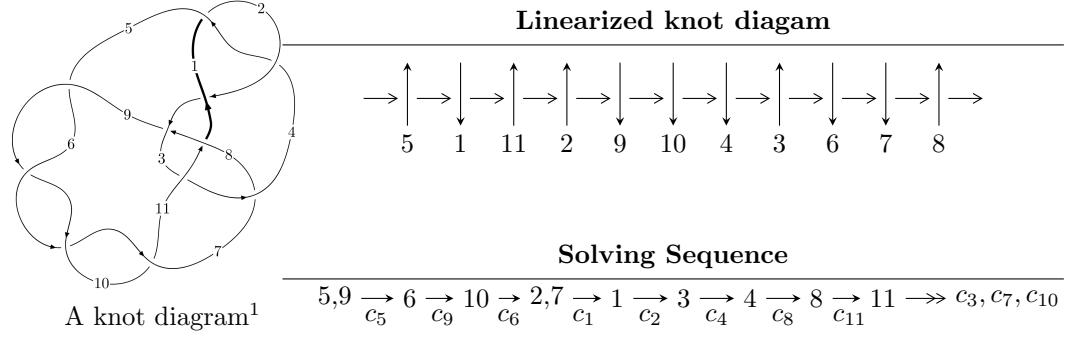


## $11a_{68}$ ( $K11a_{68}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 1.33754 \times 10^{33}u^{52} - 3.23197 \times 10^{33}u^{51} + \dots + 3.06100 \times 10^{33}b - 5.79603 \times 10^{32},$$

$$2.88344 \times 10^{33}u^{52} - 6.19301 \times 10^{33}u^{51} + \dots + 1.53050 \times 10^{33}a + 5.13286 \times 10^{33}, u^{53} - 3u^{52} + \dots - 2u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 55 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.34 \times 10^{33}u^{52} - 3.23 \times 10^{33}u^{51} + \dots + 3.06 \times 10^{33}b - 5.80 \times 10^{32}, 2.88 \times 10^{33}u^{52} - 6.19 \times 10^{33}u^{51} + \dots + 1.53 \times 10^{33}a + 5.13 \times 10^{33}, u^{53} - 3u^{52} + \dots - 2u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.88398u^{52} + 4.04640u^{51} + \dots - 10.2306u - 3.35372 \\ -0.436961u^{52} + 1.05586u^{51} + \dots + 2.97372u + 0.189351 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1.44702u^{52} + 2.99054u^{51} + \dots - 13.2043u - 3.54307 \\ -0.436961u^{52} + 1.05586u^{51} + \dots + 2.97372u + 0.189351 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 7.03077u^{52} - 17.2162u^{51} + \dots + 48.9314u + 11.3527 \\ -0.134450u^{52} + 0.381432u^{51} + \dots + 3.81964u + 1.58483 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -7.77919u^{52} + 19.0017u^{51} + \dots - 53.0234u - 12.7464 \\ 0.270228u^{52} - 0.655751u^{51} + \dots - 3.43986u - 1.30077 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -4.90683u^{52} + 11.3667u^{51} + \dots - 31.5879u - 8.19442 \\ -0.449321u^{52} + 0.286138u^{51} + \dots + 3.58531u + 0.111845 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 - 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 - 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $44.2881u^{52} - 103.441u^{51} + \dots + 256.874u + 76.5517$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{53} + 2u^{52} + \cdots - 11u - 1$
$c_2$	$u^{53} + 24u^{52} + \cdots + 25u - 1$
$c_3$	$u^{53} + 5u^{52} + \cdots + 4u - 4$
$c_5, c_6, c_9$ $c_{10}$	$u^{53} + 3u^{52} + \cdots - 2u + 1$
$c_7$	$u^{53} + 2u^{52} + \cdots - 127u - 29$
$c_8$	$u^{53} - 20u^{51} + \cdots + 127u + 59$
$c_{11}$	$u^{53} - 3u^{52} + \cdots - 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{53} + 24y^{52} + \cdots + 25y - 1$
$c_2$	$y^{53} + 12y^{52} + \cdots + 425y - 1$
$c_3$	$y^{53} + 15y^{52} + \cdots + 8y - 16$
$c_5, c_6, c_9$ $c_{10}$	$y^{53} - 63y^{52} + \cdots + 8y - 1$
$c_7$	$y^{53} - 60y^{52} + \cdots + 14273y - 841$
$c_8$	$y^{53} - 40y^{52} + \cdots - 44759y - 3481$
$c_{11}$	$y^{53} - 7y^{52} + \cdots + 8y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.733711 + 0.645681I$		
$a = -1.46416 - 1.02659I$	$-3.39428 - 3.43400I$	0
$b = 0.413624 - 1.013730I$		
$u = 0.733711 - 0.645681I$		
$a = -1.46416 + 1.02659I$	$-3.39428 + 3.43400I$	0
