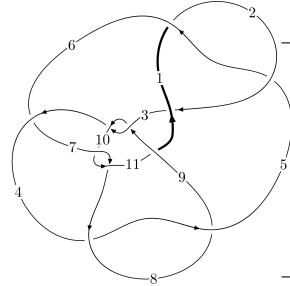
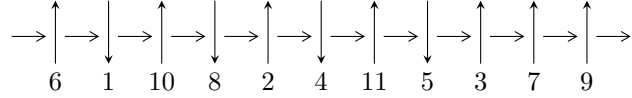


11a<sub>157</sub> (K11a<sub>157</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,5 \xrightarrow{c_5} 6 \xrightarrow{c_1} 1 \xrightarrow{c_2} 3,9 \xrightarrow{c_9} 10 \xrightarrow{c_8} 8 \xrightarrow{c_4} 4 \xrightarrow{c_{11}} 11 \xrightarrow{c_7} 7 \longrightarrow c_3, c_6, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -116u^{51} - 310u^{50} + \dots + 2304b + 7136, -3775u^{52} - 16066u^{51} + \dots + 52992a + 229724, u^{53} + 4u^{52} + \dots - 92u - 46 \rangle$$

$$I_2^u = \langle -a^2u + 2b + a - 2, a^3 + 2a^2u - au + 2a + 2, u^2 - u + 1 \rangle$$

