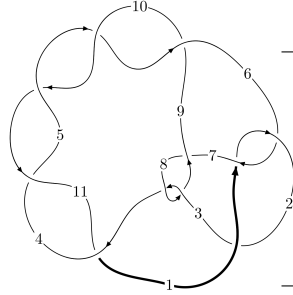
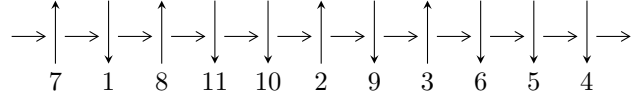


# 11a<sub>214</sub> (K11a<sub>214</sub>)



A knot diagram<sup>1</sup>

## Linearized knot diagram



## Solving Sequence

$$4,8 \xrightarrow{c_3} 3 \xrightarrow{c_8} 1,9 \xrightarrow{c_2} 2 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \xrightarrow{c_{11}} 11 \xrightarrow{c_4} 5 \xrightarrow{c_{10}} 10 \longrightarrow c_1, c_5, c_9$$

## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned} I_1^u &= \langle u^{15} - u^{14} + 2u^{13} - u^{12} + 5u^{11} - 5u^{10} + 4u^9 - 2u^8 + 7u^7 - 11u^6 + 4u^5 - 4u^4 + 5u^3 - 11u^2 + 4b - 1, \\ &\quad - u^{15} + u^{14} - 2u^{13} + u^{12} - 5u^{11} + 5u^{10} - 4u^9 + 2u^8 - 7u^7 + 11u^6 - 4u^5 - 5u^3 + 7u^2 + 4a - 3, \\ &\quad u^{16} + 3u^{14} + u^{13} + 8u^{12} + 2u^{11} + 11u^{10} + 4u^9 + 15u^8 + 2u^7 + 13u^6 + 2u^5 + 11u^4 + 5u^2 + u + 1 \rangle \\ I_2^u &= \langle 24532u^{21} + 99990u^{20} + \dots + 429733b + 160508, \\ &\quad 1188174u^{21} - 128444u^{20} + \dots + 2148665a + 5939931, u^{22} - u^{21} + \dots - 6u + 5 \rangle \\ I_3^u &= \langle b + a + 1, a^2 - au + 2a - u + 2, u^2 + 1 \rangle \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 42 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{15} - u^{14} + \dots + 4b - 1, -u^{15} + u^{14} + \dots + 4a - 3, u^{16} + 3u^{14} + \dots + u + 1 \rangle \quad \mathbf{I.}$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{4}u^{15} - \frac{1}{4}u^{14} + \dots - \frac{7}{4}u^2 + \frac{3}{4} \\ -\frac{1}{4}u^{15} + \frac{1}{4}u^{14} + \dots + \frac{11}{4}u^2 + \frac{1}{4} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{4}u^{15} - \frac{1}{4}u^{14} + \dots - \frac{7}{4}u^2 + \frac{3}{4} \\ -\frac{1}{4}u^{15} + \frac{1}{4}u^{14} + \dots + \frac{7}{4}u^2 + \frac{1}{4} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{4}u^{15} + \frac{1}{4}u^{14} + \dots - \frac{1}{2}u + \frac{1}{4} \\ -\frac{1}{4}u^{15} - \frac{1}{4}u^{14} + \dots + \frac{1}{2}u - \frac{1}{4} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^4 + u^2 + 1 \\ -\frac{1}{4}u^{15} + \frac{1}{4}u^{14} + \dots + \frac{11}{4}u^2 + \frac{1}{4} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{4}u^{15} + \frac{1}{4}u^{14} + \dots + \frac{11}{4}u^2 + \frac{5}{4} \\ u^{15} + \frac{5}{2}u^{13} + \dots + u - \frac{1}{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{4}u^{15} + \frac{3}{4}u^{14} + \dots + u + \frac{5}{4} \\ -\frac{1}{2}u^{14} - \frac{1}{2}u^{13} + \dots - \frac{5}{2}u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{4}u^{15} + \frac{3}{4}u^{14} + \dots + u + \frac{5}{4} \\ -\frac{1}{2}u^{14} - \frac{1}{2}u^{13} + \dots - \frac{5}{2}u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 3u^{15} - 2u^{14} + 9u^{13} - 2u^{12} + 21u^{11} - 9u^{10} + 27u^9 - 8u^8 + 32u^7 - 26u^6 + 30u^5 - 17u^4 + 23u^3 - 23u^2 + 11u - 3$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$u^{16} + 3u^{14} + \dots - u + 1$
