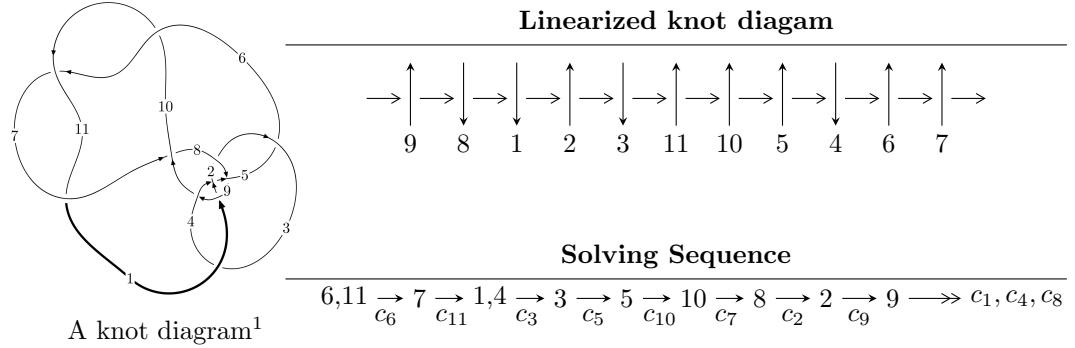


## $11a_{248}$ ( $K11a_{248}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -7806u^{39} - 28939u^{38} + \dots + 1091b + 30599, 20501u^{39} + 69845u^{38} + \dots + 4364a - 128043, \\
 &\quad u^{40} + 5u^{39} + \dots + 9u - 4 \rangle \\
 I_2^u &= \langle u^{26}a + u^{26} + \dots + b - u, -4u^{26}a + 4u^{26} + \dots - a + 5, u^{27} - 2u^{26} + \dots - 4u^2 - 1 \rangle \\
 I_3^u &= \langle -u^{11} + 6u^9 + u^8 - 12u^7 - 5u^6 + 8u^5 + 7u^4 + 2u^3 - 2u^2 + b - 3u, \\
 &\quad u^{12} - 6u^{10} - u^9 + 13u^8 + 4u^7 - 11u^6 - 6u^5 + u^4 + 4u^3 + 3u^2 + a - 2u - 2, \\
 &\quad u^{13} - 2u^{12} - 5u^{11} + 10u^{10} + 10u^9 - 17u^8 - 11u^7 + 8u^6 + 7u^5 + 7u^4 - u^3 - 7u^2 - 1 \rangle \\
 I_4^u &= \langle b + 1, a^2 - 3a + 3, u + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 109 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -7806u^{39} - 28939u^{38} + \cdots + 1091b + 30599, 20501u^{39} + 69845u^{38} + \cdots + 4364a - 128043, u^{40} + 5u^{39} + \cdots + 9u - 4 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -4.69775u^{39} - 16.0048u^{38} + \cdots - 70.7569u + 29.3407 \\ 7.15490u^{39} + 26.5252u^{38} + \cdots + 78.3217u - 28.0467 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 12.9365u^{39} + 44.7789u^{38} + \cdots + 77.7912u - 24.2945 \\ -13.4088u^{39} - 49.4097u^{38} + \cdots - 90.1567u + 27.8689 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -7.68492u^{39} - 28.0323u^{38} + \cdots - 26.6533u + 1.57356 \\ 11.5527u^{39} + 43.6728u^{38} + \cdots + 54.5325u - 10.8295 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 7.93103u^{39} + 26.6478u^{38} + \cdots + 51.3183u - 18.2514 \\ -11.2988u^{39} - 41.7883u^{38} + \cdots - 83.6975u + 27.0073 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1.73854u^{39} + 0.0602658u^{38} + \cdots + 26.7647u - 19.7436 \\ -1.46379u^{39} - 2.72044u^{38} + \cdots - 15.8863u + 10.2997 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1.73854u^{39} + 0.0602658u^{38} + \cdots + 26.7647u - 19.7436 \\ -1.46379u^{39} - 2.72044u^{38} + \cdots - 15.8863u + 10.2997 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

$$(iii) \text{ Cusp Shapes} = -\frac{10012}{1091}u^{39} - \frac{44785}{1091}u^{38} + \cdots + \frac{78319}{1091}u - \frac{64130}{1091}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_8$	$u^{40} - u^{39} + \cdots + 2u - 1$
$c_2, c_9$	$u^{40} + 2u^{38} + \cdots - u - 1$
$c_3, c_5$	$u^{40} + 6u^{39} + \cdots - 23u + 1$
$c_4$	$u^{40} + 22u^{39} + \cdots + 9u + 2$
$c_6, c_{10}, c_{11}$	$u^{40} - 5u^{39} + \cdots - 9u - 4$
$c_7$	$u^{40} + 15u^{39} + \cdots + 89u + 4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_8$	$y^{40} + 17y^{39} + \cdots + 44y + 1$
$c_2, c_9$	$y^{40} + 4y^{39} + \cdots - 23y + 1$
$c_3, c_5$	$y^{40} - 24y^{39} + \cdots - 199y + 1$
$c_4$	$y^{40} + 28y^{38} + \cdots - 5y + 4$
$c_6, c_{10}, c_{11}$	$y^{40} - 37y^{39} + \cdots - 9y + 16$
