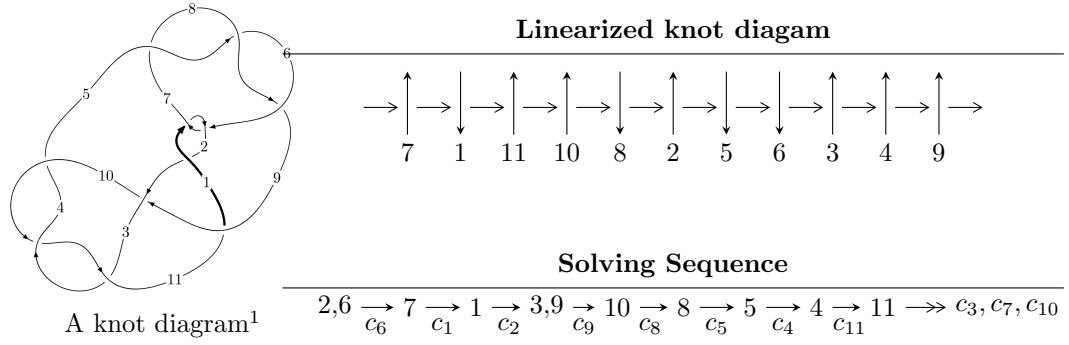


11a<sub>222</sub> (K11a<sub>222</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -3.72396 \times 10^{40} u^{52} - 2.67316 \times 10^{41} u^{51} + \dots + 2.67330 \times 10^{41} b + 1.99338 \times 10^{42}, \\ 4.74949 \times 10^{40} u^{52} + 1.41444 \times 10^{41} u^{51} + \dots + 1.06932 \times 10^{42} a - 1.40219 \times 10^{42}, u^{53} + u^{52} + \dots - 12u - 8 \rangle$$

$$I_1^v = \langle a, b - 1, v^3 + v^2 - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 56 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -3.72 \times 10^{40} u^{52} - 2.67 \times 10^{41} u^{51} + \dots + 2.67 \times 10^{41} b + 1.99 \times 10^{42}, 4.75 \times 10^{40} u^{52} + 1.41 \times 10^{41} u^{51} + \dots + 1.07 \times 10^{42} a - 1.40 \times 10^{42}, u^{53} + u^{52} + \dots - 12u - 8 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0444159u^{52} - 0.132274u^{51} + \dots + 1.64666u + 1.31129 \\ 0.139302u^{52} + 0.999947u^{51} + \dots - 7.49767u - 7.45663 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.343615u^{52} + 0.405811u^{51} + \dots - 0.582641u - 2.59994 \\ 0.279844u^{52} + 1.23840u^{51} + \dots - 9.65395u - 10.2736 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0948858u^{52} + 0.867673u^{51} + \dots - 5.85102u - 6.14534 \\ 0.139302u^{52} + 0.999947u^{51} + \dots - 7.49767u - 7.45663 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0948858u^{52} + 0.867673u^{51} + \dots - 5.85102u - 6.14534 \\ 0.275865u^{52} - 0.199028u^{51} + \dots - 2.53486u + 1.27433 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1.49188u^{52} - 0.252221u^{51} + \dots + 12.9241u + 1.42483 \\ -0.260130u^{52} - 0.116987u^{51} + \dots + 1.92031u - 1.17979 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.424578u^{52} + 0.931561u^{51} + \dots - 9.23571u - 8.47524 \\ 0.273370u^{52} + 0.479526u^{51} + \dots - 2.54983u - 4.25728 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.424578u^{52} + 0.931561u^{51} + \dots - 9.23571u - 8.47524 \\ 0.273370u^{52} + 0.479526u^{51} + \dots - 2.54983u - 4.25728 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.353691u^{52} - 0.908611u^{51} + \dots + 0.108906u + 7.17724$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{53} + u^{52} + \dots - 12u - 8$
$c_2$	$u^{53} + 21u^{52} + \dots - 112u - 64$
$c_3, c_4, c_{10}$	$u^{53} + 2u^{52} + \dots - 3u - 1$
$c_5, c_7, c_8$	$u^{53} - 4u^{52} + \dots + 6u - 1$
$c_9$	$u^{53} - 2u^{52} + \dots - 3u - 1$
$c_{11}$	$u^{53} + 12u^{52} + \dots - 1235u - 131$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{53} + 21y^{52} + \dots - 112y - 64$
$c_2$	$y^{53} + 17y^{52} + \dots + 167168y - 4096$
$c_3, c_4, c_{10}$	$y^{53} + 48y^{52} + \dots + y - 1$
$c_5, c_7, c_8$	$y^{53} - 46y^{52} + \dots + 38y - 1$
$c_9$	$y^{53} + 54y^{51} + \dots + y - 1$
