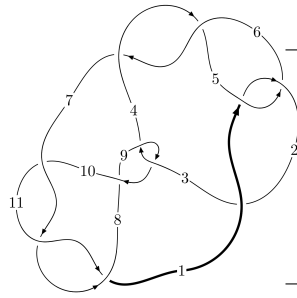
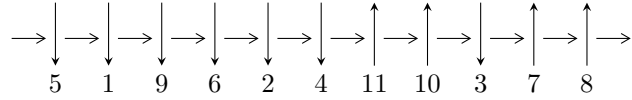


11a<sub>153</sub> (K11a<sub>153</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$1,5 \xrightarrow{c_1} 2 \xrightarrow{c_2} 3 \xrightarrow{c_5} 6,9 \xrightarrow{c_9} 10 \xrightarrow{c_4} 4 \xrightarrow{c_6} 7 \xrightarrow{c_8} 8 \xrightarrow{c_{11}} 11 \rightsquigarrow c_3, c_7, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^{45} + u^{44} + \dots + 5u^4 + b, -u^{43} + 6u^{41} + \dots - 5u^3 + a, u^{47} - 2u^{46} + \dots + 2u^2 - 1 \rangle$$

$$I_2^u = \langle b - 1, a - u, u^3 + u^2 - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 50 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -u^{45} + u^{44} + \dots + 5u^4 + b, -u^{43} + 6u^{41} + \dots - 5u^3 + a, u^{47} - 2u^{46} + \dots + 2u^2 - 1 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{43} - 6u^{41} + \dots - 4u^5 + 5u^3 \\ u^{45} - u^{44} + \dots + 5u^5 - 5u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u^{46} - 2u^{45} + \dots - u + 1 \\ -u^{46} + u^{45} + \dots + u^2 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^5 - u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{44} + u^{43} + \dots + 5u^3 - u^2 \\ -u^{46} + u^{45} + \dots - 9u^4 + u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{46} - u^{45} + \dots - u + 1 \\ -u^{46} + u^{45} + \dots + u^2 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{46} - u^{45} + \dots - u + 1 \\ -u^{46} + u^{45} + \dots + u^2 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-u^{46} + 2u^{45} + \dots - 11u - 3$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{47} + 2u^{46} + \dots - 2u^2 + 1$
$c_2, c_4, c_6$	$u^{47} + 12u^{46} + \dots + 4u + 1$
$c_3, c_9$	$u^{47} + u^{46} + \dots + 28u + 8$
$c_7, c_{10}, c_{11}$	$u^{47} + 4u^{46} + \dots + 5u + 1$
$c_8$	$u^{47} - 21u^{46} + \dots - 112u + 64$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{47} - 12y^{46} + \dots + 4y - 1$
$c_2, c_4, c_6$	$y^{47} + 48y^{46} + \dots - 20y - 1$
$c_3, c_9$	$y^{47} + 21y^{46} + \dots - 112y - 64$
$c_7, c_{10}, c_{11}$	$y^{47} - 42y^{46} + \dots + 53y - 1$
$c_8$	$y^{47} + 5y^{46} + \dots + 249088y - 4096$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.951038 + 0.332468I$ $a = -0.548939 - 0.454811I$ $b = -1.39671 - 0.26399I$	$-2.29859 + 5.08605I$	$-6.19055 - 7.78708I$
$u = -0.951038 - 0.332468I$ $a = -0.548939 + 0.454811I$ $b = -1.39671 + 0.26399I$	$-2.29859 - 5.08605I$	$-6.19055 + 7.78708I$