$c_7$	$y^{40} - y^{39} + \cdots - 937y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.833239 + 0.478940I$	$-0.67356 - 9.11808I$	$3.09330 + 5.04292I$
$a = 1.36899 + 1.05581I$		
$b = 0.113249 - 0.613771I$		
$u = 0.833239 - 0.478940I$	$-0.67356 + 9.11808I$	$3.09330 - 5.04292I$
$a = 1.36899 - 1.05581I$		
$b = 0.113249 + 0.613771I$		
$u = 0.944818 + 0.044872I$	$-1.64126 - 1.68382I$	$-2.62360 + 4.24820I$
$a = -1.88518 - 0.83264I$		
$b = 1.092540 + 0.590515I$		
$u = 0.944818 - 0.044872I$	$-1.64126 + 1.68382I$	$-2.62360 - 4.24820I$
$a = -1.88518 + 0.83264I$		
$b = 1.092540 - 0.590515I$		
$u = 1.045020 + 0.426092I$	$-1.51874 + 7.98713I$	$1.00079 - 8.43785I$
$a = 1.40350 - 0.24037I$		
$b = -0.777991 - 0.700678I$		
$u = 1.045020 - 0.426092I$	$-1.51874 - 7.98713I$	$1.00079 + 8.43785I$
$a = 1.40350 + 0.24037I$		
$b = -0.777991 + 0.700678I$		
$u = 0.127215 + 0.839082I$	$-4.35513 - 3.45950I$	$-3.88332 + 4.09172I$
$a = -0.212294 + 0.072049I$		
$b = -0.507546 + 1.079890I$		
$u = 0.127215 - 0.839082I$	$-4.35513 + 3.45950I$	$-3.88332 - 4.09172I$
$a = -0.212294 - 0.072049I$		
$b = -0.507546 - 1.079890I$		
$u = 0.277504 + 0.801125I$	$-2.45998 + 13.64270I$	$1.03420 - 9.07195I$
$a = 0.171151 - 0.043121I$		
$b = 0.77473 + 1.69376I$		
$u = 0.277504 - 0.801125I$	$-2.45998 - 13.64270I$	$1.03420 + 9.07195I$
$a = 0.171151 + 0.043121I$		
$b = 0.77473 - 1.69376I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.777292$		
$a = -0.568128$	1.36099	8.46400
$b = -0.113354$		
$u = 0.225491 + 0.702834I$		
$a = 0.212358 + 0.335622I$	$-3.63204 + 5.12135I$	$-5.87713 - 8.64312I$
$b = -0.39127 - 1.71232I$		
$u = 0.225491 - 0.702834I$		
$a = 0.212358 - 0.335622I$	$-3.63204 - 5.12135I$	$-5.87713 + 8.64312I$
$b = -0.39127 + 1.71232I$		
$u = 0.290696 + 0.655817I$		
$a = -0.279795 + 0.357972I$	$-3.25229 + 1.41438I$	$-4.70580 - 2.22096I$
$b = 0.417996 - 0.903025I$		
$u = 0.290696 - 0.655817I$		
$a = -0.279795 - 0.357972I$	$-3.25229 - 1.41438I$	$-4.70580 + 2.22096I$
$b = 0.417996 + 0.903025I$		
$u = -1.283570 + 0.210194I$		
$a = 0.89404 - 1.55425I$	1.12425 - 2.76728I	0. + 3.97586I
$b = -0.229292 + 0.859047I$		
$u = -1.283570 - 0.210194I$		
$a = 0.89404 + 1.55425I$	1.12425 + 2.76728I	0. - 3.97586I
$b = -0.229292 - 0.859047I$		
$u = 1.317130 + 0.218392I$		
$a = -2.22707 - 0.75204I$	1.43716 + 2.94730I	0
$b = 2.17192 + 1.88185I$		
$u = 1.317130 - 0.218392I$		
$a = -2.22707 + 0.75204I$	1.43716 - 2.94730I	0
$b = 2.17192 - 1.88185I$		
$u = 0.646576 + 0.028959I$		
$a = -1.71193 - 0.86713I$	$-1.67832 - 1.69625I$	$-1.45396 + 4.31564I$
$b = 0.662046 + 0.361055I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.646576 - 0.028959I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$
$a = -1.71193 + 0.86713I$	$-1.67832 + 1.69625I$	$-1.45396 - 4.31564I$
$b = 0.662046 - 0.361055I$		
$u = -1.307710 + 0.361702I$		
$a = -0.730497 + 0.872523I$	$0.125718 - 0.859000I$	0
$b = -0.038517 - 0.940647I$		
$u = -1.307710 - 0.361702I$		
$a = -0.730497 - 0.872523I$	$0.125718 + 0.859000I$	0
