^3 - au + b - a + u + 1, u^3a - 2u^2a - u^3 + a^2 + 2au + u^2 - 2a - u + 1, \\
&\quad u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle \\
I_5^u &= \langle -u^4 + d, -u^2 + c - 1, u^4 - u^3 + u^2 + b + 1, 2u^4 - u^3 + 4u^2 + a + 2, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle
\end{aligned}$$

$$I_1^v = \langle c, d - 1, b, a - 1, v + 1 \rangle$$

$$I_2^v = \langle a, d, c - 1, b + 1, v - 1 \rangle$$

$$I_3^v = \langle a, d + 1, c - a, b + 1, v - 1 \rangle$$

$$I_4^v = \langle a, da + c - 1, dv + 1, cv - a - v, b + 1 \rangle$$

\* 8 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 59 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

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<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -6.82 \times 10^7 u^{16} + 1.03 \times 10^8 u^{15} + \dots + 6.90 \times 10^9 d + 5.58 \times 10^8, -1.18 \times 10^8 u^{16} + 3.74 \times 10^7 u^{15} + \dots + 1.38 \times 10^{10} c - 2.78 \times 10^9, -7.04 \times 10^7 u^{16} + 3.88 \times 10^7 u^{15} + \dots + 6.90 \times 10^9 b + 3.90 \times 10^9, -3.27 \times 10^8 u^{16} + 2.76 \times 10^8 u^{15} + \dots + 6.90 \times 10^9 a - 7.90 \times 10^9, u^{17} - 2u^{16} + \dots - 4u^2 + 8 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0474326u^{16} - 0.0400933u^{15} + \dots + 0.133884u + 1.14602 \\ 0.0102058u^{16} - 0.00562150u^{15} + \dots + 0.589483u - 0.564985 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0115535u^{16} - 0.0103886u^{15} + \dots - 0.835060u + 1.27282 \\ -0.0135318u^{16} + 0.0739510u^{15} + \dots + 1.06137u + 0.141156 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0576384u^{16} - 0.0457148u^{15} + \dots + 0.723367u + 0.581031 \\ -0.0339841u^{16} + 0.0141997u^{15} + \dots - 1.05059u + 0.00848878 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.00853629u^{16} - 0.00271483u^{15} + \dots - 0.843158u + 0.201558 \\ 0.00989156u^{16} - 0.0149684u^{15} + \dots + 0.971920u - 0.0809529 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0184279u^{16} + 0.0176833u^{15} + \dots - 0.128762u - 0.120605 \\ 0.00989156u^{16} - 0.0149684u^{15} + \dots + 0.971920u - 0.0809529 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0196690u^{16} + 0.00798947u^{15} + \dots - 0.197053u - 0.235467 \\ 0.0111327u^{16} - 0.00527464u^{15} + \dots + 1.04021u + 0.0339091 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0321906u^{16} - 0.0342299u^{15} + \dots - 0.170381u + 0.791078 \\ 0.00701992u^{16} + 0.00619838u^{15} + \dots + 0.764986u - 0.330652 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0321906u^{16} - 0.0342299u^{15} + \dots - 0.170381u + 0.791078 \\ 0.00701992u^{16} + 0.00619838u^{15} + \dots + 0.764986u - 0.330652 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{975451789}{3447876362}u^{16} - \frac{210120269}{3447876362}u^{15} + \dots + \frac{8037027246}{1723938181}u - \frac{2146878348}{1723938181}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{17} - 2u^{16} + \cdots - 8u + 4$
$c_2$	$u^{17} + 6u^{16} + \cdots + 88u + 16$
$c_3, c_8$	$u^{17} - 2u^{16} + \cdots - 4u^2 + 8$
$c_5, c_6, c_7$ $c_9, c_{10}, c_{11}$	$u^{17} + 2u^{16} + \cdots + 3u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{17} - 6y^{16} + \cdots + 88y - 16$
$c_2$	$y^{17} + 10y^{16} + \cdots + 288y - 256$