$c_{11}$	$y^{53} + 12y^{52} + \dots - 263187y - 17161$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.098959 + 0.985230I$ $a = -0.216031 - 0.691134I$ $b = 0.741431 + 0.530945I$	$-6.86405 - 3.34890I$	$-5.53237 + 3.71045I$
$u = 0.098959 - 0.985230I$ $a = -0.216031 + 0.691134I$ $b = 0.741431 - 0.530945I$	$-6.86405 + 3.34890I$	$-5.53237 - 3.71045I$
$u = 0.484801 + 0.904145I$ $a = -0.86642 - 2.04538I$ $b = -1.271870 + 0.230719I$	$-0.82302 + 2.29845I$	$2.07591 - 2.82759I$
$u = 0.484801 - 0.904145I$ $a = -0.86642 + 2.04538I$ $b = -1.271870 - 0.230719I$	$-0.82302 - 2.29845I$	$2.07591 + 2.82759I$
$u = 0.665810 + 0.798402I$ $a = 0.568425 + 1.140550I$ $b = 0.077045 - 0.713159I$	$0.59121 + 2.50996I$	$4.33610 - 3.95071I$
$u = 0.665810 - 0.798402I$ $a = 0.568425 - 1.140550I$ $b = 0.077045 + 0.713159I$	$0.59121 - 2.50996I$	$4.33610 + 3.95071I$
$u = -0.704489 + 0.647178I$ $a = 0.750323 - 1.123850I$ $b = -0.034455 + 0.645365I$	$2.99577 + 0.83630I$	$8.46469 - 1.37155I$
$u = -0.704489 - 0.647178I$ $a = 0.750323 + 1.123850I$ $b = -0.034455 - 0.645365I$	$2.99577 - 0.83630I$	$8.46469 + 1.37155I$
$u = -0.701831 + 0.644298I$ $a = -0.707620 + 0.370746I$ $b = 1.161210 - 0.306433I$	$-2.68045 + 1.19639I$	$0.561902 - 0.388264I$
$u = -0.701831 - 0.644298I$ $a = -0.707620 - 0.370746I$ $b = 1.161210 + 0.306433I$	$-2.68045 - 1.19639I$	$0.561902 + 0.388264I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.438735 + 0.954883I$		
$a = -0.519557 + 0.602280I$	$-5.75404 - 4.81132I$	$-3.33331 + 4.06462I$
$b = 0.993065 - 0.486660I$		
$u = -0.438735 - 0.954883I$		
$a = -0.519557 - 0.602280I$	$-5.75404 + 4.81132I$	$-3.33331 - 4.06462I$
$b = 0.993065 + 0.486660I$		
$u = 0.456523 + 0.829696I$		
$a = -0.527363 - 0.500478I$	$-0.53651 + 1.57348I$	$1.80074 - 4.58385I$
$b = 1.006360 + 0.404023I$		
$u = 0.456523 - 0.829696I$		
$a = -0.527363 + 0.500478I$	$-0.53651 - 1.57348I$	$1.80074 + 4.58385I$
$b = 1.006360 - 0.404023I$		
$u = 0.576999 + 0.889147I$		
$a = 0.435650 + 1.098150I$	$0.38779 + 2.33704I$	$2.43384 - 2.57524I$
$b = 0.180982 - 0.721453I$		
$u = 0.576999 - 0.889147I$		
$a = 0.435650 - 1.098150I$	$0.38779 - 2.33704I$	$2.43384 + 2.57524I$
$b = 0.180982 + 0.721453I$		
$u = 0.753024 + 0.562381I$		
$a = 0.86895 + 1.15997I$	$-1.92655 - 4.26986I$	$3.38600 + 2.83654I$
$b = -0.115897 - 0.626414I$		
$u = 0.753024 - 0.562381I$		
$a = 0.86895 - 1.15997I$	$-1.92655 + 4.26986I$	$3.38600 - 2.83654I$
$b = -0.115897 + 0.626414I$		
$u = 1.030490 + 0.261952I$		
$a = -0.910866 - 0.146722I$	$-8.23681 + 0.97965I$	$-4.65901 - 0.74482I$
$b = 1.337480 + 0.124077I$		
$u = 1.030490 - 0.261952I$		
$a = -0.910866 + 0.146722I$	$-8.23681 - 0.97965I$	$-4.65901 + 0.74482I$
$b = 1.337480 - 0.124077I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.388639 + 0.850959I$ $a = -1.37535 + 2.10142I$ $b = -1.248240 - 0.181646I$	$-5.29869 + 1.45751I$	$-3.56392 + 1.11425I$
$u = -0.388639 - 0.850959I$ $a = -1.37535 - 2.10142I$ $b = -1.248240 + 0.181646I$	$-5.29869 - 1.45751I$	$-3.56392 - 1.11425I$