$$I_3^u = \langle b + 1, 6a + u + 4, u^2 + 2 \rangle$$

$$I_4^u = \langle b^2au + b^3 - bu - au - b + u - 1, u^2 - u + 1 \rangle$$

$$I_1^v = \langle a, b^3 - b - 1, v - 1 \rangle$$

$$I_2^v = \langle a, b - 1, v - 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 65 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -116u^{51} - 310u^{50} + \dots + 2304b + 7136, -3775u^{52} - 16066u^{51} + \dots + 52992a + 229724, u^{53} + 4u^{52} + \dots - 92u - 46 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.0712372u^{52} + 0.303178u^{51} + \dots - 8.73049u - 4.33507 \\ 0.0503472u^{51} + 0.134549u^{50} + \dots - 1.31510u - 3.09722 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.184518u^{52} + 0.705088u^{51} + \dots - 14.9597u - 6.29167 \\ 0.0625000u^{52} + 0.159722u^{51} + \dots - 1.55729u - 1.65972 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0712372u^{52} + 0.353525u^{51} + \dots - 10.0456u - 7.43229 \\ 0.0503472u^{51} + 0.134549u^{50} + \dots - 1.31510u - 3.09722 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.119226u^{52} + 0.443048u^{51} + \dots - 9.10745u - 4.01302 \\ 0.00520833u^{52} - 0.0195313u^{51} + \dots + 1.50521u + 0.684896 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0306839u^{52} - 0.0914855u^{51} + \dots + 4.15433u + 4.34635 \\ 0.109375u^{52} + 0.342448u^{51} + \dots - 4.84375u - 0.565104 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0805405u^{52} - 0.300460u^{51} + \dots + 7.03842u + 4.68750 \\ -0.0625000u^{52} - 0.165799u^{51} + \dots + 0.802083u + 1.18924 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0805405u^{52} - 0.300460u^{51} + \dots + 7.03842u + 4.68750 \\ -0.0625000u^{52} - 0.165799u^{51} + \dots + 0.802083u + 1.18924 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{1153}{1728}u^{52} + \frac{1951}{864}u^{51} + \dots - \frac{7271}{216}u + \frac{1}{4}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{53} + 4u^{52} + \dots - 92u - 46$
$c_2$	$u^{53} + 24u^{52} + \dots + 3496u - 2116$
$c_3, c_9$	$9(9u^{53} - 18u^{52} + \dots - 77u - 19)$
$c_4, c_8$	$9(9u^{53} + 18u^{52} + \dots - 9u - 19)$
$c_6$	$16(16u^{53} - 16u^{52} + \dots + 103779u - 3609)$
$c_7, c_{10}$	$u^{53} + 6u^{52} + \dots - 5832u - 1706$
$c_{11}$	$16(16u^{53} + 32u^{52} + \dots - 16641u - 6003)$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{53} + 24y^{52} + \dots + 3496y - 2116$
$c_2$	$y^{53} + 12y^{52} + \dots + 393508288y - 4477456$
$c_3, c_9$	$81(81y^{53} - 3510y^{52} + \dots + 3421y - 361)$
$c_4, c_8$	$81(81y^{53} - 2214y^{52} + \dots + 7149y - 361)$
$c_6$	$256(256y^{53} + 6016y^{52} + \dots + 9.94255 \times 10^9y - 1.30249 \times 10^7)$
$c_7, c_{10}$	$y^{53} - 30y^{52} + \dots - 5573800y - 2910436$
$c_{11}$	$256(256y^{53} - 6528y^{52} + \dots - 3.68087 \times 10^8y - 3.60360 \times 10^7)$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.809668 + 0.591571I$ $a = -0.38862 + 1.53061I$ $b = -0.262654 - 1.151540I$	$9.44289 + 4.62072I$	$10.24286 - 2.08237I$
$u = -0.809668 - 0.591571I$ $a = -0.38862 - 1.53061I$ $b = -0.262654 + 1.151540I$	$9.44289 - 4.62072I$	$10.24286 + 2.08237I$
$u = 0.932904 + 0.475451I$ $a = 0.719049 + 0.844934I$ $b = -1.26960 - 0.64309I$	$6.27152 - 10.90750I$	$7.14898 + 5.53843I$
$u = 0.932904 - 0.475451I$ $a = 0.719049 - 0.844934I$ $b = -1.26960 + 0.64309I$	$6.27152 + 10.90750I$	$7.14898 - 5.53843I$
$u = 0.880838 + 0.326928I$ $a = -0.164167 + 0.799269I$ $b = -0.573186 - 0.653434I$	$7.95194 + 1.12051I$	$10.90095 + 0.04798I$
$u = 0.880838 - 0.326928I$ $a = -0.164167 - 0.799269I$ $b = -0.573186 + 0.653434I$	$7.95194 - 1.12051I$	$10.90095 - 0.04798I$
$u = -0.817792 + 0.679811I$ $a = 0.418946 - 0.981125I$ $b = 0.303446 + 0.604240I$	$4.38963 + 0.38285I$	$8.33080 + 0.50210I$
$u = -0.817792 - 0.679811I$ $a = 0.418946 + 0.981125I$ $b = 0.303446 - 0.604240I$	$4.38963 - 0.38285I$	$8.33080 - 0.50210I$
$u = 0.994126 + 0.446360I$ $a = -0.477878 - 0.579642I$ $b = 1.071810 + 0.473560I$	$2.22320 - 4.60694I$	$5.52820 + 4.35998I$
$u = 0.994126 - 0.446360I$ $a = -0.477878 + 0.579642I$ $b = 1.071810 - 0.473560I$	$2.22320 + 4.60694I$	$5.52820 - 4.35998I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.611609 + 0.908410I$ $a = -1.30709 + 0.63481I$ $b = 0.809891 + 0.174593I$	$0.872134 + 1.079720I$	$0. + 2.41019I$
$u = 0.611609 - 0.908410I$ $a = -1.30709 - 0.63481I$ $b = 0.809891 - 0.174593I$	$0.872134 - 1.079720I$	$0. - 2.41019I$
$u = 0.170302 + 1.087830I$ $a = 0.635126 + 0.069933I$ $b = 0.001690 + 0.649953I$	$3.08054 + 4.00121I$	$5.97068 - 4.06106I$
$u = 0.170302 - 1.087830I$ $a = 0.635126 - 0.069933I$ $b = 0.001690 - 0.649953I$	$3.08054 - 4.00121I$	$5.97068 + 4.06106I$
