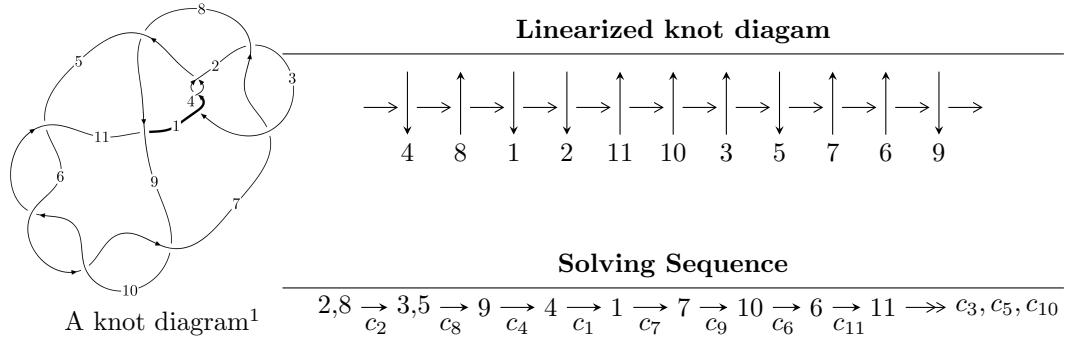


## 11a<sub>258</sub> ( $K11a_{258}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 4.93541 \times 10^{32} u^{40} + 2.04760 \times 10^{32} u^{39} + \dots + 1.23008 \times 10^{33} b - 8.08350 \times 10^{33}, \\ 1.21871 \times 10^{33} u^{40} - 1.85520 \times 10^{33} u^{39} + \dots + 2.46016 \times 10^{33} a + 1.04083 \times 10^{34}, u^{41} - u^{40} + \dots + 8u - 16 \rangle$$

$$I_1^v = \langle a, b - 1, v^4 - v^3 + v^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 4.94 \times 10^{32}u^{40} + 2.05 \times 10^{32}u^{39} + \dots + 1.23 \times 10^{33}b - 8.08 \times 10^{33}, 1.22 \times 10^{33}u^{40} - 1.86 \times 10^{33}u^{39} + \dots + 2.46 \times 10^{33}a + 1.04 \times 10^{34}, u^{41} - u^{40} + \dots + 8u - 16 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.495378u^{40} + 0.754100u^{39} + \dots + 8.36593u - 4.23073 \\ -0.401227u^{40} - 0.166461u^{39} + \dots + 3.25878u + 6.57153 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.00964588u^{40} + 0.868205u^{39} + \dots + 3.33085u - 12.4271 \\ -0.279000u^{40} + 0.570378u^{39} + \dots + 6.14986u - 4.36198 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.896605u^{40} + 0.587639u^{39} + \dots + 11.6247u + 2.34080 \\ -0.401227u^{40} - 0.166461u^{39} + \dots + 3.25878u + 6.57153 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.896605u^{40} + 0.587639u^{39} + \dots + 11.6247u + 2.34080 \\ -0.623981u^{40} + 0.594016u^{39} + \dots + 8.61517u - 1.62808 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.181324u^{40} + 0.551451u^{39} + \dots + 0.442667u - 9.89004 \\ -0.175096u^{40} + 0.493041u^{39} + \dots + 5.13059u - 4.57783 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.295942u^{40} + 0.237376u^{39} + \dots + 3.40554u + 0.455300 \\ -0.311321u^{40} - 0.0909921u^{39} + \dots + 2.02971u + 5.46031 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.248888u^{40} - 0.460318u^{39} + \dots - 0.398174u + 9.13315 \\ -0.0375077u^{40} - 0.244171u^{39} + \dots - 1.75912u + 2.99026 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.248888u^{40} - 0.460318u^{39} + \dots - 0.398174u + 9.13315 \\ -0.0375077u^{40} - 0.244171u^{39} + \dots - 1.75912u + 2.99026 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $0.312617u^{40} + 1.81495u^{39} + \dots + 9.58739u - 33.8289$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$	$u^{41} - 5u^{40} + \cdots - 3u + 1$
$c_2, c_7$	$u^{41} + u^{40} + \cdots + 8u + 16$
$c_5, c_6, c_9$ $c_{10}$	$u^{41} + 2u^{40} + \cdots - 3u - 1$
$c_8$	$u^{41} + 2u^{40} + \cdots - 20u - 100$
$c_{11}$	$u^{41} - 12u^{40} + \cdots + 549u - 131$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$	$y^{41} - 41y^{40} + \cdots - 13y - 1$
$c_2, c_7$	$y^{41} + 27y^{40} + \cdots - 960y - 256$
$c_5, c_6, c_9$ $c_{10}$	$y^{41} + 48y^{40} + \cdots - 7y - 1$
$c_8$	$y^{41} - 24y^{40} + \cdots - 163800y - 10000$
$c_{11}$	$y^{41} - 12y^{40} + \cdots + 112237y - 17161$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.04360$		
$a = -0.918815$	-3.09864	-0.703580
$b = 1.34522$		
$u = -0.280650 + 1.032300I$		
$a = 0.113218 - 0.945326I$	-0.98467 - 2.16041I	0.30534 + 3.36601I
$b = 0.451556 + 0.680540I$		