$u = -0.412964 + 1.005730I$ $a = 0.231844 - 1.026890I$ $b = 0.346311 + 0.718386I$	$-5.68668 - 1.06282I$	$-2.80690 + 2.95348I$
$u = -0.412964 - 1.005730I$ $a = 0.231844 + 1.026890I$ $b = 0.346311 - 0.718386I$	$-5.68668 + 1.06282I$	$-2.80690 - 2.95348I$
$u = 0.961697 + 0.529123I$ $a = -0.870380 - 0.301578I$ $b = 1.299930 + 0.254117I$	$-1.18376 - 4.09953I$	$2.32118 + 4.98239I$
$u = 0.961697 - 0.529123I$ $a = -0.870380 + 0.301578I$ $b = 1.299930 - 0.254117I$	$-1.18376 + 4.09953I$	$2.32118 - 4.98239I$
$u = -0.815444 + 0.371656I$ $a = -0.786076 + 0.206543I$ $b = 1.231550 - 0.172173I$	$-2.47497 + 0.74735I$	$-0.90212 + 1.24909I$
$u = -0.815444 - 0.371656I$ $a = -0.786076 - 0.206543I$ $b = 1.231550 + 0.172173I$	$-2.47497 - 0.74735I$	$-0.90212 - 1.24909I$
$u = -0.580487 + 0.976562I$ $a = -0.46963 + 1.90355I$ $b = -1.306780 - 0.280326I$	$-3.72441 - 6.08956I$	$-1.10463 + 6.46640I$
$u = -0.580487 - 0.976562I$ $a = -0.46963 - 1.90355I$ $b = -1.306780 + 0.280326I$	$-3.72441 + 6.08956I$	$-1.10463 - 6.46640I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.041700 + 0.533025I$		
$a = -0.917846 + 0.303340I$	$-6.53406 + 7.50813I$	$-2.48060 - 5.10060I$
$b = 1.340090 - 0.256972I$		
$u = -1.041700 - 0.533025I$		
$a = -0.917846 - 0.303340I$	$-6.53406 - 7.50813I$	$-2.48060 + 5.10060I$
$b = 1.340090 + 0.256972I$		
$u = -0.633586 + 0.994698I$		
$a = 0.371306 - 1.203140I$	$1.93858 - 5.99540I$	$5.14118 + 7.31361I$
$b = 0.199005 + 0.815326I$		
$u = -0.633586 - 0.994698I$		
$a = 0.371306 + 1.203140I$	$1.93858 + 5.99540I$	$5.14118 - 7.31361I$
$b = 0.199005 - 0.815326I$		
$u = -0.053370 + 0.778256I$		
$a = -0.099463 + 0.457828I$	$-1.43718 + 1.12513I$	$-2.70988 - 5.24060I$
$b = 0.673274 - 0.340918I$		
$u = -0.053370 - 0.778256I$		
$a = -0.099463 - 0.457828I$	$-1.43718 - 1.12513I$	$-2.70988 + 5.24060I$
$b = 0.673274 + 0.340918I$		
$u = 0.634803 + 1.049780I$		
$a = 0.326864 + 1.231490I$	$-3.39969 + 9.56118I$	$0. - 7.56251I$
$b = 0.224599 - 0.849112I$		
$u = 0.634803 - 1.049780I$		
$a = 0.326864 - 1.231490I$	$-3.39969 - 9.56118I$	$0. + 7.56251I$
$b = 0.224599 + 0.849112I$		
$u = -0.061506 + 1.244360I$		
$a = -0.819931 + 0.179681I$	$-8.22882 - 1.96670I$	$-4.21460 + 3.59094I$
$b = -1.44045 - 0.02930I$		
$u = -0.061506 - 1.244360I$		
$a = -0.819931 - 0.179681I$	$-8.22882 + 1.96670I$	$-4.21460 - 3.59094I$
$b = -1.44045 + 0.02930I$		



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.630774 + 1.106670I$ $a = -0.22899 + 1.62310I$ $b = -1.372550 - 0.306311I$	$-4.53517 - 6.09494I$	0
$u = -0.630774 - 1.106670I$ $a = -0.22899 - 1.62310I$ $b = -1.372550 + 0.306311I$	$-4.53517 + 6.09494I$	0
$u = 0.564987 + 1.202570I$ $a = -0.252964 - 1.360110I$ $b = -1.42026 + 0.27304I$	$-11.29940 + 4.62469I$	0
$u = 0.564987 - 1.202570I$ $a = -0.252964 + 1.360110I$ $b = -1.42026 - 0.27304I$	$-11.29940 - 4.62469I$	0
$u = 0.698514 + 1.133990I$ $a = -0.07006 - 1.62273I$ $b = -1.38677 + 0.34044I$	$-3.08458 + 10.16490I$	0