$c_3, c_8$	$y^{17} + 6y^{16} + \cdots + 64y - 64$
$c_5, c_6, c_7$ $c_9, c_{10}, c_{11}$	$y^{17} - 20y^{16} + \cdots + 27y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.679716 + 0.561358I$		
$a = 0.469715 + 0.071775I$		
$b = -1.066150 + 0.686891I$	$-3.14388 + 1.09865I$	$-5.52136 - 1.09882I$
$c = -0.482279 - 0.453082I$		
$d = 0.255516 + 0.765465I$		
$u = 0.679716 - 0.561358I$		
$a = 0.469715 - 0.071775I$		
$b = -1.066150 - 0.686891I$	$-3.14388 - 1.09865I$	$-5.52136 + 1.09882I$
$c = -0.482279 + 0.453082I$		
$d = 0.255516 - 0.765465I$		
$u = 0.555749 + 1.023030I$		
$a = -0.24717 + 1.86349I$		
$b = -0.866669 - 1.12847I$	$-1.71782 - 5.90288I$	$-0.75718 + 7.23695I$
$c = -0.493632 - 0.522885I$		
$d = -0.051009 + 0.779355I$		
$u = 0.555749 - 1.023030I$		
$a = -0.24717 - 1.86349I$		
$b = -0.866669 + 1.12847I$	$-1.71782 + 5.90288I$	$-0.75718 - 7.23695I$
$c = -0.493632 + 0.522885I$		
$d = -0.051009 - 0.779355I$		
$u = -1.247530 + 0.318357I$		
$a = 0.505620 + 0.282992I$		
$b = 0.454441 + 0.853023I$	$8.60033 - 1.91429I$	$8.38805 + 0.33236I$
$c = -1.114330 - 0.162230I$		
$d = -0.517027 + 0.098116I$		
$u = -1.247530 - 0.318357I$		
$a = 0.505620 - 0.282992I$		
$b = 0.454441 - 0.853023I$	$8.60033 + 1.91429I$	$8.38805 - 0.33236I$
$c = -1.114330 + 0.162230I$		
$d = -0.517027 - 0.098116I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.022849 + 0.695780I$		
$a = 1.92972 - 1.22120I$		
$b = -0.342039 + 0.295037I$	$0.88275 + 1.29794I$	$5.86581 - 6.22804I$
$c = 0.324109 - 0.810541I$		
$d = 0.054070 + 0.438524I$		
$u = -0.022849 - 0.695780I$		
$a = 1.92972 + 1.22120I$		
$b = -0.342039 - 0.295037I$	$0.88275 - 1.29794I$	$5.86581 + 6.22804I$
$c = 0.324109 + 0.810541I$		
$d = 0.054070 - 0.438524I$		
$u = 1.235140 + 0.560024I$		
$a = 0.436143 + 0.137389I$		
$b = -0.74733 + 1.42693I$	$6.85439 + 7.49245I$	$6.04980 - 5.00652I$
$c = 1.046940 - 0.255771I$		
$d = 0.525994 + 0.171484I$		
$u = 1.235140 - 0.560024I$		
$a = 0.436143 - 0.137389I$		
$b = -0.74733 - 1.42693I$	$6.85439 - 7.49245I$	$6.04980 + 5.00652I$
$c = 1.046940 + 0.255771I$		
$d = 0.525994 - 0.171484I$		
$u = -0.66454 + 1.33308I$		
$a = 0.446199 + 0.683104I$		
$b = 0.944156 - 0.676727I$	$11.9481 + 8.6770I$	$9.06927 - 4.38269I$
$c = 0.252205 + 0.988893I$		
$d = -0.30957 - 2.53920I$		
$u = -0.66454 - 1.33308I$		
$a = 0.446199 - 0.683104I$		
$b = 0.944156 + 0.676727I$	$11.9481 - 8.6770I$	$9.06927 + 4.38269I$
$c = 0.252205 - 0.988893I$		
$d = -0.30957 + 2.53920I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.79652 + 1.26851I$ $a = -0.46664 + 1.36075I$ $b = -1.06945 - 1.61168I$ $c = -0.297727 + 0.961003I$ $d = 0.35861 - 2.47585I$	$9.1924 - 14.7354I$	$6.16899 + 8.15927I$
$u = 0.79652 - 1.26851I$ $a = -0.46664 - 1.36075I$ $b = -1.06945 + 1.61168I$ $c = -0.297727 - 0.961003I$ $d = 0.35861 + 2.47585I$	$9.1924 + 14.7354I$	$6.16899 - 8.15927I$
$u = -0.11728 + 1.54547I$ $a = 0.161885 - 1.071490I$ $b = 0.08928 + 1.57333I$ $c = 0.041573 + 1.021680I$ $d = -0.05064 - 2.64219I$	$15.7365 + 3.2760I$	$10.07807 - 2.58290I$
$u = -0.11728 - 1.54547I$ $a = 0.161885 + 1.071490I$ $b = 0.08928 - 1.57333I$ $c = 0.041573 - 1.021680I$ $d = -0.05064 + 2.64219I$	$15.7365 - 3.2760I$	$10.07807 + 2.58290I$
$u = -0.429856$ $a = 0.529049$ $b = -0.792429$ $c = 0.446280$ $d = -0.531893$	-1.29941	-8.68290

