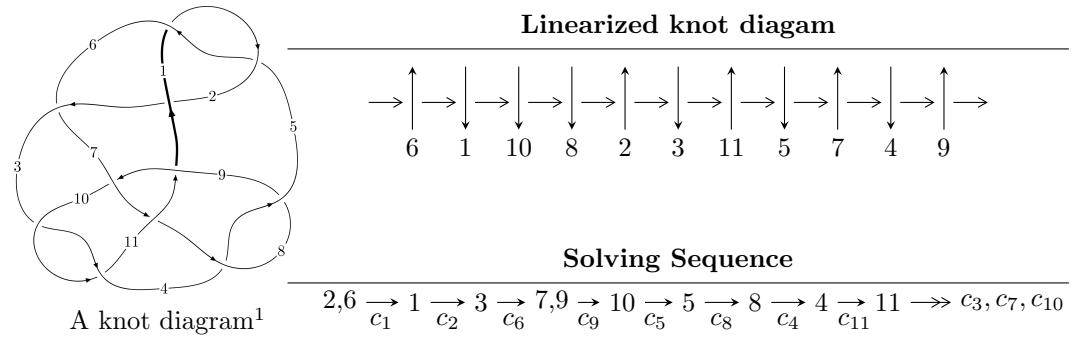


$$\frac{1}{11}a_{99} \left( K \frac{1}{11}a_{99} \right)$$



## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
I_1^u &= \langle -3u^{27} - 26u^{26} + \cdots + 2b - 6, 9u^{27} + 72u^{26} + \cdots + 4a + 84, u^{28} + 6u^{27} + \cdots + 26u + 4 \rangle \\
I_2^u &= \langle 5947395u^9a^3 - 110563267u^9a^2 + \cdots + 261341462a - 88347236, -u^9a^3 - 5u^9a^2 + \cdots - 8a - 7, \\
&\quad u^{10} - u^9 + 3u^8 - 3u^7 + 5u^6 - 5u^5 + 4u^4 - 4u^3 + 3u^2 - 2u + 1 \rangle \\
I_3^u &= \langle u^{11} - u^{10} + 4u^9 - 3u^8 + 7u^7 - 4u^6 + 4u^5 - u^3 + 3u^2 + b - 2u + 3, \\
&\quad -2u^{12} + u^{11} - 6u^{10} + u^9 - 8u^8 - u^7 - 2u^6 - 4u^5 + u^4 - 2u^3 + a - 2u - 2, \\
&\quad u^{13} - u^{12} + 4u^{11} - 3u^{10} + 7u^9 - 4u^8 + 5u^7 - u^6 + 2u^4 - 2u^3 + 3u^2 - u + 1 \rangle \\
I_4^u &= \langle a^3u - a^2u^2 + a^2u + u^2a - a^2 + 4u^2 + b + a - 2u + 5, \\
&\quad a^4 - 3a^2u^2 + a^3 + 3a^2u - 3u^2a - 4a^2 + 3au + 9u^2 - 4a - 6u + 13, u^3 + u + 1 \rangle
\end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 93 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -3u^{27} - 26u^{26} + \dots + 2b - 6, 9u^{27} + 72u^{26} + \dots + 4a + 84, u^{28} + 6u^{27} + \dots + 26u + 4 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^2 + 1 \\ u^4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^5 - 2u^3 - u \\ -u^7 - u^5 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{9}{4}u^{27} - 18u^{26} + \dots - \frac{513}{4}u - 21 \\ \frac{3}{2}u^{27} + 13u^{26} + \dots + \frac{77}{2}u + 3 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{11}{4}u^{27} + 14u^{26} + \dots + \frac{143}{4}u + 5 \\ -\frac{5}{2}u^{27} - 15u^{26} + \dots - \frac{127}{2}u - 11 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{21}{4}u^{27} - 29u^{26} + \dots - \frac{449}{4}u - 19 \\ \frac{9}{2}u^{27} + 24u^{26} + \dots + \frac{45}{2}u + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -\frac{1}{2}u^{27} - \frac{3}{2}u^{26} + \dots - \frac{41}{2}u - \frac{7}{2} \\ -\frac{5}{2}u^{27} - 14u^{26} + \dots - \frac{55}{2}u - 4 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{1}{2}u^{27} + \frac{9}{2}u^{26} + \dots + \frac{73}{2}u + \frac{13}{2} \\ -\frac{1}{2}u^{27} - 3u^{26} + \dots + \frac{7}{2}u + 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{1}{2}u^{27} + \frac{9}{2}u^{26} + \dots + \frac{73}{2}u + \frac{13}{2} \\ -\frac{1}{2}u^{27} - 3u^{26} + \dots + \frac{7}{2}u + 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -13u^{27} - 78u^{26} - 316u^{25} - 906u^{24} - 2126u^{23} - 4197u^{22} - \\ &7359u^{21} - 11710u^{20} - 17291u^{19} - 23878u^{18} - 30954u^{17} - 37835u^{16} - 43786u^{15} - \\ &48249u^{14} - 50700u^{13} - 50669u^{12} - 48099u^{11} - 43213u^{10} - 36755u^9 - 29326u^8 - \\ &21691u^7 - 14716u^6 - 9106u^5 - 5172u^4 - 2641u^3 - 1112u^2 - 342u - 54 \end{aligned}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{28} - 6u^{27} + \cdots - 26u + 4$
$c_2$	$u^{28} + 14u^{27} + \cdots + 36u + 16$
$c_3, c_4, c_8$ $c_{10}$	$u^{28} + u^{27} + \cdots + 3u + 1$