$b = 0.413624 + 1.013730I$		
$u = -0.858540 + 0.570989I$		
$a = -1.30456 + 1.52035I$	$-2.08339 + 11.83770I$	0
$b = 0.626693 + 1.121900I$		
$u = -0.858540 - 0.570989I$		
$a = -1.30456 - 1.52035I$	$-2.08339 - 11.83770I$	0
$b = 0.626693 - 1.121900I$		
$u = -0.890477 + 0.316821I$		
$a = 0.33516 - 1.62827I$	$-5.68960 + 3.88038I$	$-9.36604 - 5.67169I$
$b = 0.071350 - 1.206910I$		
$u = -0.890477 - 0.316821I$		
$a = 0.33516 + 1.62827I$	$-5.68960 - 3.88038I$	$-9.36604 + 5.67169I$
$b = 0.071350 + 1.206910I$		
$u = -0.790831 + 0.511450I$		
$a = 0.133210 + 0.424681I$	$0.02021 + 6.36572I$	$0. - 6.01738I$
$b = 0.848973 - 0.421707I$		
$u = -0.790831 - 0.511450I$		
$a = 0.133210 - 0.424681I$	$0.02021 - 6.36572I$	$0. + 6.01738I$
$b = 0.848973 + 0.421707I$		
$u = 1.042420 + 0.526470I$		
$a = 0.186261 + 0.817290I$	$-2.96394 + 2.74414I$	0
$b = 0.483358 + 1.013930I$		
$u = 1.042420 - 0.526470I$		
$a = 0.186261 - 0.817290I$	$-2.96394 - 2.74414I$	0
$b = 0.483358 - 1.013930I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.143820 + 0.277610I$		
$a = -0.769630 - 1.108100I$	$-1.68806 - 1.03417I$	0
$b = 0.398755 - 0.662277I$		
$u = 1.143820 - 0.277610I$		
$a = -0.769630 + 1.108100I$	$-1.68806 + 1.03417I$	0
$b = 0.398755 + 0.662277I$		
$u = -0.058774 + 0.801973I$		
$a = -0.804431 - 0.186468I$	$0.34476 - 7.28943I$	$-1.89770 + 7.29263I$
$b = 0.583629 - 1.059960I$		
$u = -0.058774 - 0.801973I$		
$a = -0.804431 + 0.186468I$	$0.34476 + 7.28943I$	$-1.89770 - 7.29263I$
$b = 0.583629 + 1.059960I$		
$u = 0.687960 + 0.265512I$		
$a = -0.675163 - 0.410284I$	$-1.33343 - 0.48154I$	$-6.01943 + 1.63910I$
$b = 0.229892 + 0.048634I$		
$u = 0.687960 - 0.265512I$		
$a = -0.675163 + 0.410284I$	$-1.33343 + 0.48154I$	$-6.01943 - 1.63910I$
$b = 0.229892 - 0.048634I$		
$u = -0.651505 + 0.261966I$		
$a = 1.01458 - 2.10036I$	$-0.87805 + 4.69027I$	$-3.22278 - 10.95263I$
$b = -0.598899 - 1.150440I$		
$u = -0.651505 - 0.261966I$		
$a = 1.01458 + 2.10036I$	$-0.87805 - 4.69027I$	$-3.22278 + 10.95263I$
$b = -0.598899 + 1.150440I$		
$u = -0.116335 + 0.680396I$		
$a = -1.030080 + 0.147365I$	$2.06084 - 2.35698I$	$2.09384 + 2.25421I$
$b = 0.691596 + 0.477793I$		
$u = -0.116335 - 0.680396I$		
$a = -1.030080 - 0.147365I$	$2.06084 + 2.35698I$	$2.09384 - 2.25421I$
$b = 0.691596 - 0.477793I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.269726 + 0.624271I$		
$a = -0.593135 - 0.023709I$	$-2.15945 - 0.98457I$	$-6.47095 + 3.55570I$
$b = 0.209100 + 0.945558I$		
$u = 0.269726 - 0.624271I$		
$a = -0.593135 + 0.023709I$	$-2.15945 + 0.98457I$	$-6.47095 - 3.55570I$
$b = 0.209100 - 0.945558I$		
$u = 0.655763 + 0.086361I$		
$a = 2.67182 + 5.33529I$	$-1.15754 - 2.23299I$	$20.7265 - 16.6825I$
$b = -0.482724 + 0.895174I$		
$u = 0.655763 - 0.086361I$		
$a = 2.67182 - 5.33529I$	$-1.15754 + 2.23299I$	$20.7265 + 16.6825I$
$b = -0.482724 - 0.895174I$		