$u = -0.280650 - 1.032300I$		
$a = 0.113218 + 0.945326I$	-0.98467 + 2.16041I	0.30534 - 3.36601I
$b = 0.451556 - 0.680540I$		
$u = -0.636469 + 0.676356I$		
$a = -0.663046 + 0.390386I$	-8.62893 + 1.18234I	-6.12242 + 0.09680I
$b = 1.123470 - 0.320823I$		
$u = -0.636469 - 0.676356I$		
$a = -0.663046 - 0.390386I$	-8.62893 - 1.18234I	-6.12242 - 0.09680I
$b = 1.123470 + 0.320823I$		
$u = 0.067485 + 1.087720I$		
$a = -1.345840 - 0.268602I$	-3.50700 + 1.95785I	-4.15911 - 3.79195I
$b = -1.365970 + 0.031939I$		
$u = 0.067485 - 1.087720I$		
$a = -1.345840 + 0.268602I$	-3.50700 - 1.95785I	-4.15911 + 3.79195I
$b = -1.365970 - 0.031939I$		
$u = 0.053492 + 1.097010I$		
$a = -0.119204 + 0.861224I$	-3.46087 - 0.57126I	-6.38744 + 1.36032I
$b = 0.644526 - 0.652721I$		
$u = 0.053492 - 1.097010I$		
$a = -0.119204 - 0.861224I$	-3.46087 + 0.57126I	-6.38744 - 1.36032I
$b = 0.644526 + 0.652721I$		
$u = -0.231068 + 1.076220I$		
$a = -1.18409 + 0.88552I$	-9.84300 - 4.44580I	-7.49047 + 4.00982I
$b = -1.359660 - 0.109695I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.231068 - 1.076220I$		
$a = -1.18409 - 0.88552I$	$-9.84300 + 4.44580I$	$-7.49047 - 4.00982I$
$b = -1.359660 + 0.109695I$		
$u = 0.575963 + 0.681143I$		
$a = 0.654397 + 0.985833I$	$-5.44874 + 2.20051I$	$-0.49288 - 3.58387I$
$b = 0.064994 - 0.588385I$		
$u = 0.575963 - 0.681143I$		
$a = 0.654397 - 0.985833I$	$-5.44874 - 2.20051I$	$-0.49288 + 3.58387I$
$b = 0.064994 + 0.588385I$		
$u = -1.179440 + 0.158362I$		
$a = -0.994717 + 0.088396I$	$-5.20973 + 3.10308I$	$-5.68137 - 4.55677I$
$b = 1.409360 - 0.075417I$		
$u = -1.179440 - 0.158362I$		
$a = -0.994717 - 0.088396I$	$-5.20973 - 3.10308I$	$-5.68137 + 4.55677I$
$b = 1.409360 + 0.075417I$		
$u = 0.353950 + 1.159500I$		
$a = 0.079020 + 1.089230I$	$-2.77750 + 5.51756I$	$-3.79773 - 7.77564I$
$b = 0.450262 - 0.797995I$		
$u = 0.353950 - 1.159500I$		
$a = 0.079020 - 1.089230I$	$-2.77750 - 5.51756I$	$-3.79773 + 7.77564I$
$b = 0.450262 + 0.797995I$		
$u = 0.005676 + 1.227250I$		
$a = -0.228021 - 0.942171I$	$-11.55890 + 2.26622I$	$-7.69126 - 0.18572I$
$b = 0.720117 + 0.732589I$		
$u = 0.005676 - 1.227250I$		
$a = -0.228021 + 0.942171I$	$-11.55890 - 2.26622I$	$-7.69126 + 0.18572I$
$b = 0.720117 - 0.732589I$		
$u = -0.383325 + 1.244490I$		
$a = 0.043543 - 1.163710I$	$-10.75100 - 7.67961I$	$-5.88345 + 5.74816I$
$b = 0.463101 + 0.864387I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.383325 - 1.244490I$		
$a = 0.043543 + 1.163710I$	$-10.75100 + 7.67961I$	$-5.88345 - 5.74816I$
$b = 0.463101 - 0.864387I$		
$u = 1.287610 + 0.202232I$		
$a = -1.055360 - 0.112449I$	$-13.2971 - 5.0740I$	$-7.49177 + 2.86395I$
$b = 1.46107 + 0.09654I$		
$u = 1.287610 - 0.202232I$		
$a = -1.055360 + 0.112449I$	$-13.2971 + 5.0740I$	$-7.49177 - 2.86395I$
$b = 1.46107 - 0.09654I$		
$u = -0.637500 + 0.135734I$		
$a = 1.71237 - 0.80495I$	$-7.29387 + 3.70140I$	$0.13489 - 3.24211I$
$b = -0.363345 + 0.258087I$		
$u = -0.637500 - 0.135734I$		
$a = 1.71237 + 0.80495I$	$-7.29387 - 3.70140I$	$0.13489 + 3.24211I$
$b = -0.363345 - 0.258087I$		
$u = -0.442927 + 0.446451I$		
$a = 0.885936 - 0.663779I$	$0.739118 - 0.963294I$	$5.38374 + 5.24951I$
$b = 0.002285 + 0.351914I$		
$u = -0.442927 - 0.446451I$		