$$\text{III. } I_2^u = \langle u^6c + 2u^5c + \dots + d - u, -u^6c - u^5c + \dots + 2c^2 - 2, -u^4 - u^3 - u^2 + b + 1, -u^6 - 3u^5 + \dots + 2a + u, u^7 + 3u^6 + \dots - 2u - 2 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} \frac{1}{2}u^6 + \frac{3}{2}u^5 + \dots + \frac{1}{2}u^2 - \frac{1}{2}u \\ u^4 + u^3 + u^2 - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{1}{2}u^6 - \frac{1}{2}u^5 + \dots + \frac{1}{2}u + 1 \\ -u^5 - u^4 - 2u^3 - u^2 + 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} \frac{1}{2}u^6 + \frac{3}{2}u^5 + \dots - \frac{1}{2}u - 1 \\ -u^5 - 2u^4 - 2u^3 - u^2 + u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} c \\ -u^6c - 2u^5c - 3u^4c - 2u^3c + u^3 + cu + u^2 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^6c + 2u^5c + 3u^4c + 2u^3c - u^3 - cu - u^2 - c - u \\ -u^6c - 2u^5c - 3u^4c - 2u^3c + u^3 + cu + u^2 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^6c + 2u^5c + 3u^4c + 2u^3c + u^2c - u^3 - cu - u^2 - c - u \\ -u^6c - 2u^5c - 3u^4c - 2u^3c - u^2c + u^3 + cu + u^2 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{1}{2}u^6 + \frac{1}{2}u^5 + \dots + \frac{1}{2}u^2 - \frac{1}{2}u \\ -u^4c + u^5 - u^3c + 2u^4 - u^2c + 3u^3 + 2u^2 + u - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{1}{2}u^6 + \frac{1}{2}u^5 + \dots + \frac{1}{2}u^2 - \frac{1}{2}u \\ -u^4c + u^5 - u^3c + 2u^4 - u^2c + 3u^3 + 2u^2 + u - 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $2u^6 + 8u^5 + 10u^4 + 10u^3 - 4u$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$(u^7 - u^6 - u^5 + 2u^4 + u^3 - 2u^2 + u + 1)^2$
$c_2$	$(u^7 + 3u^6 + 7u^5 + 8u^4 + 9u^3 + 6u^2 + 5u + 1)^2$
$c_3, c_8$	$(u^7 + 3u^6 + 6u^5 + 7u^4 + 5u^3 + u^2 - 2u - 2)^2$
$c_5, c_6, c_7$ $c_9, c_{10}, c_{11}$	$u^{14} + u^{13} + \dots - 4u - 4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^7 - 3y^6 + 7y^5 - 8y^4 + 9y^3 - 6y^2 + 5y - 1)^2$
$c_2$	$(y^7 + 5y^6 + 19y^5 + 36y^4 + 49y^3 + 38y^2 + 13y - 1)^2$
$c_3, c_8$	$(y^7 + 3y^6 + 4y^5 + y^4 - y^3 + 7y^2 + 8y - 4)^2$
$c_5, c_6, c_7$ $c_9, c_{10}, c_{11}$	$y^{14} - 11y^{13} + \dots - 40y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.984140 + 0.426152I$		
$a = 0.472917 - 0.120643I$		
$b = -0.714380 - 0.998080I$	$1.19445 - 3.93070I$	$1.74059 + 4.87230I$
$c = -1.198550 - 0.312556I$		
$d = -0.438334 + 0.145757I$		