$c_6$	$u^{28} + 6u^{27} + \cdots + 1800u + 712$
$c_7$	$u^{28} - 29u^{27} + \cdots - 118784u + 8192$
$c_9, c_{11}$	$u^{28} - 2u^{27} + \cdots - 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{28} + 14y^{27} + \cdots + 36y + 16$
$c_2$	$y^{28} - 2y^{27} + \cdots - 240y + 256$
$c_3, c_4, c_8$ $c_{10}$	$y^{28} - 23y^{27} + \cdots + 3y + 1$
$c_6$	$y^{28} - 18y^{27} + \cdots + 1943360y + 506944$
$c_7$	$y^{28} + 3y^{27} + \cdots + 486539264y + 67108864$
$c_9, c_{11}$	$y^{28} + 6y^{27} + \cdots + 40y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.007890 + 0.244456I$		
$a = 0.648218 + 0.649776I$	$-5.75558 + 1.16478I$	$-9.81484 - 5.25007I$
$b = 0.484897 - 0.362346I$		
$u = -1.007890 - 0.244456I$		
$a = 0.648218 - 0.649776I$	$-5.75558 - 1.16478I$	$-9.81484 + 5.25007I$
$b = 0.484897 + 0.362346I$		
$u = 0.450069 + 0.945327I$		
$a = 0.97063 - 1.16479I$	$1.30775 + 2.44749I$	$-4.69640 - 9.53101I$
$b = -0.92359 + 1.77022I$		
$u = 0.450069 - 0.945327I$		
$a = 0.97063 + 1.16479I$	$1.30775 - 2.44749I$	$-4.69640 + 9.53101I$
$b = -0.92359 - 1.77022I$		
$u = 0.823545 + 0.669603I$		
$a = -0.244511 + 1.089610I$	$-2.90686 - 3.71581I$	$-3.96472 + 7.21162I$
$b = -0.807023 - 0.636285I$		
$u = 0.823545 - 0.669603I$		
$a = -0.244511 - 1.089610I$	$-2.90686 + 3.71581I$	$-3.96472 - 7.21162I$
$b = -0.807023 + 0.636285I$		
$u = -0.877743 + 0.205256I$		
$a = -1.36751 - 0.95489I$	$-7.91511 + 11.38140I$	$-4.44423 - 5.90932I$
$b = -0.332382 + 1.109600I$		
$u = -0.877743 - 0.205256I$		
$a = -1.36751 + 0.95489I$	$-7.91511 - 11.38140I$	$-4.44423 + 5.90932I$
$b = -0.332382 - 1.109600I$		
$u = 0.693563 + 0.915180I$		
$a = -1.289000 - 0.358838I$	$-3.67868 + 9.29135I$	$-4.02619 - 9.42557I$
$b = 1.64479 - 0.73716I$		
$u = 0.693563 - 0.915180I$		
$a = -1.289000 + 0.358838I$	$-3.67868 - 9.29135I$	$-4.02619 + 9.42557I$
$b = 1.64479 + 0.73716I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.417630 + 1.105260I$		
$a = -0.990060 - 0.503261I$	$-2.12382 - 1.70105I$	$-2.95787 + 0.05705I$
$b = 0.343945 + 0.624215I$		
$u = -0.417630 - 1.105260I$		
$a = -0.990060 + 0.503261I$	$-2.12382 + 1.70105I$	$-2.95787 - 0.05705I$
$b = 0.343945 - 0.624215I$		
$u = -0.483475 + 1.130610I$		
$a = 1.03565 + 1.24896I$	$-1.61917 - 5.94948I$	$-1.73292 + 6.08838I$
$b = -0.38060 - 1.45896I$		
$u = -0.483475 - 1.130610I$		
$a = 1.03565 - 1.24896I$	$-1.61917 + 5.94948I$	$-1.73292 - 6.08838I$
$b = -0.38060 + 1.45896I$		
$u = 0.433444 + 0.634083I$		
$a = 1.80511 - 0.76581I$	$2.24308 + 1.31021I$	$4.48172 + 2.40271I$
$b = -1.031200 + 0.788265I$		
$u = 0.433444 - 0.634083I$		
$a = 1.80511 + 0.76581I$	$2.24308 - 1.31021I$	$4.48172 - 2.40271I$
$b = -1.031200 - 0.788265I$		
$u = -0.305330 + 0.675911I$		
$a = -0.630555 + 0.172210I$	$-0.257625 - 1.154960I$	$-2.96071 + 5.77634I$
$b = 0.360299 + 0.412592I$		
$u = -0.305330 - 0.675911I$		
$a = -0.630555 - 0.172210I$	$-0.257625 + 1.154960I$	$-2.96071 - 5.77634I$
$b = 0.360299 - 0.412592I$		
$u = -0.315106 + 1.262770I$		
$a = 0.488001 + 0.002907I$	$-12.6068 + 7.4137I$	$-9.32623 - 3.45211I$