$b = -0.038517 + 0.940647I$		
$u = -1.374750 + 0.100729I$		
$a = -0.937295 + 0.058184I$	$4.00380 + 0.89695I$	0
$b = 0.401012 + 0.417839I$		
$u = -1.374750 - 0.100729I$		
$a = -0.937295 - 0.058184I$	$4.00380 - 0.89695I$	0
$b = 0.401012 - 0.417839I$		
$u = 1.395900 + 0.204775I$		
$a = 1.022420 + 0.746778I$	$5.90256 + 4.07376I$	0
$b = -0.98876 - 1.47035I$		
$u = 1.395900 - 0.204775I$		
$a = 1.022420 - 0.746778I$	$5.90256 - 4.07376I$	0
$b = -0.98876 + 1.47035I$		
$u = -1.38885 + 0.28086I$		
$a = 2.23443 - 1.30007I$	$1.50108 - 8.69698I$	0
$b = -1.61945 + 1.79021I$		
$u = -1.38885 - 0.28086I$		
$a = 2.23443 + 1.30007I$	$1.50108 + 8.69698I$	0
$b = -1.61945 - 1.79021I$		
$u = -0.024475 + 0.578228I$		
$a = 1.202030 + 0.432697I$	$-2.81557 - 0.07740I$	$-5.03252 - 0.22412I$
$b = 0.84787 - 1.24338I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.024475 - 0.578228I$		
$a = 1.202030 - 0.432697I$	$-2.81557 + 0.07740I$	$-5.03252 + 0.22412I$
$b = 0.84787 + 1.24338I$		
$u = -0.293128 + 0.498415I$		
$a = -0.724756 + 0.441160I$	$0.54657 - 1.42879I$	$5.31935 + 4.51277I$
$b = -0.324784 + 0.529368I$		
$u = -0.293128 - 0.498415I$		
$a = -0.724756 - 0.441160I$	$0.54657 + 1.42879I$	$5.31935 - 4.51277I$
$b = -0.324784 - 0.529368I$		
$u = -1.43383 + 0.26362I$		
$a = 0.738341 - 1.202280I$	$2.31251 - 4.79347I$	0
$b = -0.54490 + 1.45255I$		
$u = -1.43383 - 0.26362I$		
$a = 0.738341 + 1.202280I$	$2.31251 + 4.79347I$	0
$b = -0.54490 - 1.45255I$		
$u = -1.42214 + 0.32372I$		
$a = -2.22593 + 1.15650I$	$2.9545 - 17.7145I$	0
$b = 1.72849 - 2.18761I$		
$u = -1.42214 - 0.32372I$		
$a = -2.22593 - 1.15650I$	$2.9545 + 17.7145I$	0
$b = 1.72849 + 2.18761I$		
$u = -1.51106 + 0.03418I$		
$a = -0.041421 + 0.318529I$	$7.13383 + 7.90887I$	0
$b = 0.551162 - 0.994771I$		
$u = -1.51106 - 0.03418I$		
$a = -0.041421 - 0.318529I$	$7.13383 - 7.90887I$	0
$b = 0.551162 + 0.994771I$		
$u = 1.64915$		
$a = 0.275951$	9.99305	0
$b = -0.563647$		

$$\text{II. } I_2^u = \langle u^{26}a + u^{26} + \dots + b - u, -4u^{26}a + 4u^{26} + \dots - a + 5, u^{27} - 2u^{26} + \dots - 4u^2 - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} a \\ -u^{26}a - u^{26} + \dots + au + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^{26}a - 2u^{26} + \dots - u - 2 \\ u^{26}a - u^{26} + \dots + a + 2u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 2u^{26}a - 3u^{26} + \dots + a - 1 \\ u^{26} - 2u^{25} + \dots - a + 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -3u^{26} + 3u^{25} + \dots + a - 2 \\ u^{26}a - u^{25}a + \dots + 3u + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^{26}a - 2u^{26} + \dots - 4u - 1 \\ 3u^{26} - 2u^{25} + \dots - a + 2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^{26}a - 2u^{26} + \dots - 4u - 1 \\ 3u^{26} - 2u^{25} + \dots - a + 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -u^{26} + 3u^{25} + 11u^{24} - 26u^{23} - 56u^{22} + 83u^{21} + 159u^{20} - 80u^{19} - 221u^{18} - 163u^{17} - 35u^{16} + 448u^{15} + 606u^{14} - 142u^{13} - 752u^{12} - 576u^{11} + 66u^{10} + 578u^9 + 432u^8 + 26u^7 - 126u^6 - 129u^5 - 81u^4 - 38u^3 - 27u^2 - 5u + 3$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_8$	$u^{54} - 4u^{53} + \cdots - u + 1$
