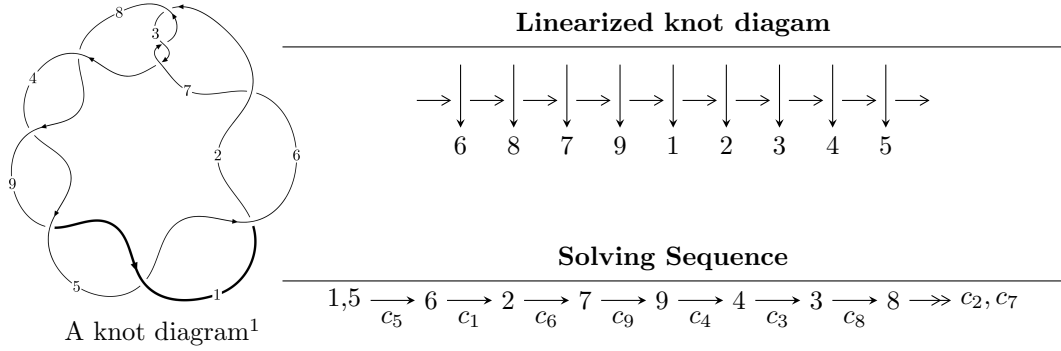


$\mathcal{G}_3 (K9a_{38})$



A knot diagram<sup>1</sup>

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^9 - u^8 - 6u^7 + 5u^6 + 11u^5 - 7u^4 - 6u^3 + 4u^2 - u - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 9 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^9 - u^8 - 6u^7 + 5u^6 + 11u^5 - 7u^4 - 6u^3 + 4u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^8 - 5u^6 + 7u^4 - 4u^2 + 1 \\ u^8 + u^7 - 5u^6 - 4u^5 + 7u^4 + 2u^3 - 4u^2 + 2u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^5 - 16u^3 + 12u - 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_9$	$u^9 - u^8 - 6u^7 + 5u^6 + 11u^5 - 7u^4 - 6u^3 + 4u^2 - u - 1$
$c_2, c_3, c_7$	$u^9 + u^8 + 4u^7 + 3u^6 + 5u^5 + 3u^4 - 3u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_9$	$y^9 - 13y^8 + 68y^7 - 183y^6 + 269y^5 - 211y^4 + 80y^3 - 18y^2 + 9y - 1$
$c_2, c_3, c_7$	$y^9 + 7y^8 + 20y^7 + 25y^6 + y^5 - 31y^4 - 24y^3 + 6y^2 + 9y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.115700 + 0.218357I$	$-1.75807 + 3.86354I$	$-12.03791 - 4.00946I$
$u = -1.115700 - 0.218357I$	$-1.75807 - 3.86354I$	$-12.03791 + 4.00946I$
$u = 1.15527$	$-5.50120$	$-16.5750$
$u = 0.344156 + 0.466288I$	$2.84789 - 1.55423I$	$-6.94040 + 4.30527I$
$u = 0.344156 - 0.466288I$	$2.84789 + 1.55423I$	$-6.94040 - 4.30527I$
$u = -0.362481$	$-0.561234$	$-17.6130$
$u = 1.76115 + 0.05266I$	$-12.16890 - 4.99486I$	$-12.86627 + 2.90812I$
$u = 1.76115 - 0.05266I$	$-12.16890 + 4.99486I$	$-12.86627 - 2.90812I$
$u = -1.77199$	$-16.1927$	$-16.1230$

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_9$	$u^9 - u^8 - 6u^7 + 5u^6 + 11u^5 - 7u^4 - 6u^3 + 4u^2 - u - 1$
$c_2, c_3, c_7$	$u^9 + u^8 + 4u^7 + 3u^6 + 5u^5 + 3u^4 - 3u - 1$

### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_9$	$y^9 - 13y^8 + 68y^7 - 183y^6 + 269y^5 - 211y^4 + 80y^3 - 18y^2 + 9y - 1$
$c_2, c_3, c_7$	$y^9 + 7y^8 + 20y^7 + 25y^6 + y^5 - 31y^4 - 24y^3 + 6y^2 + 9y - 1$