$b = 0.100408 + 1.021430I$		
$u = -0.315106 - 1.262770I$		
$a = 0.488001 - 0.002907I$	$-12.6068 - 7.4137I$	$-9.32623 + 3.45211I$
$b = 0.100408 - 1.021430I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.554721 + 1.203480I$		
$a = -1.83799 - 0.92930I$	$-10.9151 - 16.6086I$	$-7.19926 + 9.00617I$
$b = 1.96223 + 2.11484I$		
$u = -0.554721 - 1.203480I$		
$a = -1.83799 + 0.92930I$	$-10.9151 + 16.6086I$	$-7.19926 - 9.00617I$
$b = 1.96223 - 2.11484I$		
$u = -0.243939 + 1.326510I$		
$a = -0.0674133 + 0.0418679I$	$-11.26130 - 3.02152I$	$-13.62827 + 2.14467I$
$b = -0.033141 - 1.007620I$		
$u = -0.243939 - 1.326510I$		
$a = -0.0674133 - 0.0418679I$	$-11.26130 + 3.02152I$	$-13.62827 - 2.14467I$
$b = -0.033141 + 1.007620I$		
$u = -0.608424 + 0.177740I$		
$a = 0.665110 - 0.192137I$	$1.04620 + 1.66789I$	$3.14449 - 2.66380I$
$b = -0.474963 - 0.907755I$		
$u = -0.608424 - 0.177740I$		
$a = 0.665110 + 0.192137I$	$1.04620 - 1.66789I$	$3.14449 + 2.66380I$
$b = -0.474963 + 0.907755I$		
$u = -0.586363 + 1.242360I$		
$a = 1.064320 + 0.381059I$	$-8.88695 - 6.88314I$	$-9.37455 + 6.80974I$
$b = -1.41368 - 1.21973I$		
$u = -0.586363 - 1.242360I$		
$a = 1.064320 - 0.381059I$	$-8.88695 + 6.88314I$	$-9.37455 - 6.80974I$
$b = -1.41368 + 1.21973I$		

$$\text{II. } I_2^u = \langle 5.95 \times 10^6 a^3 u^9 - 1.11 \times 10^8 a^2 u^9 + \dots + 2.61 \times 10^8 a - 8.83 \times 10^7, -u^9 a^3 - 5u^9 a^2 + \dots - 8a - 7, u^{10} - u^9 + \dots - 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^2 + 1 \\ u^4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^5 - 2u^3 - u \\ -u^7 - u^5 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} a \\ -0.0456620a^3 u^9 + 0.848865a^2 u^9 + \dots - 2.00649a + 0.678298 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 2.14382a^3 u^9 + 1.09367a^2 u^9 + \dots - 1.51933a + 0.196840 \\ -0.260987a^3 u^9 + 0.338504a^2 u^9 + \dots + 0.870243a + 2.69447 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.0644237a^3 u^9 + 0.101106a^2 u^9 + \dots - 1.19004a - 1.96492 \\ -0.110086a^3 u^9 + 0.747759a^2 u^9 + \dots + 0.183553a + 2.64322 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.770676a^3 u^9 - 0.285432a^2 u^9 + \dots - 0.188169a - 1.85717 \\ -0.0386232a^3 u^9 + 0.223455a^2 u^9 + \dots + 1.74875a + 3.11581 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.277440a^3 u^9 - 0.327129a^2 u^9 + \dots - 0.0644294a + 0.411808 \\ -0.285316a^3 u^9 + 0.175678a^2 u^9 + \dots + 0.268957a - 0.519132 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.277440a^3 u^9 - 0.327129a^2 u^9 + \dots - 0.0644294a + 0.411808 \\ -0.285316a^3 u^9 + 0.175678a^2 u^9 + \dots + 0.268957a - 0.519132 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

$$(iii) \text{ Cusp Shapes} = \frac{6098888}{7661669} u^9 a^3 - \frac{21091308}{7661669} u^9 a^2 + \dots + \frac{116819364}{7661669} a + \frac{59639590}{7661669}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u^{10} + u^9 + 3u^8 + 3u^7 + 5u^6 + 5u^5 + 4u^4 + 4u^3 + 3u^2 + 2u + 1)^4$