$u = -0.466397 + 0.273654I$		
$a = 0.439898 - 0.865824I$	$1.29588 + 2.67274I$	$3.47265 - 8.90150I$
$b = -0.801200 - 0.670609I$		
$u = -0.466397 - 0.273654I$		
$a = 0.439898 + 0.865824I$	$1.29588 - 2.67274I$	$3.47265 + 8.90150I$
$b = -0.801200 + 0.670609I$		
$u = 0.495853 + 0.132805I$		
$a = -2.14393 + 2.54599I$	$-0.90053 + 1.58968I$	$-1.24595 - 11.67218I$
$b = -0.437475 - 0.833838I$		
$u = 0.495853 - 0.132805I$		
$a = -2.14393 - 2.54599I$	$-0.90053 - 1.58968I$	$-1.24595 + 11.67218I$
$b = -0.437475 + 0.833838I$		
$u = -0.339540 + 0.303762I$		
$a = -0.849048 - 0.809276I$	$1.60066 - 0.35812I$	$5.75025 - 1.86999I$
$b = -0.694807 + 0.319248I$		
$u = -0.339540 - 0.303762I$		
$a = -0.849048 + 0.809276I$	$1.60066 + 0.35812I$	$5.75025 + 1.86999I$
$b = -0.694807 - 0.319248I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.56006$		
$a = -0.846407$	-4.89339	0
$b = -1.04242$		
$u = 1.57394 + 0.03176I$		
$a = -0.266076 + 0.952973I$	$-5.77422 - 3.45795I$	0
$b = -0.981473 + 0.829936I$		
$u = 1.57394 - 0.03176I$		
$a = -0.266076 - 0.952973I$	$-5.77422 + 3.45795I$	0
$b = -0.981473 - 0.829936I$		
$u = -1.58085 + 0.00270I$		
$a = -0.420614 + 0.517476I$	$-8.08310 + 1.37745I$	0
$b = -0.490850 - 0.618356I$		
$u = -1.58085 - 0.00270I$		
$a = -0.420614 - 0.517476I$	$-8.08310 - 1.37745I$	0
$b = -0.490850 + 0.618356I$		
$u = 1.60794 + 0.05864I$		
$a = 0.21792 + 2.23198I$	$-8.69900 - 5.79684I$	0
$b = -0.60448 + 1.28732I$		
$u = 1.60794 - 0.05864I$		
$a = 0.21792 - 2.23198I$	$-8.69900 + 5.79684I$	0
$b = -0.60448 - 1.28732I$		
$u = -1.61440 + 0.12056I$		
$a = 0.0040355 + 0.1222230I$	$-9.21922 + 2.19279I$	0
$b = 0.623522 - 0.278275I$		
$u = -1.61440 - 0.12056I$		
$a = 0.0040355 - 0.1222230I$	$-9.21922 - 2.19279I$	0
$b = 0.623522 + 0.278275I$		
$u = -1.61997 + 0.02761I$		
$a = 1.27413 - 2.99101I$	$-9.14547 + 2.68229I$	0
$b = -0.490506 - 0.975564I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.61997 - 0.02761I$		
$a = 1.27413 + 2.99101I$	$-9.14547 - 2.68229I$	0
$b = -0.490506 + 0.975564I$		
$u = 1.64104 + 0.14587I$		
$a = 0.552638 - 0.075300I$	$-8.29591 - 8.86132I$	0
$b = 0.956160 + 0.388075I$		
$u = 1.64104 - 0.14587I$		
$a = 0.552638 + 0.075300I$	$-8.29591 + 8.86132I$	0
$b = 0.956160 - 0.388075I$		
$u = -1.64394 + 0.19308I$		
$a = -0.87986 + 1.71349I$	$-11.49850 + 6.63397I$	0
$b = 0.514455 + 1.092180I$		
$u = -1.64394 - 0.19308I$		
$a = -0.87986 - 1.71349I$	$-11.49850 - 6.63397I$	0
$b = 0.514455 - 1.092180I$		
$u = 1.66296 + 0.08851I$		
$a = 0.24702 + 2.16359I$	$-14.5372 - 5.4639I$	0
$b = 0.098247 + 1.348150I$		
$u = 1.66296 - 0.08851I$		
$a = 0.24702 - 2.16359I$	$-14.5372 + 5.4639I$	0
$b = 0.098247 - 1.348150I$		
$u = 1.66393 + 0.16732I$		
$a = -0.72953 - 1.98988I$	$-10.7030 - 14.7003I$	0
$b = 0.650090 - 1.173960I$		
$u = 1.66393 - 0.16732I$		
$a = -0.72953 + 1.98988I$	$-10.7030 + 14.7003I$	0