$u = -0.984140 + 0.426152I$		
$a = 0.472917 - 0.120643I$		
$b = -0.714380 - 0.998080I$	$1.19445 - 3.93070I$	$1.74059 + 4.87230I$
$c = 0.543084 - 0.485903I$		
$d = -0.376079 + 1.030380I$		
$u = -0.984140 - 0.426152I$		
$a = 0.472917 + 0.120643I$		
$b = -0.714380 + 0.998080I$	$1.19445 + 3.93070I$	$1.74059 - 4.87230I$
$c = -1.198550 + 0.312556I$		
$d = -0.438334 - 0.145757I$		
$u = -0.984140 - 0.426152I$		
$a = 0.472917 + 0.120643I$		
$b = -0.714380 + 0.998080I$	$1.19445 + 3.93070I$	$1.74059 - 4.87230I$
$c = 0.543084 + 0.485903I$		
$d = -0.376079 - 1.030380I$		
$u = -0.167785 + 1.218780I$		
$a = 0.529166 + 1.016880I$		
$b = 0.242061 - 0.924444I$	$7.14223 - 0.95540I$	$8.68929 + 2.37083I$
$c = -0.650809 - 0.592102I$		
$d = -0.300734 + 0.551723I$		
$u = -0.167785 + 1.218780I$		
$a = 0.529166 + 1.016880I$		
$b = 0.242061 - 0.924444I$	$7.14223 - 0.95540I$	$8.68929 + 2.37083I$
$c = 0.093897 + 1.158860I$		
$d = -0.13529 - 2.82138I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.167785 - 1.218780I$		
$a = 0.529166 - 1.016880I$		
$b = 0.242061 + 0.924444I$	$7.14223 + 0.95540I$	$8.68929 - 2.37083I$
$c = -0.650809 + 0.592102I$		
$d = -0.300734 - 0.551723I$		
$u = -0.167785 - 1.218780I$		
$a = 0.529166 - 1.016880I$		
$b = 0.242061 + 0.924444I$	$7.14223 + 0.95540I$	$8.68929 - 2.37083I$
$c = 0.093897 - 1.158860I$		
$d = -0.13529 + 2.82138I$		
$u = -0.654547 + 1.202470I$		
$a = -0.33478 - 1.51279I$		
$b = -0.90125 + 1.43610I$	$3.65356 + 9.93065I$	$3.53972 - 7.33664I$
$c = 0.292391 + 1.022450I$		
$d = -0.38305 - 2.56809I$		
$u = -0.654547 + 1.202470I$		
$a = -0.33478 - 1.51279I$		
$b = -0.90125 + 1.43610I$	$3.65356 + 9.93065I$	$3.53972 - 7.33664I$
$c = 0.509792 - 0.511513I$		
$d = 0.118485 + 0.850766I$		
$u = -0.654547 - 1.202470I$		
$a = -0.33478 + 1.51279I$		
$b = -0.90125 - 1.43610I$	$3.65356 - 9.93065I$	$3.53972 + 7.33664I$
$c = 0.292391 - 1.022450I$		
$d = -0.38305 + 2.56809I$		
$u = -0.654547 - 1.202470I$		
$a = -0.33478 + 1.51279I$		
$b = -0.90125 - 1.43610I$	$3.65356 - 9.93065I$	$3.53972 + 7.33664I$
$c = 0.509792 + 0.511513I$		
$d = 0.118485 - 0.850766I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.612945$		
$a = 0.665400$		
$b = -0.252863$	2.33847	2.06080
$c = -1.05845$		
$d = 1.74513$		
$u = 0.612945$		
$a = 0.665400$		
$b = -0.252863$	2.33847	2.06080
$c = 1.87884$		
$d = 0.284876$		