$c_2, c_9$	$u^{54} - 2u^{53} + \cdots - 109u + 37$
$c_3, c_5$	$u^{54} - 3u^{53} + \cdots + 18u + 27$
$c_4$	$(u^{27} - 13u^{26} + \cdots - u + 2)^2$
$c_6, c_{10}, c_{11}$	$(u^{27} + 2u^{26} + \cdots + 4u^2 + 1)^2$
$c_7$	$(u^{27} - 9u^{26} + \cdots + 37u - 8)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_8$	$y^{54} - 12y^{53} + \cdots + 5y + 1$
$c_2, c_9$	$y^{54} + 50y^{52} + \cdots + 67373y + 1369$
$c_3, c_5$	$y^{54} + 13y^{53} + \cdots - 6318y + 729$
$c_4$	$(y^{27} - 3y^{26} + \cdots + 53y - 4)^2$
$c_6, c_{10}, c_{11}$	$(y^{27} - 24y^{26} + \cdots - 8y - 1)^2$
$c_7$	$(y^{27} + 5y^{26} + \cdots - 375y - 64)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.895940 + 0.471258I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.342281 - 0.519659I$	$1.130920 + 0.684553I$	$13.8481 - 5.2893I$
$b = -0.095449 + 0.261445I$		
$u = -0.895940 + 0.471258I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.183610 + 0.725180I$	$1.130920 + 0.684553I$	$13.8481 - 5.2893I$
$b = -0.274271 - 0.648456I$		
$u = -0.895940 - 0.471258I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.342281 + 0.519659I$	$1.130920 - 0.684553I$	$13.8481 + 5.2893I$
$b = -0.095449 - 0.261445I$		
$u = -0.895940 - 0.471258I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.183610 - 0.725180I$	$1.130920 - 0.684553I$	$13.8481 + 5.2893I$
$b = -0.274271 + 0.648456I$		
$u = -1.100980 + 0.299749I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.95742 - 1.49151I$	$-0.896800 + 0.835412I$	$-3.62755 - 4.72274I$
$b = -0.305719 + 1.067790I$		
$u = -1.100980 + 0.299749I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -2.01018 - 0.00904I$	$-0.896800 + 0.835412I$	$-3.62755 - 4.72274I$
$b = 1.02376 - 1.27878I$		
$u = -1.100980 - 0.299749I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.95742 + 1.49151I$	$-0.896800 - 0.835412I$	$-3.62755 + 4.72274I$
$b = -0.305719 - 1.067790I$		
$u = -1.100980 - 0.299749I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -2.01018 + 0.00904I$	$-0.896800 - 0.835412I$	$-3.62755 + 4.72274I$
$b = 1.02376 + 1.27878I$		
$u = -0.258632 + 0.812574I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.204845 + 0.236106I$	$-0.86178 - 5.25397I$	$6.46955 + 10.01314I$
$b = -0.67915 + 1.58038I$		
$u = -0.258632 + 0.812574I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.036879 + 0.212663I$	$-0.86178 - 5.25397I$	$6.46955 + 10.01314I$
$b = 0.520153 - 0.752899I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.258632 - 0.812574I$		
$a = -0.204845 - 0.236106I$	$-0.86178 + 5.25397I$	$6.46955 - 10.01314I$
$b = -0.67915 - 1.58038I$		
$u = -0.258632 - 0.812574I$		
$a = -0.036879 - 0.212663I$	$-0.86178 + 5.25397I$	$6.46955 - 10.01314I$
$b = 0.520153 + 0.752899I$		