$u = 0.626566 + 0.643943I$ $a = 1.22653 - 0.71815I$ $b = -0.826327 + 0.364980I$	$1.59094 + 3.76796I$	$4.39825 - 7.64009I$
$u = 0.626566 - 0.643943I$ $a = 1.22653 + 0.71815I$ $b = -0.826327 - 0.364980I$	$1.59094 - 3.76796I$	$4.39825 + 7.64009I$
$u = -0.128610 + 1.112310I$ $a = 0.653956 - 0.300609I$ $b = 1.275160 - 0.403466I$	$-4.15345 + 3.73758I$	$-2.48655 - 3.09856I$
$u = -0.128610 - 1.112310I$ $a = 0.653956 + 0.300609I$ $b = 1.275160 + 0.403466I$	$-4.15345 - 3.73758I$	$-2.48655 + 3.09856I$
$u = -0.949759 + 0.608985I$ $a = 0.264387 + 0.875055I$ $b = -0.908688 - 0.564102I$	$6.99581 - 5.82913I$	$8.82739 + 6.38685I$
$u = -0.949759 - 0.608985I$ $a = 0.264387 - 0.875055I$ $b = -0.908688 + 0.564102I$	$6.99581 + 5.82913I$	$8.82739 - 6.38685I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.496009 + 1.017750I$ $a = 1.36846 - 1.83838I$ $b = 0.878140 + 0.204929I$	$0.67079 - 3.09135I$	$0. + 5.67301I$
$u = -0.496009 - 1.017750I$ $a = 1.36846 + 1.83838I$ $b = 0.878140 - 0.204929I$	$0.67079 + 3.09135I$	$0. - 5.67301I$
$u = -0.724250 + 0.436534I$ $a = 1.15534 - 0.92210I$ $b = -1.151270 + 0.693551I$	$0.72806 + 5.75739I$	$4.99130 - 5.10418I$
$u = -0.724250 - 0.436534I$ $a = 1.15534 + 0.92210I$ $b = -1.151270 - 0.693551I$	$0.72806 - 5.75739I$	$4.99130 + 5.10418I$
$u = -0.434366 + 0.666743I$ $a = 0.33515 - 2.08440I$ $b = -0.607875 + 0.260312I$	$1.88416 - 0.85038I$	$6.25673 - 3.20224I$
$u = -0.434366 - 0.666743I$ $a = 0.33515 + 2.08440I$ $b = -0.607875 - 0.260312I$	$1.88416 + 0.85038I$	$6.25673 + 3.20224I$
$u = -0.212305 + 1.189430I$ $a = -0.778145 + 0.361047I$ $b = -1.237090 + 0.111866I$	$-6.51253 - 1.42478I$	$0$
$u = -0.212305 - 1.189430I$ $a = -0.778145 - 0.361047I$ $b = -1.237090 - 0.111866I$	$-6.51253 + 1.42478I$	$0$
$u = -0.686889 + 1.004730I$ $a = 0.343976 - 0.826525I$ $b = -0.085142 + 0.784336I$	$3.37147 - 6.01200I$	$0$
$u = -0.686889 - 1.004730I$ $a = 0.343976 + 0.826525I$ $b = -0.085142 - 0.784336I$	$3.37147 + 6.01200I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.572191 + 1.085580I$ $a = -0.52093 + 1.70529I$ $b = -1.240970 - 0.438253I$	$-4.09769 - 6.18849I$	0
$u = -0.572191 - 1.085580I$ $a = -0.52093 - 1.70529I$ $b = -1.240970 + 0.438253I$	$-4.09769 + 6.18849I$	0
$u = -0.601851 + 1.072670I$ $a = 0.51488 - 1.93050I$ $b = 1.31349 + 0.76096I$	$-1.10548 - 10.82140I$	0
$u = -0.601851 - 1.072670I$ $a = 0.51488 + 1.93050I$ $b = 1.31349 - 0.76096I$	$-1.10548 + 10.82140I$	0
$u = 0.055611 + 0.764069I$ $a = -0.284386 + 0.734524I$ $b = 0.575442 - 0.355913I$	$-1.00556 + 1.44727I$	$-1.64819 - 5.47738I$
$u = 0.055611 - 0.764069I$ $a = -0.284386 - 0.734524I$ $b = 0.575442 + 0.355913I$	$-1.00556 - 1.44727I$	$-1.64819 + 5.47738I$
$u = -0.673460 + 1.041740I$ $a = -0.955719 + 0.894786I$ $b = 0.132760 - 1.273430I$	$8.08301 - 10.18320I$	0
$u = -0.673460 - 1.041740I$ $a = -0.955719 - 0.894786I$ $b = 0.132760 + 1.273430I$	$8.08301 + 10.18320I$	0
$u = -0.681987 + 0.321709I$ $a = -0.724827 + 0.615572I$ $b = 1.078220 - 0.328843I$	$-1.99983 + 1.37832I$	$-0.467710 - 0.890691I$
$u = -0.681987 - 0.321709I$ $a = -0.724827 - 0.615572I$ $b = 1.078220 + 0.328843I$	$-1.99983 - 1.37832I$	$-0.467710 + 0.890691I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.780684 + 1.053130I$		
$a = -0.293135 - 0.040674I$	$5.65031 - 0.44478I$	0
$b = 0.683599 - 0.489569I$		
$u = -0.780684 - 1.053130I$		
$a = -0.293135 + 0.040674I$	$5.65031 + 0.44478I$	0
$b = 0.683599 + 0.489569I$		
$u = 0.013214 + 1.311610I$		
$a = 0.807998 - 0.074133I$	$-0.35444 - 8.20749I$	0
$b = 1.204730 + 0.451072I$		
$u = 0.013214 - 1.311610I$		
$a = 0.807998 + 0.074133I$	$-0.35444 + 8.20749I$	0
$b = 1.204730 - 0.451072I$		
$u = 0.680239 + 1.136940I$		
$a = 0.55415 + 1.83786I$	$4.2476 + 16.8128I$	0
$b = 1.35544 - 0.64421I$		
$u = 0.680239 - 1.136940I$		
$a = 0.55415 - 1.83786I$	$4.2476 - 16.8128I$	0
$b = 1.35544 + 0.64421I$		
$u = 0.695044 + 1.161580I$		
$a = -0.43161 - 1.48086I$	$0.03277 + 10.71240I$	0
$b = -1.215140 + 0.489831I$		
$u = 0.695044 - 1.161580I$		
$a = -0.43161 + 1.48086I$	$0.03277 - 10.71240I$	0
$b = -1.215140 - 0.489831I$		
$u = 0.621820 + 1.215440I$		
$a = 0.821143 + 0.925875I$	$5.26202 + 4.45797I$	0
$b = 0.823061 - 0.470093I$		
$u = 0.621820 - 1.215440I$		
$a = 0.821143 - 0.925875I$	$5.26202 - 4.45797I$	0
$b = 0.823061 + 0.470093I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.12822 + 1.49963I$ $a = -0.590311 - 0.032839I$ $b = -0.946332 - 0.195707I$	$-4.67412 - 0.82373I$	0
$u = 0.12822 - 1.49963I$ $a = -0.590311 + 0.032839I$ $b = -0.946332 + 0.195707I$	$-4.67412 + 0.82373I$	0
$u = 0.318662$ $a = 2.19545$ $b = -0.365228$	1.00464	11.4100