$c_2, c_7$	$u^{16} + 6u^{15} + \dots + 9u + 1$
$c_4, c_5, c_9$ $c_{10}, c_{11}$	$u^{16} - 3u^{15} + \dots - 7u + 2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$y^{16} + 6y^{15} + \dots + 9y + 1$
$c_2, c_7$	$y^{16} + 14y^{15} + \dots + 13y + 1$
$c_4, c_5, c_9$ $c_{10}, c_{11}$	$y^{16} + 21y^{15} + \dots + 23y + 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.739034 + 0.627334I$ $a = 0.206056 + 0.079796I$ $b = 0.110083 + 1.130490I$	$5.48130 + 1.05317I$	$4.45688 - 2.38990I$
$u = 0.739034 - 0.627334I$ $a = 0.206056 - 0.079796I$ $b = 0.110083 - 1.130490I$	$5.48130 - 1.05317I$	$4.45688 + 2.38990I$
$u = -0.555046 + 0.909908I$ $a = -0.752118 + 0.605011I$ $b = 0.482247 - 0.564899I$	$-0.19881 - 2.75301I$	$-1.57245 + 2.26508I$
$u = -0.555046 - 0.909908I$ $a = -0.752118 - 0.605011I$ $b = 0.482247 + 0.564899I$	$-0.19881 + 2.75301I$	$-1.57245 - 2.26508I$
$u = -0.926846 + 0.626361I$ $a = 0.304991 - 0.497485I$ $b = 0.03144 - 1.74738I$	$15.8152 - 0.4292I$	$4.82755 + 2.00465I$
$u = -0.926846 - 0.626361I$ $a = 0.304991 + 0.497485I$ $b = 0.03144 + 1.74738I$	$15.8152 + 0.4292I$	$4.82755 - 2.00465I$
$u = 0.317155 + 0.789225I$ $a = 0.47307 - 1.59041I$ $b = 0.02681 + 1.56809I$	$6.59915 + 1.30998I$	$1.95561 - 5.45778I$
$u = 0.317155 - 0.789225I$ $a = 0.47307 + 1.59041I$ $b = 0.02681 - 1.56809I$	$6.59915 - 1.30998I$	$1.95561 + 5.45778I$
$u = 0.596655 + 1.032140I$ $a = -1.346280 - 0.306488I$ $b = 0.623112 - 0.209109I$	$-1.29053 + 6.45307I$	$-4.44807 - 7.45131I$
$u = 0.596655 - 1.032140I$ $a = -1.346280 + 0.306488I$ $b = 0.623112 + 0.209109I$	$-1.29053 - 6.45307I$	$-4.44807 + 7.45131I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.652805 + 1.114230I$		
$a = -1.64360 - 0.10173I$	$2.50481 - 9.84228I$	$-0.10556 + 8.25112I$
$b = 0.376764 + 1.019230I$		
$u = -0.652805 - 1.114230I$		
$a = -1.64360 + 0.10173I$	$2.50481 + 9.84228I$	$-0.10556 - 8.25112I$
$b = 0.376764 - 1.019230I$		
$u = 0.691623 + 1.176670I$		
$a = -1.83564 + 0.40291I$	$12.2077 + 11.7947I$	$0.96071 - 6.63599I$
$b = 0.10149 - 1.72523I$		
$u = 0.691623 - 1.176670I$		
$a = -1.83564 - 0.40291I$	$12.2077 - 11.7947I$	$0.96071 + 6.63599I$
$b = 0.10149 + 1.72523I$		
$u = -0.209770 + 0.436269I$		
$a = 1.093530 + 0.297205I$	$0.004513 - 0.990902I$	$-0.07468 + 7.34190I$
$b = -0.251943 - 0.426672I$		
$u = -0.209770 - 0.436269I$		
$a = 1.093530 - 0.297205I$	$0.004513 + 0.990902I$	$-0.07468 - 7.34190I$
$b = -0.251943 + 0.426672I$		