$u = -0.135996 + 0.743408I$		
$a = 0.688838 + 0.344087I$	$-3.79952 - 4.67674I$	$-5.91242 + 7.08419I$
$b = 0.74927 + 1.65652I$		
$u = -0.135996 + 0.743408I$		
$a = -0.008951 + 0.347544I$	$-3.79952 - 4.67674I$	$-5.91242 + 7.08419I$
$b = 0.87796 - 1.45827I$		
$u = -0.135996 - 0.743408I$		
$a = 0.688838 - 0.344087I$	$-3.79952 + 4.67674I$	$-5.91242 - 7.08419I$
$b = 0.74927 - 1.65652I$		
$u = -0.135996 - 0.743408I$		
$a = -0.008951 - 0.347544I$	$-3.79952 + 4.67674I$	$-5.91242 - 7.08419I$
$b = 0.87796 + 1.45827I$		
$u = 1.275050 + 0.128798I$		
$a = 0.872080 - 0.946956I$	$3.61252 - 2.75180I$	$4.02480 + 5.63147I$
$b = -0.44926 + 1.70261I$		
$u = 1.275050 + 0.128798I$		
$a = -1.61610 - 2.37871I$	$3.61252 - 2.75180I$	$4.02480 + 5.63147I$
$b = 0.40151 + 2.10435I$		
$u = 1.275050 - 0.128798I$		
$a = 0.872080 + 0.946956I$	$3.61252 + 2.75180I$	$4.02480 - 5.63147I$
$b = -0.44926 - 1.70261I$		
$u = 1.275050 - 0.128798I$		
$a = -1.61610 + 2.37871I$	$3.61252 + 2.75180I$	$4.02480 - 5.63147I$
$b = 0.40151 - 2.10435I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.426561 + 0.478609I$		
$a = -0.264904 + 0.981766I$	$0.44505 - 1.73895I$	$7.45580 + 5.77840I$
$b = -0.637652 + 0.148109I$		
$u = -0.426561 + 0.478609I$		
$a = -1.227590 + 0.092870I$	$0.44505 - 1.73895I$	$7.45580 + 5.77840I$
$b = -0.262831 + 0.693605I$		
$u = -0.426561 - 0.478609I$		
$a = -0.264904 - 0.981766I$	$0.44505 + 1.73895I$	$7.45580 - 5.77840I$
$b = -0.637652 - 0.148109I$		
$u = -0.426561 - 0.478609I$		
$a = -1.227590 - 0.092870I$	$0.44505 + 1.73895I$	$7.45580 - 5.77840I$
$b = -0.262831 - 0.693605I$		
$u = -1.361910 + 0.175704I$		
$a = 0.121170 + 0.544702I$	$5.91990 + 0.72025I$	$11.02491 - 0.63973I$
$b = -0.840179 + 0.397373I$		
$u = -1.361910 + 0.175704I$		
$a = -2.78369 + 0.64886I$	$5.91990 + 0.72025I$	$11.02491 - 0.63973I$
$b = 2.75677 - 0.87534I$		
$u = -1.361910 - 0.175704I$		
$a = 0.121170 - 0.544702I$	$5.91990 - 0.72025I$	$11.02491 + 0.63973I$
$b = -0.840179 - 0.397373I$		
$u = -1.361910 - 0.175704I$		
$a = -2.78369 - 0.64886I$	$5.91990 - 0.72025I$	$11.02491 + 0.63973I$
$b = 2.75677 + 0.87534I$		
$u = 1.346310 + 0.301034I$		
$a = 0.93357 + 1.81656I$	$0.87383 + 8.44603I$	$-0.29895 - 8.39876I$
$b = 0.46852 - 1.68017I$		
$u = 1.346310 + 0.301034I$		
$a = -2.51803 - 0.62945I$	$0.87383 + 8.44603I$	$-0.29895 - 8.39876I$
$b = 2.12120 + 1.38215I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.346310 - 0.301034I$		
$a = 0.93357 - 1.81656I$	$0.87383 - 8.44603I$	$-0.29895 + 8.39876I$
$b = 0.46852 + 1.68017I$		
$u = 1.346310 - 0.301034I$		
$a = -2.51803 + 0.62945I$	$0.87383 - 8.44603I$	$-0.29895 + 8.39876I$
$b = 2.12120 - 1.38215I$		
$u = -1.361280 + 0.230867I$		
$a = 0.76323 + 1.29097I$	$5.17654 - 7.89313I$	$8.62044 + 9.21586I$
$b = -0.68764 - 1.90684I$		
$u = -1.361280 + 0.230867I$		
$a = 2.95892 - 1.08916I$	$5.17654 - 7.89313I$	$8.62044 + 9.21586I$
$b = -2.13759 + 2.13430I$		
$u = -1.361280 - 0.230867I$		
$a = 0.76323 - 1.29097I$	$5.17654 + 7.89313I$	$8.62044 - 9.21586I$