$$\text{II. } I_2^u = \langle -a^2u + 2b + a - 2, a^3 + 2a^2u - au + 2a + 2, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ \frac{1}{2}a^2u - \frac{1}{2}a + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}a^2u + \frac{1}{2}a + 1 \\ \frac{1}{2}a^2u - \frac{1}{2}a + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{2}a^2u + \frac{1}{2}a + 1 \\ \frac{1}{2}a^2u - \frac{1}{2}a + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{2}a^2u + \frac{1}{2}a + 1 \\ -\frac{1}{2}a^2u + \frac{1}{2}a^2 - \frac{1}{2}au + a - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{2}a^2u - \frac{1}{2}a - 1 \\ -\frac{1}{2}a^2u + \frac{1}{2}a - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{2}a^2u + \frac{1}{2}a + 1 \\ \frac{1}{2}a^2u - \frac{1}{2}a + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{2}a^2u + \frac{1}{2}a + 1 \\ \frac{1}{2}a^2u - \frac{1}{2}a + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u^2 - u + 1)^3$
$c_2$	$(u^2 + u + 1)^3$
$c_3, c_4, c_6$ $c_8, c_9$	$u^6 - 2u^4 - u^3 + u^2 + u + 1$
$c_7, c_{10}$	$u^6$
$c_{11}$	$u^6 - 4u^5 + 6u^4 - 3u^3 - u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y^2 + y + 1)^3$
$c_3, c_4, c_6$ $c_8, c_9$	$y^6 - 4y^5 + 6y^4 - 3y^3 - y^2 + y + 1$
$c_7, c_{10}$	$y^6$
$c_{11}$	$y^6 - 4y^5 + 10y^4 - 11y^3 + 19y^2 - 3y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = 0.412728 + 1.011420I$ $b = 0.218964 - 0.666188I$	2.02988I	0. - 3.46410I
$u = 0.500000 + 0.866025I$ $a = -0.562490 - 0.528127I$ $b = 1.033350 + 0.428825I$	2.02988I	0. - 3.46410I
$u = 0.500000 + 0.866025I$ $a = -0.85024 - 2.21534I$ $b = -1.252310 + 0.237364I$	2.02988I	0. - 3.46410I
$u = 0.500000 - 0.866025I$ $a = 0.412728 - 1.011420I$ $b = 0.218964 + 0.666188I$	- 2.02988I	0. + 3.46410I
$u = 0.500000 - 0.866025I$ $a = -0.562490 + 0.528127I$ $b = 1.033350 - 0.428825I$	- 2.02988I	0. + 3.46410I
$u = 0.500000 - 0.866025I$ $a = -0.85024 + 2.21534I$ $b = -1.252310 - 0.237364I$	- 2.02988I	0. + 3.46410I