$u = 1.011380 + 0.139586I$ $a = 0.187121 - 1.081320I$ $b = 0.152878 + 0.035343I$	$1.25225 + 2.83779I$	$-2.68977 - 2.39473I$
$u = 1.011380 - 0.139586I$ $a = 0.187121 + 1.081320I$ $b = 0.152878 - 0.035343I$	$1.25225 - 2.83779I$	$-2.68977 + 2.39473I$
$u = 0.896160 + 0.336643I$ $a = 0.608816 - 1.251080I$ $b = 0.208048 + 0.420593I$	$0.73808 - 3.39872I$	$-3.20420 + 5.17325I$
$u = 0.896160 - 0.336643I$ $a = 0.608816 + 1.251080I$ $b = 0.208048 - 0.420593I$	$0.73808 + 3.39872I$	$-3.20420 - 5.17325I$
$u = 0.929490 + 0.212978I$ $a = -0.382863 + 1.063800I$ $b = -0.152157 - 0.188016I$	$-2.99267 - 0.24824I$	$-9.15885 + 0.73721I$
$u = 0.929490 - 0.212978I$ $a = -0.382863 - 1.063800I$ $b = -0.152157 + 0.188016I$	$-2.99267 + 0.24824I$	$-9.15885 - 0.73721I$
$u = -1.006120 + 0.373819I$ $a = 0.507879 + 0.365560I$ $b = 1.365760 + 0.114872I$	$2.62432 + 8.92326I$	$-1.23068 - 8.39839I$
$u = -1.006120 - 0.373819I$ $a = 0.507879 - 0.365560I$ $b = 1.365760 - 0.114872I$	$2.62432 - 8.92326I$	$-1.23068 + 8.39839I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.586342 + 0.704775I$ $a = 0.286240 - 0.496512I$ $b = -0.636220 - 0.653509I$	$6.94014 + 2.76747I$	$5.54266 - 3.60808I$
$u = -0.586342 - 0.704775I$ $a = 0.286240 + 0.496512I$ $b = -0.636220 + 0.653509I$	$6.94014 - 2.76747I$	$5.54266 + 3.60808I$
$u = -0.844254 + 0.267575I$ $a = 0.624042 + 0.701381I$ $b = 1.43152 + 0.59292I$	$0.239586 + 1.107160I$	$-2.87652 - 5.48870I$
$u = -0.844254 - 0.267575I$ $a = 0.624042 - 0.701381I$ $b = 1.43152 - 0.59292I$	$0.239586 - 1.107160I$	$-2.87652 + 5.48870I$
$u = -0.946938 + 0.664626I$ $a = -0.210609 - 0.192004I$ $b = -0.664543 + 0.135905I$	$5.98354 + 2.31808I$	$4.28165 - 1.64217I$
$u = -0.946938 - 0.664626I$ $a = -0.210609 + 0.192004I$ $b = -0.664543 - 0.135905I$	$5.98354 - 2.31808I$	$4.28165 + 1.64217I$
$u = -0.842514 + 0.793044I$ $a = -0.169363 + 0.125945I$ $b = 0.111786 + 0.476934I$	$3.10025 + 1.81367I$	$-3.66686 - 2.05384I$
$u = -0.842514 - 0.793044I$ $a = -0.169363 - 0.125945I$ $b = 0.111786 - 0.476934I$	$3.10025 - 1.81367I$	$-3.66686 + 2.05384I$
$u = 0.827943 + 0.860184I$ $a = 2.70969 + 0.79407I$ $b = -2.83895 + 0.82810I$	$5.30471 + 2.88795I$	$0.68944 - 2.66752I$
$u = 0.827943 - 0.860184I$ $a = 2.70969 - 0.79407I$ $b = -2.83895 - 0.82810I$	$5.30471 - 2.88795I$	$0.68944 + 2.66752I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.847216 + 0.855752I$ $a = 0.256476 - 0.116248I$ $b = -0.054478 - 0.688171I$	$8.19027 - 0.67694I$	$2.91715 + 0.I$