$u = 0.698514 - 1.133990I$ $a = -0.07006 + 1.62273I$ $b = -1.38677 - 0.34044I$	$-3.08458 - 10.16490I$	0
$u = 0.109910 + 1.333410I$ $a = -0.563705 - 0.274434I$ $b = -1.48292 + 0.05239I$	$-14.2996 + 4.8556I$	0
$u = 0.109910 - 1.333410I$ $a = -0.563705 + 0.274434I$ $b = -1.48292 - 0.05239I$	$-14.2996 - 4.8556I$	0
$u = -0.723673 + 1.167980I$ $a = 0.00012 + 1.57826I$ $b = -1.40426 - 0.35282I$	$-8.5679 - 13.8903I$	0
$u = -0.723673 - 1.167980I$ $a = 0.00012 - 1.57826I$ $b = -1.40426 + 0.35282I$	$-8.5679 + 13.8903I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.546347 + 0.172932I$ $a = 1.47434 - 0.57598I$ $b = -0.248192 + 0.218926I$	$-3.39404 - 2.40292I$	$4.22803 + 2.59091I$
$u = -0.546347 - 0.172932I$ $a = 1.47434 + 0.57598I$ $b = -0.248192 - 0.218926I$	$-3.39404 + 2.40292I$	$4.22803 - 2.59091I$
$u = 0.394055$ $a = 1.34884$ $b = -0.159324$	0.852216	12.0640

$$\text{II. } I_1^v = \langle a, b - 1, v^3 + v^2 - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v^2 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v^2 + v - 1 \\ v^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ v \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ v \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-v^2 + 3v + 1$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_6$	$u^3$
$c_3, c_4$	$u^3 - u^2 + 2u - 1$
$c_5$	$(u - 1)^3$
$c_7, c_8$	$(u + 1)^3$
$c_9$	$u^3 - u^2 + 1$
$c_{10}$	$u^3 + u^2 + 2u + 1$
$c_{11}$	$u^3 + u^2 - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$	$y^3$
$c_3, c_4, c_{10}$	$y^3 + 3y^2 + 2y - 1$
$c_5, c_7, c_8$	$(y - 1)^3$
$c_9, c_{11}$	$y^3 - y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.877439 + 0.744862I$ $a = 0$ $b = 1.00000$	$-4.66906 - 2.82812I$	$-1.84740 + 3.54173I$
$v = -0.877439 - 0.744862I$ $a = 0$ $b = 1.00000$	$-4.66906 + 2.82812I$	$-1.84740 - 3.54173I$
$v = 0.754878$ $a = 0$ $b = 1.00000$	$-0.531480$	$2.69480$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^3(u^{53} + u^{52} + \dots - 12u - 8)$
$c_2$	$u^3(u^{53} + 21u^{52} + \dots - 112u - 64)$
$c_3, c_4$	$(u^3 - u^2 + 2u - 1)(u^{53} + 2u^{52} + \dots - 3u - 1)$
$c_5$	$((u - 1)^3)(u^{53} - 4u^{52} + \dots + 6u - 1)$
$c_7, c_8$	$((u + 1)^3)(u^{53} - 4u^{52} + \dots + 6u - 1)$
$c_9$	$(u^3 - u^2 + 1)(u^{53} - 2u^{52} + \dots - 3u - 1)$
$c_{10}$	$(u^3 + u^2 + 2u + 1)(u^{53} + 2u^{52} + \dots - 3u - 1)$
$c_{11}$	$(u^3 + u^2 - 1)(u^{53} + 12u^{52} + \dots - 1235u - 131)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^3(y^{53} + 21y^{52} + \dots - 112y - 64)$
$c_2$	$y^3(y^{53} + 17y^{52} + \dots + 167168y - 4096)$
$c_3, c_4, c_{10}$	$(y^3 + 3y^2 + 2y - 1)(y^{53} + 48y^{52} + \dots + y - 1)$
$c_5, c_7, c_8$	$((y - 1)^3)(y^{53} - 46y^{52} + \dots + 38y - 1)$
$c_9$	$(y^3 - y^2 + 2y - 1)(y^{53} + 54y^{51} + \dots + y - 1)$
$c_{11}$	$(y^3 - y^2 + 2y - 1)(y^{53} + 12y^{52} + \dots - 263187y - 17161)$