$$\text{III. } I_3^u = \langle b + 1, 6a + u + 4, u^2 + 2 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u \\ 3u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{6}u - \frac{2}{3} \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{13}{6}u - \frac{2}{3} \\ -3u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{6}u - \frac{5}{3} \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{6}u - \frac{2}{3} \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{23}{18}u - \frac{1}{9} \\ -\frac{4}{3}u - \frac{1}{3} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{5}{18}u + \frac{8}{9} \\ -\frac{1}{3}u + \frac{5}{3} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{5}{18}u + \frac{8}{9} \\ -\frac{1}{3}u + \frac{5}{3} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_7$ $c_{10}$	$u^2 + 2$
$c_2$	$(u + 2)^2$
$c_3, c_4$	$(u + 1)^2$
$c_6, c_{11}$	$3(3u^2 - 2u + 1)$
$c_8, c_9$	$(u - 1)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_7$ $c_{10}$	$(y + 2)^2$
$c_2$	$(y - 4)^2$
$c_3, c_4, c_8$ $c_9$	$(y - 1)^2$
$c_6, c_{11}$	$9(9y^2 + 2y + 1)$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.414210I$ $a = -0.666667 - 0.235702I$ $b = -1.00000$	-4.93480	0
$u = -1.414210I$ $a = -0.666667 + 0.235702I$ $b = -1.00000$	-4.93480	0

$$\text{IV. } I_4^u = \langle b^2au + b^3 - bu - au - b + u - 1, u^2 - u + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} b + a \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b + a \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -b^2 - ba + 1 \\ -b^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -bau - a^2u + a^2 - u \\ -b^2u - bau + ba + u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} bau + a^2u - a^2 + b + a + u \\ b^2u + bau - ba + b - u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} bau + a^2u - a^2 + b + a + u \\ b^2u + bau - ba + b - u + 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $-4u + 8$**

**(iv) u-Polynomials at the component :** It cannot be defined for a positive dimension component.

**(v) Riley Polynomials at the component :** It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

Solution to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = \dots$		
$a = \dots$	$1.64493 - 2.02988I$	$6.00000 - 3.46410I$
$b = \dots$		

$$\mathbf{V}. I_1^v = \langle a, b^3 - b - 1, v - 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -b^2 + 1 \\ -b^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ b^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} b + 1 \\ b^2 + b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} b + 1 \\ b^2 + b \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes = 6**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$u^3$
$c_3, c_4, c_8$ $c_9, c_{11}$	$u^3 - u + 1$
$c_6$	$u^3 + 2u^2 + u + 1$
$c_7, c_{10}$	$(u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$y^3$
$c_3, c_4, c_8$ $c_9, c_{11}$	$y^3 - 2y^2 + y - 1$
$c_6$	$y^3 - 2y^2 - 3y - 1$
$c_7, c_{10}$	$(y - 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$ $a = 0$ $b = -0.662359 + 0.562280I$	1.64493	6.00000
$v = 1.00000$ $a = 0$ $b = -0.662359 - 0.562280I$	1.64493	6.00000
$v = 1.00000$ $a = 0$ $b = 1.32472$	1.64493	6.00000