$u = -0.847216 - 0.855752I$ $a = 0.256476 + 0.116248I$ $b = -0.054478 + 0.688171I$	$8.19027 + 0.67694I$	$2.91715 + 0.I$
$u = 0.863506 + 0.840738I$ $a = -2.93690 - 1.29712I$ $b = 3.21491 - 0.72537I$	$7.05051 - 2.00460I$	$3.77294 + 2.26192I$
$u = 0.863506 - 0.840738I$ $a = -2.93690 + 1.29712I$ $b = 3.21491 + 0.72537I$	$7.05051 + 2.00460I$	$3.77294 - 2.26192I$
$u = 0.815670 + 0.889580I$ $a = -2.42001 - 0.70946I$ $b = 2.67739 - 0.69105I$	$10.89330 + 7.08520I$	$3.93867 - 3.32748I$
$u = 0.815670 - 0.889580I$ $a = -2.42001 + 0.70946I$ $b = 2.67739 + 0.69105I$	$10.89330 - 7.08520I$	$3.93867 + 3.32748I$
$u = -0.930838 + 0.775441I$ $a = 0.203539 + 0.027785I$ $b = 0.305087 - 0.418436I$	$2.82936 + 4.09126I$	$-3.95731 - 3.33683I$
$u = -0.930838 - 0.775441I$ $a = 0.203539 - 0.027785I$ $b = 0.305087 + 0.418436I$	$2.82936 - 4.09126I$	$-3.95731 + 3.33683I$
$u = 0.935935 + 0.814528I$ $a = -2.21964 - 2.45540I$ $b = 3.34946 + 0.19998I$	$6.82306 - 4.16721I$	$3.15551 + 3.14334I$
$u = 0.935935 - 0.814528I$ $a = -2.21964 + 2.45540I$ $b = 3.34946 - 0.19998I$	$6.82306 + 4.16721I$	$3.15551 - 3.14334I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.953997 + 0.816453I$ $a = -0.258063 - 0.008399I$ $b = -0.328975 + 0.602645I$	$7.85574 + 6.89913I$	$0. - 4.81630I$
$u = -0.953997 - 0.816453I$ $a = -0.258063 + 0.008399I$ $b = -0.328975 - 0.602645I$	$7.85574 - 6.89913I$	$0. + 4.81630I$
$u = 0.967508 + 0.809416I$ $a = 1.72066 + 2.45725I$ $b = -3.04108 - 0.38491I$	$4.86878 - 9.09918I$	$0. + 7.51593I$
$u = 0.967508 - 0.809416I$ $a = 1.72066 - 2.45725I$ $b = -3.04108 + 0.38491I$	$4.86878 + 9.09918I$	$0. - 7.51593I$
$u = 0.917330 + 0.873542I$ $a = 2.18776 + 1.62070I$ $b = -3.01700 + 0.23550I$	$15.4002 - 3.2295I$	$6.21908 + 0.I$
$u = 0.917330 - 0.873542I$ $a = 2.18776 - 1.62070I$ $b = -3.01700 - 0.23550I$	$15.4002 + 3.2295I$	$6.21908 + 0.I$
$u = -0.194123 + 0.690391I$ $a = -0.768909 + 0.672272I$ $b = 0.832582 + 0.572354I$	$5.21653 - 5.13195I$	$4.47363 + 3.77222I$
$u = -0.194123 - 0.690391I$ $a = -0.768909 - 0.672272I$ $b = 0.832582 - 0.572354I$	$5.21653 + 5.13195I$	$4.47363 - 3.77222I$
$u = 0.989025 + 0.818280I$ $a = -1.52457 - 2.27011I$ $b = 2.85418 + 0.32452I$	$10.3470 - 13.4113I$	$0. + 8.12644I$
$u = 0.989025 - 0.818280I$ $a = -1.52457 + 2.27011I$ $b = 2.85418 - 0.32452I$	$10.3470 + 13.4113I$	$0. - 8.12644I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.682080$ $a = 0.611660$ $b = -0.132637$	-0.926103	-11.4570
$u = -0.525813 + 0.373412I$ $a = -0.094058 + 1.038330I$ $b = 0.733120 + 0.760322I$	$1.13890 + 1.31315I$	$3.11319 - 5.85317I$