$c_2$	$(u^{10} + 5u^9 + 13u^8 + 19u^7 + 17u^6 + 7u^5 - 2u^3 + u^2 + 2u + 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$u^{40} - u^{39} + \cdots - 18u^2 + 1$
$c_6$	$(u^{10} + 2u^9 - u^8 - 5u^7 - 3u^6 + 4u^5 + 12u^4 + 13u^3 + 5u^2 + u + 2)^4$
$c_7$	$(u^2 + u + 1)^{20}$
$c_9, c_{11}$	$u^{40} + 11u^{39} + \cdots + 644u + 61$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$(y^{10} + 5y^9 + 13y^8 + 19y^7 + 17y^6 + 7y^5 - 2y^3 + y^2 + 2y + 1)^4$
$c_2$	$(y^{10} + y^9 + 13y^8 + 11y^7 + 45y^6 + 35y^5 + 12y^4 + 2y^3 + 9y^2 - 2y + 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$y^{40} - 33y^{39} + \cdots - 36y + 1$
$c_6$	$(y^{10} - 6y^9 + \cdots + 19y + 4)^4$
$c_7$	$(y^2 + y + 1)^{20}$
$c_9, c_{11}$	$y^{40} + 11y^{39} + \cdots + 62528y + 3721$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.584958 + 0.771492I$		
$a = -0.811252 - 0.684607I$	$0.002387 - 0.280172I$	$-1.136314 + 0.057227I$
$b = 0.326566 + 1.346250I$		
$u = -0.584958 + 0.771492I$		
$a = -0.13825 + 1.48131I$	$0.002387 - 0.280172I$	$-1.136314 + 0.057227I$
$b = 0.856552 - 0.765235I$		
$u = -0.584958 + 0.771492I$		
$a = 1.41803 - 0.77086I$	$0.00239 - 4.33994I$	$-1.13631 + 6.98543I$
$b = -1.87810 - 0.26325I$		
$u = -0.584958 + 0.771492I$		
$a = -1.63324 - 0.44978I$	$0.00239 - 4.33994I$	$-1.13631 + 6.98543I$
$b = 0.783367 + 0.997354I$		
$u = -0.584958 - 0.771492I$		
$a = -0.811252 + 0.684607I$	$0.002387 + 0.280172I$	$-1.136314 - 0.057227I$
$b = 0.326566 - 1.346250I$		
$u = -0.584958 - 0.771492I$		
$a = -0.13825 - 1.48131I$	$0.002387 + 0.280172I$	$-1.136314 - 0.057227I$
$b = 0.856552 + 0.765235I$		
$u = -0.584958 - 0.771492I$		
$a = 1.41803 + 0.77086I$	$0.00239 + 4.33994I$	$-1.13631 - 6.98543I$
$b = -1.87810 + 0.26325I$		
$u = -0.584958 - 0.771492I$		
$a = -1.63324 + 0.44978I$	$0.00239 + 4.33994I$	$-1.13631 - 6.98543I$
$b = 0.783367 - 0.997354I$		
$u = 0.248527 + 0.782547I$		
$a = -0.528657 + 0.220233I$	$-5.38286 + 3.26157I$	$-6.90177 - 8.91318I$
$b = 0.80276 - 1.85708I$		
$u = 0.248527 + 0.782547I$		
$a = -0.77879 + 1.65055I$	$-5.38286 - 0.79819I$	$-6.90177 - 1.98497I$
$b = -0.1103870 - 0.0163537I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.248527 + 0.782547I$		
$a = -2.16490 - 1.33388I$	$-5.38286 - 0.79819I$	$-6.90177 - 1.98497I$
$b = 2.78977 + 0.25266I$		
$u = 0.248527 + 0.782547I$		
$a = 2.27476 + 2.17074I$	$-5.38286 + 3.26157I$	$-6.90177 - 8.91318I$
$b = -1.93781 - 0.58149I$		
$u = 0.248527 - 0.782547I$		
$a = -0.528657 - 0.220233I$	$-5.38286 - 3.26157I$	$-6.90177 + 8.91318I$
$b = 0.80276 + 1.85708I$		
$u = 0.248527 - 0.782547I$		
$a = -0.77879 - 1.65055I$	$-5.38286 + 0.79819I$	$-6.90177 + 1.98497I$
$b = -0.1103870 + 0.0163537I$		
$u = 0.248527 - 0.782547I$		
$a = -2.16490 + 1.33388I$	$-5.38286 + 0.79819I$	$-6.90177 + 1.98497I$
$b = 2.78977 - 0.25266I$		
$u = 0.248527 - 0.782547I$		
$a = 2.27476 - 2.17074I$	$-5.38286 - 3.26157I$	$-6.90177 + 8.91318I$
$b = -1.93781 + 0.58149I$		
$u = 0.761643 + 0.208049I$		
$a = -0.888121 - 0.198095I$	$-2.52120 - 5.50828I$	$-2.80497 + 6.25925I$
$b = 0.169145 - 1.209710I$		
$u = 0.761643 + 0.208049I$		