$$\text{VI. } I_2^v = \langle a, b - 1, v - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_5$ $c_7, c_{10}$	$u$
$c_3, c_4, c_{11}$	$u - 1$
$c_6, c_8, c_9$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_7, c_{10}$	$y$
$c_3, c_4, c_6$ $c_8, c_9, c_{11}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$	0	0
$b = 1.00000$		

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^4(u^2 + 2)(u^2 - u + 1)^3(u^{53} + 4u^{52} + \dots - 92u - 46)$
$c_2$	$u^4(u + 2)^2(u^2 + u + 1)^3(u^{53} + 24u^{52} + \dots + 3496u - 2116)$
$c_3$	$9(u - 1)(u + 1)^2(u^3 - u + 1)(u^6 - 2u^4 - u^3 + u^2 + u + 1)$ $\cdot (9u^{53} - 18u^{52} + \dots - 77u - 19)$
$c_4$	$9(u - 1)(u + 1)^2(u^3 - u + 1)(u^6 - 2u^4 - u^3 + u^2 + u + 1)$ $\cdot (9u^{53} + 18u^{52} + \dots - 9u - 19)$
$c_6$	$48(u + 1)(3u^2 - 2u + 1)(u^3 + 2u^2 + u + 1)(u^6 - 2u^4 + \dots + u + 1)$ $\cdot (16u^{53} - 16u^{52} + \dots + 103779u - 3609)$
$c_7, c_{10}$	$u^7(u - 1)^3(u^2 + 2)(u^{53} + 6u^{52} + \dots - 5832u - 1706)$
$c_8$	$9(u - 1)^2(u + 1)(u^3 - u + 1)(u^6 - 2u^4 - u^3 + u^2 + u + 1)$ $\cdot (9u^{53} + 18u^{52} + \dots - 9u - 19)$
$c_9$	$9(u - 1)^2(u + 1)(u^3 - u + 1)(u^6 - 2u^4 - u^3 + u^2 + u + 1)$ $\cdot (9u^{53} - 18u^{52} + \dots - 77u - 19)$
$c_{11}$	$48(u - 1)(3u^2 - 2u + 1)(u^3 - u + 1)(u^6 - 4u^5 + \dots + u + 1)$ $\cdot (16u^{53} + 32u^{52} + \dots - 16641u - 6003)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^4(y+2)^2(y^2+y+1)^3(y^{53} + 24y^{52} + \dots + 3496y - 2116)$
$c_2$	$y^4(y-4)^2(y^2+y+1)^3$ $\cdot (y^{53} + 12y^{52} + \dots + 393508288y - 4477456)$
$c_3, c_9$	$81(y-1)^3(y^3-2y^2+y-1)(y^6-4y^5+6y^4-3y^3-y^2+y+1)$ $\cdot (81y^{53} - 3510y^{52} + \dots + 3421y - 361)$
$c_4, c_8$	$81(y-1)^3(y^3-2y^2+y-1)(y^6-4y^5+6y^4-3y^3-y^2+y+1)$ $\cdot (81y^{53} - 2214y^{52} + \dots + 7149y - 361)$
$c_6$	$2304(y-1)(9y^2+2y+1)(y^3-2y^2-3y-1)$ $\cdot (y^6-4y^5+6y^4-3y^3-y^2+y+1)$ $\cdot (256y^{53} + 6016y^{52} + \dots + 9942551577y - 13024881)$
$c_7, c_{10}$	$y^7(y-1)^3(y+2)^2(y^{53} - 30y^{52} + \dots - 5573800y - 2910436)$
$c_{11}$	$2304(y-1)(9y^2+2y+1)(y^3-2y^2+y-1)$ $\cdot (y^6-4y^5+10y^4-11y^3+19y^2-3y+1)$ $\cdot (256y^{53} - 6528y^{52} + \dots - 368087463y - 36036009)$