$$\text{III. } I_3^u = \langle -u^4 + d, -u^2 + c - 1, -u^4a + u^3 + \dots - a + 1, u^3a - u^3 + \dots - 2a + 1, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ u^4a + 2u^2a - u^3 + au + a - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4a - u^2a + u^3 - au + u + 1 \\ u^4a + u^4 + u^2a - 2u^3 + au + 2u^2 - 2u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^4a + 2u^2a - u^3 + au + 2a - u - 1 \\ -u^4 + 2u^3 - au - 2u^2 + 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^4 - u^2 - 1 \\ u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^4a - u^2a + u^3 - au + u + 1 \\ u^4a + u^4 + u^2a - 2u^3 + au + 2u^2 - 2u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^4a - u^2a + u^3 - au + u + 1 \\ u^4a + u^4 + u^2a - 2u^3 + au + 2u^2 - 2u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^3 + 4u^2 - 4u + 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}, c_{11}$	$u^{10} - u^9 - 2u^8 + 4u^7 - 4u^5 + 3u^4 + u^3 - 2u^2 + 1$
$c_2$	$u^{10} + 5u^9 + \dots + 4u + 1$
$c_3, c_8$	$(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$
$c_6, c_7, c_9$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}, c_{11}$	$y^{10} - 5y^9 + \dots - 4y + 1$
$c_2$	$y^{10} - y^9 - 6y^7 + 22y^6 + 6y^5 + 45y^4 + 15y^3 + 22y^2 + 4y + 1$
$c_3, c_8$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$
$c_6, c_7, c_9$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.339110 + 0.822375I$ $a = 0.445032 - 0.031192I$ $b = -1.50324 - 0.38743I$ $c = 0.438694 - 0.557752I$ $d = 0.003977 + 0.626138I$	$0.32910 + 1.53058I$	$2.51511 - 4.43065I$
$u = -0.339110 + 0.822375I$ $a = 0.46155 - 2.45660I$ $b = -0.703115 + 0.728284I$ $c = 0.438694 - 0.557752I$ $d = 0.003977 + 0.626138I$	$0.32910 + 1.53058I$	$2.51511 - 4.43065I$
$u = -0.339110 - 0.822375I$ $a = 0.445032 + 0.031192I$ $b = -1.50324 + 0.38743I$ $c = 0.438694 + 0.557752I$ $d = 0.003977 - 0.626138I$	$0.32910 - 1.53058I$	$2.51511 + 4.43065I$
$u = -0.339110 - 0.822375I$ $a = 0.46155 + 2.45660I$ $b = -0.703115 - 0.728284I$ $c = 0.438694 + 0.557752I$ $d = 0.003977 - 0.626138I$	$0.32910 - 1.53058I$	$2.51511 + 4.43065I$
$u = 0.766826$ $a = 0.595741 + 0.124010I$ $b = -0.258559 + 0.407825I$ $c = 1.58802$ $d = 0.345770$	2.40108	3.48110
$u = 0.766826$ $a = 0.595741 - 0.124010I$ $b = -0.258559 - 0.407825I$ $c = 1.58802$ $d = 0.345770$	2.40108	3.48110