$$\text{II. } I_2^u = \langle 24532u^{21} + 99990u^{20} + \dots + 429733b + 160508, 1.19 \times 10^6 u^{21} - 1.28 \times 10^5 u^{20} + \dots + 2.15 \times 10^6 a + 5.94 \times 10^6, u^{22} - u^{21} + \dots - 6u + 5 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.552982u^{21} + 0.0597785u^{20} + \dots + 1.60210u - 2.76448 \\ -0.0570866u^{21} - 0.232679u^{20} + \dots + 0.277416u - 0.373506 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.610069u^{21} - 0.172901u^{20} + \dots + 1.87951u - 2.13798 \\ -0.295974u^{21} - 0.109836u^{20} + \dots - 0.426602u - 0.137709 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.857671u^{21} + 1.08755u^{20} + \dots - 5.92382u + 3.22114 \\ -0.358651u^{21} + 0.737100u^{20} + \dots - 1.13075u + 1.90093 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.610069u^{21} - 0.172901u^{20} + \dots + 1.87951u - 3.13798 \\ -0.0570866u^{21} - 0.232679u^{20} + \dots + 0.277416u - 0.373506 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.297712u^{21} - 0.0832768u^{20} + \dots + 0.722951u - 1.80592 \\ -0.0824745u^{21} - 0.0617407u^{20} + \dots + 0.677572u - 1.65554 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.116673u^{21} + 0.386783u^{20} + \dots + 2.80778u + 0.179480 \\ 0.531833u^{21} - 0.160528u^{20} + \dots + 2.45702u - 1.02872 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.116673u^{21} + 0.386783u^{20} + \dots + 2.80778u + 0.179480 \\ 0.531833u^{21} - 0.160528u^{20} + \dots + 2.45702u - 1.02872 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{412776}{429733}u^{21} - \frac{136152}{429733}u^{20} + \dots + \frac{1938508}{429733}u - \frac{1667194}{429733}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$u^{22} + u^{21} + \dots + 6u + 5$
$c_2, c_7$	$u^{22} + 11u^{21} + \dots + 124u + 25$
$c_4, c_5, c_9$ $c_{10}, c_{11}$	$(u^{11} + u^{10} + 8u^9 + 7u^8 + 22u^7 + 16u^6 + 24u^5 + 13u^4 + 9u^3 + 3u^2 - 1)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$y^{22} + 11y^{21} + \dots + 124y + 25$
$c_2, c_7$	$y^{22} - y^{21} + \dots + 4824y + 625$
$c_4, c_5, c_9$ $c_{10}, c_{11}$	$(y^{11} + 15y^{10} + \dots + 6y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.579803 + 0.857238I$ $a = -1.85524 - 1.12681I$ $b = 0.03037 - 1.69780I$	$7.95553 + 2.30219I$	$0.32022 - 2.86330I$
$u = 0.579803 - 0.857238I$ $a = -1.85524 + 1.12681I$ $b = 0.03037 + 1.69780I$	$7.95553 - 2.30219I$	$0.32022 + 2.86330I$
$u = -0.399913 + 0.875160I$ $a = -1.65574 + 0.96794I$ $b = 0.147502 + 0.884325I$	$-1.26759 - 1.65848I$	$-0.54419 + 4.72916I$
$u = -0.399913 - 0.875160I$ $a = -1.65574 - 0.96794I$ $b = 0.147502 - 0.884325I$	$-1.26759 + 1.65848I$	$-0.54419 - 4.72916I$
$u = -0.529162 + 0.802687I$ $a = 1.204780 - 0.193673I$ $b = -0.499488 - 0.319159I$	$0.18031 - 1.62554I$	$-1.42199 + 3.91435I$
$u = -0.529162 - 0.802687I$ $a = 1.204780 + 0.193673I$ $b = -0.499488 + 0.319159I$	$0.18031 + 1.62554I$	$-1.42199 - 3.91435I$
$u = -0.848321 + 0.450725I$ $a = 0.353490 + 0.072972I$ $b = -0.275765 + 1.061690I$	$4.47712 + 4.26374I$	$2.95029 - 4.02329I$
$u = -0.848321 - 0.450725I$ $a = 0.353490 - 0.072972I$ $b = -0.275765 - 1.061690I$	$4.47712 - 4.26374I$	$2.95029 + 4.02329I$
$u = 0.197868 + 1.057100I$ $a = -1.010600 - 0.780021I$ $b = 0.337740$	$-3.92670$	$-11.69818 + 0.I$
$u = 0.197868 - 1.057100I$ $a = -1.010600 + 0.780021I$ $b = 0.337740$	$-3.92670$	$-11.69818 + 0.I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.986171 + 0.439556I$ $a = 0.194359 - 0.406737I$ $b = -0.07149 - 1.73688I$	$14.4695 - 5.6984I$	$3.54476 + 2.83577I$
$u = 0.986171 - 0.439556I$ $a = 0.194359 + 0.406737I$ $b = -0.07149 + 1.73688I$	$14.4695 + 5.6984I$	$3.54476 - 2.83577I$
$u = 0.662778 + 0.976432I$ $a = 1.42879 + 0.04455I$ $b = -0.275765 + 1.061690I$	$4.47712 + 4.26374I$	$2.95029 - 4.02329I$
$u = 0.662778 - 0.976432I$ $a = 1.42879 - 0.04455I$ $b = -0.275765 - 1.061690I$	$4.47712 - 4.26374I$	$2.95029 + 4.02329I$
$u = 0.610796 + 0.518790I$ $a = 0.780853 + 0.341379I$ $b = -0.499488 - 0.319159I$	$0.18031 - 1.62554I$	$-1.42199 + 3.91435I$
$u = 0.610796 - 0.518790I$ $a = 0.780853 - 0.341379I$ $b = -0.499488 + 0.319159I$	$0.18031 + 1.62554I$	$-1.42199 - 3.91435I$
$u = -0.125296 + 1.244620I$ $a = -0.270054 + 1.088140I$ $b = 0.147502 - 0.884325I$	$-1.26759 + 1.65848I$	$-0.54419 - 4.72916I$
$u = -0.125296 - 1.244620I$ $a = -0.270054 - 1.088140I$ $b = 0.147502 + 0.884325I$	$-1.26759 - 1.65848I$	$-0.54419 + 4.72916I$
$u = -0.746289 + 1.064200I$ $a = 1.62058 + 0.05160I$ $b = -0.07149 - 1.73688I$	$14.4695 - 5.6984I$	$3.54476 + 2.83577I$
$u = -0.746289 - 1.064200I$ $a = 1.62058 - 0.05160I$ $b = -0.07149 + 1.73688I$	$14.4695 + 5.6984I$	$3.54476 - 2.83577I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.111564 + 1.357150I$		
$a = 0.00879 - 1.46999I$	$7.95553 - 2.30219I$	$0.32022 + 2.86330I$
$b = 0.03037 + 1.69780I$		
$u = 0.111564 - 1.357150I$		
$a = 0.00879 + 1.46999I$	$7.95553 + 2.30219I$	$0.32022 - 2.86330I$
$b = 0.03037 - 1.69780I$		