$b = -0.68764 + 1.90684I$		
$u = -1.361280 - 0.230867I$		
$a = 2.95892 + 1.08916I$	$5.17654 + 7.89313I$	$8.62044 - 9.21586I$
$b = -2.13759 - 2.13430I$		
$u = 1.392250 + 0.184425I$		
$a = 0.689778 + 0.165914I$	$6.04501 + 4.08549I$	$10.80221 - 3.62417I$
$b = -0.713590 - 1.011530I$		
$u = 1.392250 + 0.184425I$		
$a = 1.47187 + 1.27394I$	$6.04501 + 4.08549I$	$10.80221 - 3.62417I$
$b = -1.51868 - 1.81027I$		
$u = 1.392250 - 0.184425I$		
$a = 0.689778 - 0.165914I$	$6.04501 - 4.08549I$	$10.80221 + 3.62417I$
$b = -0.713590 + 1.011530I$		
$u = 1.392250 - 0.184425I$		
$a = 1.47187 - 1.27394I$	$6.04501 - 4.08549I$	$10.80221 + 3.62417I$
$b = -1.51868 + 1.81027I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.162222 + 0.561060I$		
$a = -0.051560 - 0.625386I$	$0.32804 + 4.95240I$	$2.66900 - 10.41191I$
$b = -0.96597 - 1.94808I$		
$u = 0.162222 + 0.561060I$		
$a = 1.86160 + 0.59224I$	$0.32804 + 4.95240I$	$2.66900 - 10.41191I$
$b = -0.603163 + 0.183472I$		
$u = 0.162222 - 0.561060I$		
$a = -0.051560 + 0.625386I$	$0.32804 - 4.95240I$	$2.66900 + 10.41191I$
$b = -0.96597 + 1.94808I$		
$u = 0.162222 - 0.561060I$		
$a = 1.86160 - 0.59224I$	$0.32804 - 4.95240I$	$2.66900 + 10.41191I$
$b = -0.603163 - 0.183472I$		
$u = 1.41446 + 0.33004I$		
$a = -1.46356 - 0.33947I$	$4.46105 + 9.38162I$	$9.06666 - 9.66600I$
$b = 1.30700 + 0.85510I$		
$u = 1.41446 + 0.33004I$		
$a = 1.96789 + 1.01697I$	$4.46105 + 9.38162I$	$9.06666 - 9.66600I$
$b = -1.41394 - 2.11422I$		
$u = 1.41446 - 0.33004I$		
$a = -1.46356 + 0.33947I$	$4.46105 - 9.38162I$	$9.06666 + 9.66600I$
$b = 1.30700 - 0.85510I$		
$u = 1.41446 - 0.33004I$		
$a = 1.96789 - 1.01697I$	$4.46105 - 9.38162I$	$9.06666 + 9.66600I$
$b = -1.41394 + 2.11422I$		
$u = 1.48928$		
$a = 0.414877 + 0.101829I$	9.10414	14.2140
$b = -0.663673 - 0.708724I$		
$u = 1.48928$		
$a = 0.414877 - 0.101829I$	9.10414	14.2140
$b = -0.663673 + 0.708724I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.206359 + 0.377187I$		
$a = 0.000240 - 1.391780I$	$0.97705 - 2.90650I$	$6.25021 - 1.54831I$
$b = 0.959931 + 1.036890I$		
$u = 0.206359 + 0.377187I$		
$a = -2.67387 - 0.24264I$	$0.97705 - 2.90650I$	$6.25021 - 1.54831I$
$b = -0.437309 + 0.531753I$		
$u = 0.206359 - 0.377187I$		
$a = 0.000240 + 1.391780I$	$0.97705 + 2.90650I$	$6.25021 + 1.54831I$
$b = 0.959931 - 1.036890I$		
$u = 0.206359 - 0.377187I$		
$a = -2.67387 + 0.24264I$	$0.97705 + 2.90650I$	$6.25021 + 1.54831I$
$b = -0.437309 - 0.531753I$		

**III.**

$$I_3^u = \langle -u^{11} + 6u^9 + \dots + b - 3u, u^{12} - 6u^{10} + \dots + a - 2, u^{13} - 2u^{12} + \dots - 7u^2 - 1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{12} + 6u^{10} + \dots + 2u + 2 \\ u^{11} - 6u^9 - u^8 + 12u^7 + 5u^6 - 8u^5 - 7u^4 - 2u^3 + 2u^2 + 3u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -4u^{12} + 2u^{11} + \dots - 20u^3 - 21u^2 \\ 2u^{12} - u^{11} + \dots + 4u + 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2u^{12} + 