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.455697 + 1.200150I$ $a = 0.542114 - 0.781069I$ $b = 0.586363 + 0.691742I$ $c = -0.232705 + 1.093810I$ $d = 0.32314 - 2.69669I$	$5.87256 - 4.40083I$	$6.74431 + 3.49859I$
$u = 0.455697 + 1.200150I$ $a = -0.04444 + 1.54938I$ $b = -0.62145 - 1.31364I$ $c = -0.232705 + 1.093810I$ $d = 0.32314 - 2.69669I$	$5.87256 - 4.40083I$	$6.74431 + 3.49859I$
$u = 0.455697 - 1.200150I$ $a = 0.542114 + 0.781069I$ $b = 0.586363 - 0.691742I$ $c = -0.232705 - 1.093810I$ $d = 0.32314 + 2.69669I$	$5.87256 + 4.40083I$	$6.74431 - 3.49859I$
$u = 0.455697 - 1.200150I$ $a = -0.04444 - 1.54938I$ $b = -0.62145 + 1.31364I$ $c = -0.232705 - 1.093810I$ $d = 0.32314 + 2.69669I$	$5.87256 + 4.40083I$	$6.74431 - 3.49859I$

$$\text{IV. } I_4^u = \langle 2u^4a - 2u^4 + \cdots + 4a - 4, -u^4a + u^4 + \cdots - 2a + 2, -u^4a + u^3 + \cdots - a + 1, u^3a - u^3 + \cdots - 2a + 1, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ u^4a + 2u^2a - u^3 + au + a - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4a - u^2a + u^3 - au + u + 1 \\ u^4a + u^4 + u^2a - 2u^3 + au + 2u^2 - 2u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^4a + 2u^2a - u^3 + au + 2a - u - 1 \\ -u^4 + 2u^3 - au - 2u^2 + 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^4a - u^4 + 2u^2a + u^3 - 3u^2 + 2a + u - 2 \\ -2u^4a + 2u^4 - 4u^2a - 2u^3 - au + 6u^2 - 4a - 2u + 4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^4a - u^4 + 2u^2a + u^3 + au - 3u^2 + 2a + u - 2 \\ -2u^4a + 2u^4 - 4u^2a - 2u^3 - au + 6u^2 - 4a - 2u + 4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2u^4a - u^3a - 2u^4 + 4u^2a + u^3 + au - 4u^2 + 3a - 2 \\ -3u^4a + u^3a + 3u^4 - 6u^2a - 2u^3 - au + 7u^2 - 5a - u + 4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 3u^4a - 2u^4 + 5u^2a + u^3 + au - 4u^2 + 4a - 3 \\ -3u^4a + 3u^4 - 5u^2a - 2u^3 - au + 6u^2 - 4a - u + 4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 3u^4a - 2u^4 + 5u^2a + u^3 + au - 4u^2 + 4a - 3 \\ -3u^4a + 3u^4 - 5u^2a - 2u^3 - au + 6u^2 - 4a - u + 4 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^3 + 4u^2 - 4u + 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_6$ $c_7, c_9$	$u^{10} - u^9 - 2u^8 + 4u^7 - 4u^5 + 3u^4 + u^3 - 2u^2 + 1$
$c_2$	$u^{10} + 5u^9 + \dots + 4u + 1$
$c_3, c_8$	$(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$
$c_5, c_{10}, c_{11}$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_6$ $c_7, c_9$	$y^{10} - 5y^9 + \dots - 4y + 1$
$c_2$	$y^{10} - y^9 - 6y^7 + 22y^6 + 6y^5 + 45y^4 + 15y^3 + 22y^2 + 4y + 1$
$c_3, c_8$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$
$c_5, c_{10}, c_{11}$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.339110 + 0.822375I$ $a = 0.445032 - 0.031192I$ $b = -1.50324 - 0.38743I$ $c = 0.366828 + 1.351750I$ $d = -0.60839 - 3.08007I$	$0.32910 + 1.53058I$	$2.51511 - 4.43065I$
$u = -0.339110 + 0.822375I$ $a = 0.46155 - 2.45660I$ $b = -0.703115 + 0.728284I$ $c = -0.805522 - 0.794001I$ $d = -0.252685 + 0.375376I$	$0.32910 + 1.53058I$	$2.51511 - 4.43065I$
$u = -0.339110 - 0.822375I$ $a = 0.445032 + 0.031192I$ $b = -1.50324 + 0.38743I$ $c = 0.366828 - 1.351750I$ $d = -0.60839 + 3.08007I$	$0.32910 - 1.53058I$	$2.51511 + 4.43065I$
$u = -0.339110 - 0.822375I$ $a = 0.46155 + 2.45660I$ $b = -0.703115 - 0.728284I$ $c = -0.805522 + 0.794001I$ $d = -0.252685 - 0.375376I$	$0.32910 - 1.53058I$	$2.51511 + 4.43065I$
$u = 0.766826$ $a = 0.595741 + 0.124010I$ $b = -0.258559 + 0.407825I$ $c = -0.794011 + 0.436741I$ $d = 1.13119 - 0.96858I$	2.40108	3.48110
$u = 0.766826$ $a = 0.595741 - 0.124010I$ $b = -0.258559 - 0.407825I$ $c = -0.794011 - 0.436741I$ $d = 1.13119 + 0.96858I$	2.40108	3.48110

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.455697 + 1.200150I$		
$a = 0.542114 - 0.781069I$		
$b = 0.586363 + 0.691742I$	$5.87256 - 4.40083I$	$6.74431 + 3.49859I$
$c = -0.518554 - 0.530425I$		
$d = -0.147334 + 0.766162I$		
$u = 0.455697 + 1.200150I$		
$a = -0.04444 + 1.54938I$		
$b = -0.62145 - 1.31364I$	$5.87256 - 4.40083I$	$6.74431 + 3.49859I$
$c = 0.751259 - 0.563387I$		
$d = 0.377218 + 0.474060I$		
$u = 0.455697 - 1.200150I$		
$a = 0.542114 + 0.781069I$		
$b = 0.586363 - 0.691742I$	$5.87256 + 4.40083I$	$6.74431 - 3.49859I$
$c = -0.518554 + 0.530425I$		
$d = -0.147334 - 0.766162I$		
$u = 0.455697 - 1.200150I$		
$a = -0.04444 - 1.54938I$		
$b = -0.62145 + 1.31364I$	$5.87256 + 4.40083I$	$6.74431 - 3.49859I$
$c = 0.751259 + 0.563387I$		
$d = 0.377218 - 0.474060I$		