$$\text{III. } I_3^u = \langle b + a + 1, a^2 - au + 2a - u + 2, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ -a - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ -a - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} au \\ -au - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -a - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a + 2 \\ au + u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -au - a - u - 1 \\ a + u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -au - a - u - 1 \\ a + u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$(u^2 + 1)^2$
$c_2$	$(u + 1)^4$
$c_4, c_5, c_9$ $c_{10}, c_{11}$	$u^4 + 3u^2 + 1$
$c_7$	$(u - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$(y + 1)^4$
$c_2, c_7$	$(y - 1)^4$
$c_4, c_5, c_9$ $c_{10}, c_{11}$	$(y^2 + 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$		
$a = -1.000000 - 0.618034I$	-2.30291	-4.00000
$b = 0.618034I$		
$u = 1.000000I$		
$a = -1.000000 + 1.61803I$	5.59278	-4.00000
$b = -1.61803I$		
$u = -1.000000I$		
$a = -1.000000 + 0.618034I$	-2.30291	-4.00000
$b = -0.618034I$		
$u = -1.000000I$		
$a = -1.000000 - 1.61803I$	5.59278	-4.00000
$b = 1.61803I$		



#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$((u^2 + 1)^2)(u^{16} + 3u^{14} + \dots - u + 1)(u^{22} + u^{21} + \dots + 6u + 5)$
$c_2$	$((u + 1)^4)(u^{16} + 6u^{15} + \dots + 9u + 1)(u^{22} + 11u^{21} + \dots + 124u + 25)$
$c_4, c_5, c_9$ $c_{10}, c_{11}$	$(u^4 + 3u^2 + 1)$ $\cdot (u^{11} + u^{10} + 8u^9 + 7u^8 + 22u^7 + 16u^6 + 24u^5 + 13u^4 + 9u^3 + 3u^2 - 1)^2$ $\cdot (u^{16} - 3u^{15} + \dots - 7u + 2)$
$c_7$	$((u - 1)^4)(u^{16} + 6u^{15} + \dots + 9u + 1)(u^{22} + 11u^{21} + \dots + 124u + 25)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_8$	$((y + 1)^4)(y^{16} + 6y^{15} + \dots + 9y + 1)(y^{22} + 11y^{21} + \dots + 124y + 25)$
$c_2, c_7$	$((y - 1)^4)(y^{16} + 14y^{15} + \dots + 13y + 1)(y^{22} - y^{21} + \dots + 4824y + 625)$
$c_4, c_5, c_9$ $c_{10}, c_{11}$	$((y^2 + 3y + 1)^2)(y^{11} + 15y^{10} + \dots + 6y - 1)^2$ $\cdot (y^{16} + 21y^{15} + \dots + 23y + 4)$