13u^{10} + \dots - 10u - 1 \\ u^{12} - u^{11} - 6u^{10} + 4u^9 + 13u^8 - 3u^7 - 10u^6 - 5u^5 - 3u^4 + 6u^3 + 6u^2 + 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^{12} + u^{11} + \dots + 3u + 1 \\ u^{12} - 6u^{10} + \dots + 4u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -3u^{12} + 3u^{11} + \dots + u - 4 \\ u^{12} - u^{11} - 6u^{10} + 4u^9 + 14u^8 - 3u^7 - 14u^6 - 6u^5 + 2u^4 + 8u^3 + 5u^2 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -3u^{12} + 3u^{11} + \dots + u - 4 \\ u^{12} - u^{11} - 6u^{10} + 4u^9 + 14u^8 - 3u^7 - 14u^6 - 6u^5 + 2u^4 + 8u^3 + 5u^2 - u \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes**

$$= -12u^{12} + 3u^{11} + 69u^{10} + 4u^9 - 142u^8 - 61u^7 + 92u^6 + 111u^5 + 61u^4 - 41u^3 - 73u^2 - 22u - 10$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_8$	$u^{13} + u^{12} + \cdots - 2u^2 + 1$
$c_2, c_9$	$u^{13} - 2u^{11} + \cdots + u + 1$
$c_3, c_5$	$u^{13} + 4u^{12} + \cdots + 7u + 1$
$c_4$	$u^{13} - 9u^{12} + \cdots + 22u - 3$
$c_6$	$u^{13} - 2u^{12} + \cdots - 7u^2 - 1$
$c_7$	$u^{13} + 6u^{12} + \cdots + 8u + 3$
$c_{10}, c_{11}$	$u^{13} + 2u^{12} + \cdots + 7u^2 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_8$	$y^{13} - 7y^{12} + \cdots + 4y - 1$
$c_2, c_9$	$y^{13} - 4y^{12} + \cdots + 7y - 1$
$c_3, c_5$	$y^{13} + 8y^{12} + \cdots + 11y - 1$
$c_4$	$y^{13} + 3y^{12} + \cdots - 38y - 9$
$c_6, c_{10}, c_{11}$	$y^{13} - 14y^{12} + \cdots - 14y - 1$
$c_7$	$y^{13} - 6y^{12} + \cdots - 122y - 9$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.009960 + 0.393104I$		
$a = 0.925275 - 0.638185I$	$0.418219 + 0.647136I$	$0.16669 - 3.99472I$
$b = -0.104514 + 0.740294I$		
$u = -1.009960 - 0.393104I$		
$a = 0.925275 + 0.638185I$	$0.418219 - 0.647136I$	$0.16669 + 3.99472I$
$b = -0.104514 - 0.740294I$		
$u = -0.167884 + 0.751728I$		
$a = -0.226076 - 0.027387I$	$-2.18684 - 4.76062I$	$0.16967 + 6.96566I$
$b = 0.47713 - 1.33789I$		
$u = -0.167884 - 0.751728I$		
$a = -0.226076 + 0.027387I$	$-2.18684 + 4.76062I$	$0.16967 - 6.96566I$
$b = 0.47713 + 1.33789I$		
$u = 1.341150 + 0.144131I$		
$a = 1.56947 + 0.55075I$	$4.89774 - 1.83075I$	$8.30741 + 4.84620I$
$b = -0.882764 - 0.005150I$		
$u = 1.341150 - 0.144131I$		
$a = 1.56947 - 0.55075I$	$4.89774 + 1.83075I$	$8.30741 - 4.84620I$
$b = -0.882764 + 0.005150I$		
$u = -1.374030 + 0.142033I$		
$a = -0.56717 + 1.54087I$	$5.16744 - 5.48401I$	$6.26872 + 7.46655I$
$b = 0.23741 - 2.17678I$		
$u = -1.374030 - 0.142033I$		
$a = -0.56717 - 1.54087I$	$5.16744 + 5.48401I$	$6.26872 - 7.46655I$
$b = 0.23741 + 2.17678I$		
$u = 1.365520 + 0.295205I$		
$a = -2.00613 - 0.78110I$	$2.66514 + 8.52224I$	$6.00968 - 8.13315I$
$b = 1.34623 + 1.31239I$		
$u = 1.365520 - 0.295205I$		
$a = -2.00613 + 0.78110I$	$2.66514 - 8.52224I$	$6.00968 + 8.13315I$
$b = 1.34623 - 1.31239I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.015927 + 0.356982I$		
$a = 2.40486 + 0.90799I$	$0.51888 + 3.68063I$	$0.09698 - 6.26701I$
$b = -0.330299 + 1.152730I$		