$$\mathbf{V. } I_5^u = \langle -u^4 + d, -u^2 + c - 1, u^4 - u^3 + u^2 + b + 1, 2u^4 - u^3 + 4u^2 + a + 2, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2u^4 + u^3 - 4u^2 - 2 \\ -u^4 + u^3 - u^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^4 - 4u^2 - u - 2 \\ -2u^4 + 2u^3 - 2u^2 + u - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -3u^4 + 2u^3 - 5u^2 - 3 \\ u^4 - 2u^3 - 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^4 - u^2 - 1 \\ u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2u^4 - 4u^2 - u - 2 \\ -2u^4 + 2u^3 - 2u^2 + u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2u^4 - 4u^2 - u - 2 \\ -2u^4 + 2u^3 - 2u^2 + u - 2 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^3 + 4u^2 - 4u + 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_7, c_9$ $c_{10}, c_{11}$	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
$c_2$	$u^5 + 5u^4 + 8u^3 + 3u^2 - u + 1$
$c_3, c_8$	$u^5 - u^4 + 2u^3 - u^2 + u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_7, c_9$ $c_{10}, c_{11}$	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$
$c_2$	$y^5 - 9y^4 + 32y^3 - 35y^2 - 5y - 1$
$c_3, c_8$	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.339110 + 0.822375I$ $a = 0.886294 + 0.706265I$ $b = 0.206354 - 0.340852I$ $c = 0.438694 - 0.557752I$ $d = 0.003977 + 0.626138I$	$0.32910 + 1.53058I$	$2.51511 - 4.43065I$
$u = -0.339110 - 0.822375I$ $a = 0.886294 - 0.706265I$ $b = 0.206354 + 0.340852I$ $c = 0.438694 + 0.557752I$ $d = 0.003977 - 0.626138I$	$0.32910 - 1.53058I$	$2.51511 + 4.43065I$
$u = 0.766826$ $a = -4.59272$ $b = -1.48288$ $c = 1.58802$ $d = 0.345770$	2.40108	3.48110
$u = 0.455697 + 1.200150I$ $a = 0.410064 + 0.037156I$ $b = -1.96491 + 0.62190I$ $c = -0.232705 + 1.093810I$ $d = 0.32314 - 2.69669I$	$5.87256 - 4.40083I$	$6.74431 + 3.49859I$
$u = 0.455697 - 1.200150I$ $a = 0.410064 - 0.037156I$ $b = -1.96491 - 0.62190I$ $c = -0.232705 - 1.093810I$ $d = 0.32314 + 2.69669I$	$5.87256 + 4.40083I$	$6.74431 - 3.49859I$

$$\text{VI. } I_1^v = \langle c, d-1, b, a-1, v+1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8$	$u$
$c_5, c_9$	$u - 1$
$c_6, c_7, c_{10}$ $c_{11}$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8$	$y$
$c_5, c_6, c_7$ $c_9, c_{10}, c_{11}$	$y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 1.00000$		
$b = 0$	3.28987	12.0000
$c = 0$		
$d = 1.00000$		

$$\text{VII. } I_2^v = \langle a, d, c - 1, b + 1, v - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{10}, c_{11}$	$u - 1$
$c_2, c_4, c_5$	$u + 1$
$c_3, c_6, c_7$ $c_8, c_9$	$u$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_{10}, c_{11}$	$y - 1$
$c_3, c_6, c_7$ $c_8, c_9$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$		
$b = -1.00000$	0	0
$c = 1.00000$		
$d = 0$		

$$\text{VIII. } I_3^v = \langle a, d+1, c-a, b+1, v-1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u - 1$
$c_2, c_4, c_6$ $c_7$	$u + 1$
$c_3, c_5, c_8$ $c_{10}, c_{11}$	$u$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_6, c_7, c_9$	$y - 1$
$c_3, c_5, c_8$ $c_{10}, c_{11}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$		
$b = -1.00000$	0	0
$c = 0$		
$d = -1.00000$		

$$\text{IX. } I_4^v = \langle a, da + c - 1, dv + 1, cv - a - v, b + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ d \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v - 1 \\ -d \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -d \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ d - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ d - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $d^2 + v^2 + 4$

(iv) u-Polynomials at the component : It cannot be defined for a positive dimension component.

(v) Riley Polynomials at the component : It cannot be defined for a positive dimension component.