$a = -1.109160 + 0.691872I$	$-2.52120 - 1.44851I$	$-2.80497 - 0.66896I$
$b = -0.405801 - 0.684900I$		
$u = 0.761643 + 0.208049I$		
$a = -0.465789 - 0.420142I$	$-2.52120 - 1.44851I$	$-2.80497 - 0.66896I$
$b = 0.307020 + 0.341147I$		
$u = 0.761643 + 0.208049I$		
$a = 1.44027 - 1.30172I$	$-2.52120 - 5.50828I$	$-2.80497 + 6.25925I$
$b = 0.177943 + 1.296040I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.761643 - 0.208049I$		
$a = -0.888121 + 0.198095I$	$-2.52120 + 5.50828I$	$-2.80497 - 6.25925I$
$b = 0.169145 + 1.209710I$		
$u = 0.761643 - 0.208049I$		
$a = -1.109160 - 0.691872I$	$-2.52120 + 1.44851I$	$-2.80497 + 0.66896I$
$b = -0.405801 + 0.684900I$		
$u = 0.761643 - 0.208049I$		
$a = -0.465789 + 0.420142I$	$-2.52120 + 1.44851I$	$-2.80497 + 0.66896I$
$b = 0.307020 - 0.341147I$		
$u = 0.761643 - 0.208049I$		
$a = 1.44027 + 1.30172I$	$-2.52120 + 5.50828I$	$-2.80497 - 6.25925I$
$b = 0.177943 - 1.296040I$		
$u = -0.449566 + 1.164790I$		
$a = 0.79423 - 1.18245I$	$-9.81146 - 6.17573I$	$-10.98134 + 7.44010I$
$b = -0.42710 + 2.17011I$		
$u = -0.449566 + 1.164790I$		
$a = 0.152868 - 0.428323I$	$-9.81146 - 2.11597I$	$-10.98134 + 0.51190I$
$b = -1.107140 - 0.677603I$		
$u = -0.449566 + 1.164790I$		
$a = 1.92707 + 0.90418I$	$-9.81146 - 6.17573I$	$-10.98134 + 7.44010I$
$b = -1.82941 - 2.34062I$		
$u = -0.449566 + 1.164790I$		
$a = -1.75450 - 1.78926I$	$-9.81146 - 2.11597I$	$-10.98134 + 0.51190I$
$b = 2.08774 + 2.71705I$		
$u = -0.449566 - 1.164790I$		
$a = 0.79423 + 1.18245I$	$-9.81146 + 6.17573I$	$-10.98134 - 7.44010I$
$b = -0.42710 - 2.17011I$		
$u = -0.449566 - 1.164790I$		
$a = 0.152868 + 0.428323I$	$-9.81146 + 2.11597I$	$-10.98134 - 0.51190I$
$b = -1.107140 + 0.677603I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.449566 - 1.164790I$		
$a = 1.92707 - 0.90418I$	$-9.81146 + 6.17573I$	$-10.98134 - 7.44010I$
$b = -1.82941 + 2.34062I$		
$u = -0.449566 - 1.164790I$		
$a = -1.75450 + 1.78926I$	$-9.81146 + 2.11597I$	$-10.98134 - 0.51190I$
$b = 2.08774 - 2.71705I$		
$u = 0.524355 + 1.163410I$		
$a = 0.740427 + 0.151085I$	$-5.31595 + 6.25643I$	$-6.17560 - 2.68471I$
$b = -0.650836 - 0.191721I$		
$u = 0.524355 + 1.163410I$		
$a = -1.43496 + 0.55642I$	$-5.31595 + 6.25643I$	$-6.17560 - 2.68471I$
$b = 1.51204 - 1.58158I$		
$u = 0.524355 + 1.163410I$		
$a = -1.20657 + 1.25082I$	$-5.31595 + 10.31620I$	$-6.17560 - 9.61291I$
$b = 0.33739 - 1.88156I$		
$u = 0.524355 + 1.163410I$		
$a = 2.16655 - 1.00309I$	$-5.31595 + 10.31620I$	$-6.17560 - 9.61291I$
$b = -2.30372 + 2.02238I$		
$u = 0.524355 - 1.163410I$		
$a = 0.740427 - 0.151085I$	$-5.31595 - 6.25643I$	$-6.17560 + 2.68471I$
$b = -0.650836 + 0.191721I$		
$u = 0.524355 - 1.163410I$		
$a = -1.43496 - 0.55642I$	$-5.31595 - 6.25643I$	$-6.17560 + 2.68471I$
$b = 1.51204 + 1.58158I$		
$u = 0.524355 - 1.163410I$		
$a = -1.20657 - 1.25082I$	$-5.31595 - 10.31620I$	$-6.17560 + 9.61291I$
$b = 0.33739 + 1.88156I$		
$u = 0.524355 - 1.163410I$		
$a = 2.16655 + 1.00309I$	$-5.31595 - 10.31620I$	$-6.17560 + 9.61291I$
$b = -2.30372 - 2.02238I$		