$u = -0.525813 - 0.373412I$ $a = -0.094058 - 1.038330I$ $b = 0.733120 - 0.760322I$	$1.13890 - 1.31315I$	$3.11319 + 5.85317I$
$u = -0.160803 + 0.538431I$ $a = 0.823656 - 0.894795I$ $b = -0.721771 - 0.493724I$	$0.05463 - 1.88803I$	$0.05102 + 3.76347I$
$u = -0.160803 - 0.538431I$ $a = 0.823656 + 0.894795I$ $b = -0.721771 + 0.493724I$	$0.05463 + 1.88803I$	$0.05102 - 3.76347I$
$u = 0.295011 + 0.434696I$ $a = -1.38778 + 0.73289I$ $b = 0.681477 - 0.043588I$	$2.53395 + 0.36100I$	$2.22031 + 1.00355I$
$u = 0.295011 - 0.434696I$ $a = -1.38778 - 0.73289I$ $b = 0.681477 + 0.043588I$	$2.53395 - 0.36100I$	$2.22031 - 1.00355I$

$$\text{II. } I_2^u = \langle b - 1, a - u, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u + 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u + 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $2u^2 - u - 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^3 + u^2 - 1$
$c_2, c_6$	$u^3 + u^2 + 2u + 1$
$c_3, c_8, c_9$	$u^3$
$c_4$	$u^3 - u^2 + 2u - 1$
$c_5$	$u^3 - u^2 + 1$
$c_7$	$(u + 1)^3$
$c_{10}, c_{11}$	$(u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^3 - y^2 + 2y - 1$
$c_2, c_4, c_6$	$y^3 + 3y^2 + 2y - 1$
$c_3, c_8, c_9$	$y^3$
$c_7, c_{10}, c_{11}$	$(y - 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$ $a = -0.877439 + 0.744862I$ $b = 1.00000$	$4.66906 + 2.82812I$	$-0.69240 - 3.35914I$
$u = -0.877439 - 0.744862I$ $a = -0.877439 - 0.744862I$ $b = 1.00000$	$4.66906 - 2.82812I$	$-0.69240 + 3.35914I$
$u = 0.754878$ $a = 0.754878$ $b = 1.00000$	$0.531480$	$-1.61520$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^3 + u^2 - 1)(u^{47} + 2u^{46} + \dots - 2u^2 + 1)$
$c_2, c_6$	$(u^3 + u^2 + 2u + 1)(u^{47} + 12u^{46} + \dots + 4u + 1)$
$c_3, c_9$	$u^3(u^{47} + u^{46} + \dots + 28u + 8)$
$c_4$	$(u^3 - u^2 + 2u - 1)(u^{47} + 12u^{46} + \dots + 4u + 1)$
$c_5$	$(u^3 - u^2 + 1)(u^{47} + 2u^{46} + \dots - 2u^2 + 1)$
$c_7$	$((u + 1)^3)(u^{47} + 4u^{46} + \dots + 5u + 1)$
$c_8$	$u^3(u^{47} - 21u^{46} + \dots - 112u + 64)$
$c_{10}, c_{11}$	$((u - 1)^3)(u^{47} + 4u^{46} + \dots + 5u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$(y^3 - y^2 + 2y - 1)(y^{47} - 12y^{46} + \dots + 4y - 1)$
$c_2, c_4, c_6$	$(y^3 + 3y^2 + 2y - 1)(y^{47} + 48y^{46} + \dots - 20y - 1)$
$c_3, c_9$	$y^3(y^{47} + 21y^{46} + \dots - 112y - 64)$
$c_7, c_{10}, c_{11}$	$((y - 1)^3)(y^{47} - 42y^{46} + \dots + 53y - 1)$
$c_8$	$y^3(y^{47} + 5y^{46} + \dots + 249088y - 4096)$