**(iv) Complex Volumes and Cusp Shapes**

Solution to $I_4^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	1.64493	$2.23718 - 0.09992I$
$c = \dots$		
$d = \dots$		

## X. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u(u-1)^2(u^5 + u^4 - 2u^3 - u^2 + u - 1)$ $\cdot (u^7 - u^6 - u^5 + 2u^4 + u^3 - 2u^2 + u + 1)^2$ $\cdot (u^{10} - u^9 - 2u^8 + 4u^7 - 4u^5 + 3u^4 + u^3 - 2u^2 + 1)^2$ $\cdot (u^{17} - 2u^{16} + \dots - 8u + 4)$
$c_2$	$u(u+1)^2(u^5 + 5u^4 + 8u^3 + 3u^2 - u + 1)$ $\cdot (u^7 + 3u^6 + 7u^5 + 8u^4 + 9u^3 + 6u^2 + 5u + 1)^2$ $\cdot ((u^{10} + 5u^9 + \dots + 4u + 1)^2)(u^{17} + 6u^{16} + \dots + 88u + 16)$
$c_3, c_8$	$u^3(u^5 - u^4 + 2u^3 - u^2 + u - 1)^5$ $\cdot ((u^7 + 3u^6 + \dots - 2u - 2)^2)(u^{17} - 2u^{16} + \dots - 4u^2 + 8)$
$c_4$	$u(u+1)^2(u^5 + u^4 - 2u^3 - u^2 + u - 1)$ $\cdot (u^7 - u^6 - u^5 + 2u^4 + u^3 - 2u^2 + u + 1)^2$ $\cdot (u^{10} - u^9 - 2u^8 + 4u^7 - 4u^5 + 3u^4 + u^3 - 2u^2 + 1)^2$ $\cdot (u^{17} - 2u^{16} + \dots - 8u + 4)$
$c_5, c_{10}, c_{11}$	$u(u-1)(u+1)(u^5 + u^4 - 2u^3 - u^2 + u - 1)^3$ $\cdot (u^{10} - u^9 - 2u^8 + 4u^7 - 4u^5 + 3u^4 + u^3 - 2u^2 + 1)$ $\cdot (u^{14} + u^{13} + \dots - 4u - 4)(u^{17} + 2u^{16} + \dots + 3u + 1)$
$c_6, c_7$	$u(u+1)^2(u^5 + u^4 - 2u^3 - u^2 + u - 1)^3$ $\cdot (u^{10} - u^9 - 2u^8 + 4u^7 - 4u^5 + 3u^4 + u^3 - 2u^2 + 1)$ $\cdot (u^{14} + u^{13} + \dots - 4u - 4)(u^{17} + 2u^{16} + \dots + 3u + 1)$
$c_9$	$u(u-1)^2(u^5 + u^4 - 2u^3 - u^2 + u - 1)^3$ $\cdot (u^{10} - u^9 - 2u^8 + 4u^7 - 4u^5 + 3u^4 + u^3 - 2u^2 + 1)$ $\cdot (u^{14} + u^{13} + \dots - 4u - 4)(u^{17} + 2u^{16} + \dots + 3u + 1)$

## XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y(y-1)^2(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)$ $\cdot (y^7 - 3y^6 + 7y^5 - 8y^4 + 9y^3 - 6y^2 + 5y - 1)^2$ $\cdot ((y^{10} - 5y^9 + \dots - 4y + 1)^2)(y^{17} - 6y^{16} + \dots + 88y - 16)$
$c_2$	$y(y-1)^2(y^5 - 9y^4 + 32y^3 - 35y^2 - 5y - 1)$ $\cdot (y^7 + 5y^6 + 19y^5 + 36y^4 + 49y^3 + 38y^2 + 13y - 1)^2$ $\cdot (y^{10} - y^9 - 6y^7 + 22y^6 + 6y^5 + 45y^4 + 15y^3 + 22y^2 + 4y + 1)^2$ $\cdot (y^{17} + 10y^{16} + \dots + 288y - 256)$
$c_3, c_8$	$y^3(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^5$ $\cdot (y^7 + 3y^6 + 4y^5 + y^4 - y^3 + 7y^2 + 8y - 4)^2$ $\cdot (y^{17} + 6y^{16} + \dots + 64y - 64)$
$c_5, c_6, c_7$ $c_9, c_{10}, c_{11}$	$y(y-1)^2(y^5 - 5y^4 + \dots - y - 1)^3(y^{10} - 5y^9 + \dots - 4y + 1)$ $\cdot (y^{14} - 11y^{13} + \dots - 40y + 16)(y^{17} - 20y^{16} + \dots + 27y - 1)$