### III.

$$I_3^u = \langle u^{11} - u^{10} + \cdots + b + 3, -2u^{12} + u^{11} + \cdots + a - 2, u^{13} - u^{12} + \cdots - u + 1 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^5 - 2u^3 - u \\ -u^7 - u^5 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^{12} - u^{11} + 6u^{10} - u^9 + 8u^8 + u^7 + 2u^6 + 4u^5 - u^4 + 2u^3 + 2u + 2 \\ -u^{11} + u^{10} - 4u^9 + 3u^8 - 7u^7 + 4u^6 - 4u^5 + u^3 - 3u^2 + 2u - 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u^{12} - u^{11} + 6u^{10} - 2u^9 + 8u^8 - u^7 + 2u^6 + 2u^5 - u^4 + 2u^3 + 2u + 2 \\ -u^{11} + u^{10} - 3u^9 + 3u^8 - 5u^7 + 4u^6 - 2u^5 + u^3 - 2u^2 + 2u - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{12} + 3u^{10} + u^9 + 4u^8 + 3u^7 + u^6 + 3u^5 + u^2 + 2 \\ u^{12} - 2u^{11} + \cdots + 4u - 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{12} - u^{11} - 2u^{10} - 4u^9 - 2u^8 - 6u^7 - 3u^5 - u^4 + u^3 - 2u^2 - 3 \\ -2u^{12} + 3u^{11} + \cdots - 5u + 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{12} - 2u^{11} + \cdots + 3u - 2 \\ -2u^{12} + 2u^{11} + \cdots - 4u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{12} - 2u^{11} + \cdots + 3u - 2 \\ -2u^{12} + 2u^{11} + \cdots - 4u + 1 \end{pmatrix}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** =  $2u^{10} - 4u^9 + 6u^8 - 8u^7 + 7u^6 - 5u^5 + u^4 + 6u^3 - 3u^2 + 3u - 9$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{13} - u^{12} + \cdots - u + 1$
$c_2$	$u^{13} + 7u^{12} + \cdots - 5u - 1$
$c_3, c_8$	$u^{13} - u^{12} + \cdots + 3u + 1$
$c_4, c_{10}$	$u^{13} + u^{12} + \cdots + 3u - 1$
$c_5$	$u^{13} + u^{12} + \cdots - u - 1$
$c_6$	$u^{13} - u^{12} + \cdots + u - 1$
$c_7$	$u^{13} - 2u^{12} + \cdots + 2u - 1$
$c_9, c_{11}$	$u^{13} + 2u^{12} + \cdots + 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{13} + 7y^{12} + \cdots - 5y - 1$
$c_2$	$y^{13} - y^{12} + \cdots + 7y - 1$
$c_3, c_4, c_8$ $c_{10}$	$y^{13} - 15y^{12} + \cdots - 9y - 1$
$c_6$	$y^{13} - 9y^{12} + \cdots - 11y - 1$
$c_7$	$y^{13} + 2y^{12} + \cdots - 2y - 1$
$c_9, c_{11}$	$y^{13} + 2y^{12} + \cdots - 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.429348 + 0.836369I$		
$a = -1.06443 - 0.95489I$	$1.50284 - 1.80144I$	$-0.975171 + 0.624326I$
$b = 0.90233 + 1.19418I$		
$u = -0.429348 - 0.836369I$		
$a = -1.06443 + 0.95489I$	$1.50284 + 1.80144I$	$-0.975171 - 0.624326I$
$b = 0.90233 - 1.19418I$		
$u = 0.777700 + 0.380482I$		
$a = -0.544452 + 0.841459I$	$-3.52105 - 2.68668I$	$-6.71015 + 2.69355I$
$b = -0.722544 - 0.675961I$		
$u = 0.777700 - 0.380482I$		
$a = -0.544452 - 0.841459I$	$-3.52105 + 2.68668I$	$-6.71015 - 2.69355I$
$b = -0.722544 + 0.675961I$		
$u = -0.851574$		
$a = 1.29542$	$-5.58548$	$-6.40050$
$b = 0.236834$		
$u = 0.354755 + 1.099910I$		
$a = 0.261043 - 1.280070I$	$-7.44002 - 0.06234I$	$-10.48891 - 0.49082I$
$b = 0.463549 + 0.404379I$		
$u = 0.354755 - 1.099910I$		
$a = 0.261043 + 1.280070I$	$-7.44002 + 0.06234I$	$-10.48891 + 0.49082I$
$b = 0.463549 - 0.404379I$		
$u = -0.432945 + 1.190570I$		
$a = 0.574206 + 0.848947I$	$-9.24726 - 4.36417I$	$-9.35230 + 3.32302I$
$b = -0.88235 - 1.94320I$		
$u = -0.432945 - 1.190570I$		
$a = 0.574206 - 0.848947I$	$-9.24726 + 4.36417I$	$-9.35230 - 3.32302I$
$b = -0.88235 + 1.94320I$		
$u = 0.555159 + 1.145130I$		
$a = -1.45591 + 0.17932I$	$-5.89830 + 7.73676I$	$-8.25887 - 7.75024I$
$b = 1.45752 - 1.05620I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.555159 - 1.145130I$	$-5.89830 - 7.73676I$	$-8.25887 + 7.75024I$
$a = -1.45591 - 0.17932I$		
$b = 1.45752 + 1.05620I$		
$u = 0.100465 + 0.707437I$		
$a = 2.08183 + 1.26835I$	$-5.50214 + 2.30256I$	$-8.51436 - 0.38924I$
$b = -1.83693 + 0.64675I$		
$u = 0.100465 - 0.707437I$		
$a = 2.08183 - 1.26835I$	$-5.50214 - 2.30256I$	$-8.51436 + 0.38924I$
$b = -1.83693 - 0.64675I$		

IV.