$b = 0.650090 + 1.173960I$		
$u = -0.111963 + 0.267344I$		
$a = -0.771605 - 0.811778I$	$0.54222 - 2.63785I$	$2.19810 + 0.73658I$
$b = -0.612381 + 0.946401I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.111963 - 0.267344I$		
$a = -0.771605 + 0.811778I$	$0.54222 + 2.63785I$	$2.19810 - 0.73658I$
$b = -0.612381 - 0.946401I$		
$u = -1.71557 + 0.08761I$		
$a = 0.04836 - 1.70377I$	$-12.82680 - 0.50129I$	0
$b = 0.316553 - 1.065110I$		
$u = -1.71557 - 0.08761I$		
$a = 0.04836 + 1.70377I$	$-12.82680 + 0.50129I$	0
$b = 0.316553 + 1.065110I$		

$$\text{II. } I_2^u = \langle 2b - a - 1, \ a^2 + 3, \ u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_2 &= \begin{pmatrix} a \\ \frac{1}{2}a + \frac{1}{2} \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} \frac{1}{2}a - \frac{1}{2} \\ \frac{1}{2}a + \frac{1}{2} \end{pmatrix} \\ a_3 &= \begin{pmatrix} \frac{1}{2}a - \frac{1}{2} \\ \frac{1}{2}a - \frac{1}{2} \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{1}{2}a - \frac{1}{2} \\ \frac{1}{2}a - \frac{1}{2} \end{pmatrix} \\ a_8 &= \begin{pmatrix} \frac{1}{2}a + \frac{1}{2} \\ \frac{1}{2}a + \frac{3}{2} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -1 \\ -1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -1 \\ -1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-2a - 3$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$u^2 + u + 1$
$c_3$	$u^2$
$c_4, c_7, c_8$	$u^2 - u + 1$
$c_5, c_6$	$(u - 1)^2$
$c_9, c_{10}, c_{11}$	$(u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_7, c_8$	$y^2 + y + 1$
$c_3$	$y^2$
$c_5, c_6, c_9$ $c_{10}, c_{11}$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.73205I$	$-1.64493 + 2.02988I$	$-3.00000 - 3.46410I$
$b = 0.500000 + 0.866025I$		
$u = 1.00000$		
$a = -1.73205I$	$-1.64493 - 2.02988I$	$-3.00000 + 3.46410I$
$b = 0.500000 - 0.866025I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 + u + 1)(u^{53} + 2u^{52} + \dots - 11u - 1)$
$c_2$	$(u^2 + u + 1)(u^{53} + 24u^{52} + \dots + 25u - 1)$
$c_3$	$u^2(u^{53} + 5u^{52} + \dots + 4u - 4)$
$c_4$	$(u^2 - u + 1)(u^{53} + 2u^{52} + \dots - 11u - 1)$
$c_5, c_6$	$((u - 1)^2)(u^{53} + 3u^{52} + \dots - 2u + 1)$
$c_7$	$(u^2 - u + 1)(u^{53} + 2u^{52} + \dots - 127u - 29)$
$c_8$	$(u^2 - u + 1)(u^{53} - 20u^{51} + \dots + 127u + 59)$
$c_9, c_{10}$	$((u + 1)^2)(u^{53} + 3u^{52} + \dots - 2u + 1)$
$c_{11}$	$((u + 1)^2)(u^{53} - 3u^{52} + \dots - 2u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^2 + y + 1)(y^{53} + 24y^{52} + \dots + 25y - 1)$
$c_2$	$(y^2 + y + 1)(y^{53} + 12y^{52} + \dots + 425y - 1)$
$c_3$	$y^2(y^{53} + 15y^{52} + \dots + 8y - 16)$
$c_5, c_6, c_9$ $c_{10}$	$((y - 1)^2)(y^{53} - 63y^{52} + \dots + 8y - 1)$
$c_7$	$(y^2 + y + 1)(y^{53} - 60y^{52} + \dots + 14273y - 841)$
$c_8$	$(y^2 + y + 1)(y^{53} - 40y^{52} + \dots - 44759y - 3481)$
$c_{11}$	$((y - 1)^2)(y^{53} - 7y^{52} + \dots + 8y - 1)$