$u = 0.015927 - 0.356982I$		
$a = 2.40486 - 0.90799I$	$0.51888 - 3.68063I$	$0.09698 + 6.26701I$
$b = -0.330299 - 1.152730I$		
$u = 1.65857$		
$a = -0.200450$	9.93750	-69.0380
$b = 0.513607$		

$$\text{IV. } I_4^u = \langle b + 1, a^2 - 3a + 3, u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a-1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2a-3 \\ -a+1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2a+4 \\ a-2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2a+4 \\ a-2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 3

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_8$ $c_9$	$u^2 - u + 1$
$c_3, c_5, c_6$	$(u + 1)^2$
$c_4, c_7$	$u^2$
$c_{10}, c_{11}$	$(u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_8$ $c_9$	$y^2 + y + 1$
$c_3, c_5, c_6$ $c_{10}, c_{11}$	$(y - 1)^2$
$c_4, c_7$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 1.50000 + 0.86603I$	0	3.00000
$b = -1.00000$		
$u = -1.00000$		
$a = 1.50000 - 0.86603I$	0	3.00000
$b = -1.00000$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_8$	$(u^2 - u + 1)(u^{13} + u^{12} + \dots - 2u^2 + 1)(u^{40} - u^{39} + \dots + 2u - 1) \\ \cdot (u^{54} - 4u^{53} + \dots - u + 1)$
$c_2, c_9$	$(u^2 - u + 1)(u^{13} - 2u^{11} + \dots + u + 1)(u^{40} + 2u^{38} + \dots - u - 1) \\ \cdot (u^{54} - 2u^{53} + \dots - 109u + 37)$
$c_3, c_5$	$((u + 1)^2)(u^{13} + 4u^{12} + \dots + 7u + 1)(u^{40} + 6u^{39} + \dots - 23u + 1) \\ \cdot (u^{54} - 3u^{53} + \dots + 18u + 27)$
$c_4$	$u^2(u^{13} - 9u^{12} + \dots + 22u - 3)(u^{27} - 13u^{26} + \dots - u + 2)^2 \\ \cdot (u^{40} + 22u^{39} + \dots + 9u + 2)$
$c_6$	$((u + 1)^2)(u^{13} - 2u^{12} + \dots - 7u^2 - 1)(u^{27} + 2u^{26} + \dots + 4u^2 + 1)^2 \\ \cdot (u^{40} - 5u^{39} + \dots - 9u - 4)$
$c_7$	$u^2(u^{13} + 6u^{12} + \dots + 8u + 3)(u^{27} - 9u^{26} + \dots + 37u - 8)^2 \\ \cdot (u^{40} + 15u^{39} + \dots + 89u + 4)$
$c_{10}, c_{11}$	$((u - 1)^2)(u^{13} + 2u^{12} + \dots + 7u^2 + 1)(u^{27} + 2u^{26} + \dots + 4u^2 + 1)^2 \\ \cdot (u^{40} - 5u^{39} + \dots - 9u - 4)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_8$	$(y^2 + y + 1)(y^{13} - 7y^{12} + \dots + 4y - 1)(y^{40} + 17y^{39} + \dots + 44y + 1) \\ \cdot (y^{54} - 12y^{53} + \dots + 5y + 1)$
$c_2, c_9$	$(y^2 + y + 1)(y^{13} - 4y^{12} + \dots + 7y - 1)(y^{40} + 4y^{39} + \dots - 23y + 1) \\ \cdot (y^{54} + 50y^{52} + \dots + 67373y + 1369)$
$c_3, c_5$	$((y - 1)^2)(y^{13} + 8y^{12} + \dots + 11y - 1)(y^{40} - 24y^{39} + \dots - 199y + 1) \\ \cdot (y^{54} + 13y^{53} + \dots - 6318y + 729)$
$c_4$	$y^2(y^{13} + 3y^{12} + \dots - 38y - 9)(y^{27} - 3y^{26} + \dots + 53y - 4)^2 \\ \cdot (y^{40} + 28y^{38} + \dots - 5y + 4)$
$c_6, c_{10}, c_{11}$	$((y - 1)^2)(y^{13} - 14y^{12} + \dots - 14y - 1)(y^{27} - 24y^{26} + \dots - 8y - 1)^2 \\ \cdot (y^{40} - 37y^{39} + \dots - 9y + 16)$
$c_7$	$y^2(y^{13} - 6y^{12} + \dots - 122y - 9)(y^{27} + 5y^{26} + \dots - 375y - 64)^2 \\ \cdot (y^{40} - y^{39} + \dots - 937y + 16)$