$$I_4^u = \langle -a^2u^2 + u^2a + \cdots + a + 5, -3a^2u^2 - 3u^2a + \cdots - 4a + 13, u^3 + u + 1 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ -a^3u + a^2u^2 - a^2u - u^2a + a^2 - 4u^2 - a + 2u - 5 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^3u^2 + 2a^2u^2 + a^3 - a^2u - u^2a + 3a^2 - 7u^2 - a + 5u - 11 \\ -a^3u^2 - a^3u - a^2u + au - 2u^2 + u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a^3u + a^3 + u^2a + a^2 + au - u^2 + a + 2u - 2 \\ -2a^3u + a^2u^2 - a^3 - a^2u - 2u^2a - au - 3u^2 - a - 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -a^3u^2 - 3a^2u^2 + \cdots + 3a + 14 \\ -a^3u - a^3 - 2a^2u - 2a^2 - au - 2u + 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^3u^2 + a^2u^2 + a^3 - a^2u - u^2a + 2a^2 + au - 6u^2 - 2a + 4u - 8 \\ a^2u^2 - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^3u^2 + a^2u^2 + a^3 - a^2u - u^2a + 2a^2 + au - 6u^2 - 2a + 4u - 8 \\ a^2u^2 - 2 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4a^3u + 4a^2u^2 - 4a^2u - 4u^2a + 4a^2 - 16u^2 - 4a + 8u - 30$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u^3 + u - 1)^4$
$c_2$	$(u^3 + 2u^2 + u - 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$u^{12} - 6u^{10} + \cdots + 8u + 1$
$c_6$	$(u - 1)^{12}$
$c_7$	$(u^2 + u + 1)^6$
$c_9, c_{11}$	$u^{12} + 4u^{11} + \cdots + 32u + 13$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$(y^3 + 2y^2 + y - 1)^4$
$c_2$	$(y^3 - 2y^2 + 5y - 1)^4$
$c_3, c_4, c_8$ $c_{10}$	$y^{12} - 12y^{11} + \cdots - 36y + 1$
$c_6$	$(y - 1)^{12}$
$c_7$	$(y^2 + y + 1)^6$
$c_9, c_{11}$	$y^{12} + 8y^{11} + \cdots + 848y + 169$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.341164 + 1.161540I$		
$a = -1.034830 + 0.098333I$	$-6.57974 - 2.02988I$	$-8.00000 + 3.46410I$
$b = 0.500000 + 0.866025I$		
$u = 0.341164 + 1.161540I$		
$a = 0.534830 - 0.964359I$	$-6.57974 - 2.02988I$	$-8.00000 + 3.46410I$
$b = 0.500000 + 0.866025I$		
$u = 0.341164 + 1.161540I$		
$a = -0.478220 + 1.030980I$	$-6.57974 + 2.02988I$	$-8.00000 - 3.46410I$
$b = 0.500000 - 0.866025I$		
$u = 0.341164 + 1.161540I$		
$a = -0.021780 - 0.164953I$	$-6.57974 + 2.02988I$	$-8.00000 - 3.46410I$
$b = 0.500000 - 0.866025I$		
$u = 0.341164 - 1.161540I$		
$a = -1.034830 - 0.098333I$	$-6.57974 + 2.02988I$	$-8.00000 - 3.46410I$
$b = 0.500000 - 0.866025I$		
$u = 0.341164 - 1.161540I$		
$a = 0.534830 + 0.964359I$	$-6.57974 + 2.02988I$	$-8.00000 - 3.46410I$
$b = 0.500000 - 0.866025I$		
$u = 0.341164 - 1.161540I$		
$a = -0.478220 - 1.030980I$	$-6.57974 - 2.02988I$	$-8.00000 + 3.46410I$
$b = 0.500000 + 0.866025I$		
$u = -0.682328$		
$a = 1.83446 + 0.06511I$	$-6.57974 - 2.02988I$	$-8.00000 + 3.46410I$
$b = 0.500000 + 0.866025I$		
$u = -0.682328$		
$a = 1.83446 - 0.06511I$	$-6.57974 + 2.02988I$	$-8.00000 - 3.46410I$
$b = 0.500000 - 0.866025I$		

