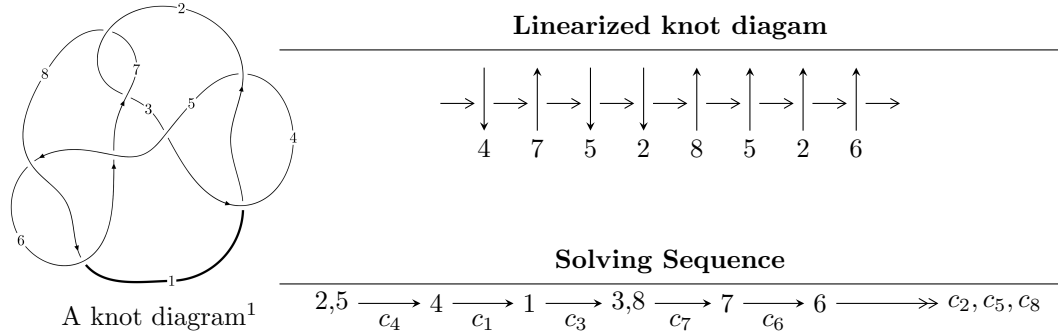


$\delta_{20} (K8n_1)$



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^4 - u^3 - 2u^2 + b + 1, -u^4 + u^3 + 2u^2 + a - 2, u^5 - 2u^4 - 2u^3 + 3u^2 + 3u - 1 \rangle$$

$$I_2^u = \langle b + 1, a, u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 6 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle u^4 - u^3 - 2u^2 + b + 1, -u^4 + u^3 + 2u^2 + a - 2, u^5 - 2u^4 - 2u^3 + 3u^2 + 3u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 - u^3 - 2u^2 + 2 \\ -u^4 + u^3 + 2u^2 - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^4 - u^3 - 2u^2 + 2 \\ u^4 - 2u^2 - 2u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 + 2u + 2 \\ u^4 - 2u^2 - 2u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^4 - 6u^3 - 8u^2 + 6u + 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^5 - 2u^4 - 2u^3 + 3u^2 + 3u - 1$
$c_2, c_7$	$u^5 + u^4 + 5u^3 + u^2 + 2u - 2$
$c_3$	$u^5 + 8u^4 + 22u^3 + 25u^2 + 15u + 1$
$c_5, c_8$	$u^5 + 2u^4 + 2u^3 - u^2 - u - 1$
$c_6$	$u^5 + 6u^3 - u^2 - u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^5 - 8y^4 + 22y^3 - 25y^2 + 15y - 1$
$c_2, c_7$	$y^5 + 9y^4 + 27y^3 + 23y^2 + 8y - 4$
$c_3$	$y^5 - 20y^4 + 114y^3 + 19y^2 + 175y - 1$
$c_5, c_8$	$y^5 + 6y^3 - y^2 - y - 1$
$c_6$	$y^5 + 12y^4 + 34y^3 - 13y^2 - y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.949895 + 0.441667I$		
$a = 0.682871 - 0.618084I$	$-1.85138 + 1.10891I$	$-2.36548 - 2.04112I$
$b = 0.317129 + 0.618084I$		
$u = -0.949895 - 0.441667I$		
$a = 0.682871 + 0.618084I$	$-1.85138 - 1.10891I$	$-2.36548 + 2.04112I$
$b = 0.317129 - 0.618084I$		
$u = 0.274898$		
$a = 1.83380$	$1.20365$	$8.94300$
$b = -0.833800$		
$u = 1.81245 + 0.17314I$		
$a = -0.099771 + 1.129450I$	$-11.90990 - 4.12490I$	$-1.10604 + 2.15443I$
$b = 1.09977 - 1.12945I$		
$u = 1.81245 - 0.17314I$		
$a = -0.099771 - 1.129450I$	$-11.90990 + 4.12490I$	$-1.10604 - 2.15443I$
$b = 1.09977 + 1.12945I$		

$$\text{II. } I_2^u = \langle b + 1, a, u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$u - 1$
$c_2, c_7$	$u$
$c_4, c_5$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_5, c_6, c_8$	$y - 1$
$c_2, c_7$	$y$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 0$	0	0
$b = -1.00000$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)(u^5 - 2u^4 - 2u^3 + 3u^2 + 3u - 1)$
$c_2, c_7$	$u(u^5 + u^4 + 5u^3 + u^2 + 2u - 2)$
$c_3$	$(u - 1)(u^5 + 8u^4 + 22u^3 + 25u^2 + 15u + 1)$
$c_4$	$(u + 1)(u^5 - 2u^4 - 2u^3 + 3u^2 + 3u - 1)$
$c_5$	$(u + 1)(u^5 + 2u^4 + 2u^3 - u^2 - u - 1)$
$c_6$	$(u - 1)(u^5 + 6u^3 - u^2 - u - 1)$
$c_8$	$(u - 1)(u^5 + 2u^4 + 2u^3 - u^2 - u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y - 1)(y^5 - 8y^4 + 22y^3 - 25y^2 + 15y - 1)$
$c_2, c_7$	$y(y^5 + 9y^4 + 27y^3 + 23y^2 + 8y - 4)$
$c_3$	$(y - 1)(y^5 - 20y^4 + 114y^3 + 19y^2 + 175y - 1)$
$c_5, c_8$	$(y - 1)(y^5 + 6y^3 - y^2 - y - 1)$
$c_6$	$(y - 1)(y^5 + 12y^4 + 34y^3 - 13y^2 - y - 1)$