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.682328$		
$a = -2.33446 + 0.93114I$	$-6.57974 + 2.02988I$	$-8.00000 - 3.46410I$
$b = 0.500000 - 0.866025I$		
$u = -0.682328$		
$a = -2.33446 - 0.93114I$	$-6.57974 - 2.02988I$	$-8.00000 + 3.46410I$
$b = 0.500000 + 0.866025I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^3 + u - 1)^4$ $\cdot (u^{10} + u^9 + 3u^8 + 3u^7 + 5u^6 + 5u^5 + 4u^4 + 4u^3 + 3u^2 + 2u + 1)^4$ $\cdot (u^{13} - u^{12} + \dots - u + 1)(u^{28} - 6u^{27} + \dots - 26u + 4)$
$c_2$	$(u^3 + 2u^2 + u - 1)^4$ $\cdot (u^{10} + 5u^9 + 13u^8 + 19u^7 + 17u^6 + 7u^5 - 2u^3 + u^2 + 2u + 1)^4$ $\cdot (u^{13} + 7u^{12} + \dots - 5u - 1)(u^{28} + 14u^{27} + \dots + 36u + 16)$
$c_3, c_8$	$(u^{12} - 6u^{10} + \dots + 8u + 1)(u^{13} - u^{12} + \dots + 3u + 1)$ $\cdot (u^{28} + u^{27} + \dots + 3u + 1)(u^{40} - u^{39} + \dots - 18u^2 + 1)$
$c_4, c_{10}$	$(u^{12} - 6u^{10} + \dots + 8u + 1)(u^{13} + u^{12} + \dots + 3u - 1)$ $\cdot (u^{28} + u^{27} + \dots + 3u + 1)(u^{40} - u^{39} + \dots - 18u^2 + 1)$
$c_5$	$(u^3 + u - 1)^4$ $\cdot (u^{10} + u^9 + 3u^8 + 3u^7 + 5u^6 + 5u^5 + 4u^4 + 4u^3 + 3u^2 + 2u + 1)^4$ $\cdot (u^{13} + u^{12} + \dots - u - 1)(u^{28} - 6u^{27} + \dots - 26u + 4)$
$c_6$	$(u - 1)^{12}$ $\cdot (u^{10} + 2u^9 - u^8 - 5u^7 - 3u^6 + 4u^5 + 12u^4 + 13u^3 + 5u^2 + u + 2)^4$ $\cdot (u^{13} - u^{12} + \dots + u - 1)(u^{28} + 6u^{27} + \dots + 1800u + 712)$
$c_7$	$((u^2 + u + 1)^{26})(u^{13} - 2u^{12} + \dots + 2u - 1)$ $\cdot (u^{28} - 29u^{27} + \dots - 118784u + 8192)$
$c_9, c_{11}$	$(u^{12} + 4u^{11} + \dots + 32u + 13)(u^{13} + 2u^{12} + \dots + 2u + 1)$ $\cdot (u^{28} - 2u^{27} + \dots - 2u + 1)(u^{40} + 11u^{39} + \dots + 644u + 61)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$(y^3 + 2y^2 + y - 1)^4$ $\cdot (y^{10} + 5y^9 + 13y^8 + 19y^7 + 17y^6 + 7y^5 - 2y^3 + y^2 + 2y + 1)^4$ $\cdot (y^{13} + 7y^{12} + \dots - 5y - 1)(y^{28} + 14y^{27} + \dots + 36y + 16)$
$c_2$	$(y^3 - 2y^2 + 5y - 1)^4$ $\cdot (y^{10} + y^9 + 13y^8 + 11y^7 + 45y^6 + 35y^5 + 12y^4 + 2y^3 + 9y^2 - 2y + 1)^4$ $\cdot (y^{13} - y^{12} + \dots + 7y - 1)(y^{28} - 2y^{27} + \dots - 240y + 256)$
$c_3, c_4, c_8$ $c_{10}$	$(y^{12} - 12y^{11} + \dots - 36y + 1)(y^{13} - 15y^{12} + \dots - 9y - 1)$ $\cdot (y^{28} - 23y^{27} + \dots + 3y + 1)(y^{40} - 33y^{39} + \dots - 36y + 1)$
$c_6$	$((y - 1)^{12})(y^{10} - 6y^9 + \dots + 19y + 4)^4(y^{13} - 9y^{12} + \dots - 11y - 1)$ $\cdot (y^{28} - 18y^{27} + \dots + 1943360y + 506944)$
$c_7$	$((y^2 + y + 1)^{26})(y^{13} + 2y^{12} + \dots - 2y - 1)$ $\cdot (y^{28} + 3y^{27} + \dots + 486539264y + 67108864)$
$c_9, c_{11}$	$(y^{12} + 8y^{11} + \dots + 848y + 169)(y^{13} + 2y^{12} + \dots - 2y - 1)$ $\cdot (y^{28} + 6y^{27} + \dots + 40y + 1)(y^{40} + 11y^{39} + \dots + 62528y + 3721)$