$a = 0.885936 + 0.663779I$	$0.739118 + 0.963294I$	$5.38374 - 5.24951I$
$b = 0.002285 - 0.351914I$		
$u = 0.545126 + 0.215241I$		
$a = 1.37573 + 0.63189I$	$0.06188 - 1.89506I$	$3.00107 + 4.96508I$
$b = -0.218730 - 0.254700I$		
$u = 0.545126 - 0.215241I$		
$a = 1.37573 - 0.63189I$	$0.06188 + 1.89506I$	$3.00107 - 4.96508I$
$b = -0.218730 + 0.254700I$		
$u = 0.332351 + 0.473594I$		
$a = -0.483789 - 0.209918I$	$-1.84031 - 0.69258I$	$-6.89864 - 1.74884I$
$b = 0.984199 + 0.167639I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.332351 - 0.473594I$		
$a = -0.483789 + 0.209918I$	$-1.84031 + 0.69258I$	$-6.89864 + 1.74884I$
$b = 0.984199 - 0.167639I$		
$u = 0.52227 + 1.35643I$		
$a = -0.110639 - 1.064090I$	$-7.31234 + 5.60210I$	0
$b = -1.49556 + 0.25090I$		
$u = 0.52227 - 1.35643I$		
$a = -0.110639 + 1.064090I$	$-7.31234 - 5.60210I$	0
$b = -1.49556 - 0.25090I$		
$u = -0.41034 + 1.42300I$		
$a = -0.140257 + 0.816586I$	$-10.55130 - 2.41180I$	0
$b = -1.52685 - 0.19609I$		
$u = -0.41034 - 1.42300I$		
$a = -0.140257 - 0.816586I$	$-10.55130 + 2.41180I$	0
$b = -1.52685 + 0.19609I$		
$u = -0.60199 + 1.38207I$		
$a = 0.024627 + 1.133790I$	$-9.13999 - 9.48739I$	0
$b = -1.50901 - 0.28951I$		
$u = -0.60199 - 1.38207I$		
$a = 0.024627 - 1.133790I$	$-9.13999 + 9.48739I$	0
$b = -1.50901 + 0.28951I$		
$u = 0.65669 + 1.41457I$		
$a = 0.127888 - 1.155240I$	$-17.2037 + 11.9877I$	0
$b = -1.52575 + 0.31574I$		
$u = 0.65669 - 1.41457I$		
$a = 0.127888 + 1.155240I$	$-17.2037 - 11.9877I$	0
$b = -1.52575 - 0.31574I$		
$u = 0.38128 + 1.53983I$		
$a = 0.017651 - 0.667778I$	$-19.3092 + 0.9583I$	0
$b = -1.58265 + 0.18117I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.38128 - 1.53983I$		
$a = 0.017651 + 0.667778I$	$-19.3092 - 0.9583I$	0
$b = -1.58265 - 0.18117I$		

$$\text{II. } I_1^v = \langle a, b - 1, v^4 - v^3 + v^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ v \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v^3 + v \\ v \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v^3 - v^2 - 1 \\ v^3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -v^2 \\ -v^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -v^2 \\ -v^2 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4v^2 - 5v - 1$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^4$
$c_2, c_7$	$u^4$
$c_3, c_4$	$(u + 1)^4$
$c_5, c_6$	$u^4 + u^3 + 3u^2 + 2u + 1$
$c_8, c_{11}$	$u^4 - u^3 + u^2 + 1$
$c_9, c_{10}$	$u^4 - u^3 + 3u^2 - 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$	$(y - 1)^4$
$c_2, c_7$	$y^4$
$c_5, c_6, c_9$ $c_{10}$	$y^4 + 5y^3 + 7y^2 + 2y + 1$
$c_8, c_{11}$	$y^4 + y^3 + 3y^2 + 2y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.351808 + 0.720342I$		
$a = 0$	$-1.43393 + 1.41510I$	$-0.82145 - 5.62908I$
$b = 1.00000$		
$v = -0.351808 - 0.720342I$		
$a = 0$	$-1.43393 - 1.41510I$	$-0.82145 + 5.62908I$
$b = 1.00000$		
$v = 0.851808 + 0.911292I$		
$a = 0$	$-8.43568 - 3.16396I$	$-5.67855 + 1.65351I$
$b = 1.00000$		
$v = 0.851808 - 0.911292I$		
$a = 0$	$-8.43568 + 3.16396I$	$-5.67855 - 1.65351I$
$b = 1.00000$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^4)(u^{41} - 5u^{40} + \cdots - 3u + 1)$
$c_2, c_7$	$u^4(u^{41} + u^{40} + \cdots + 8u + 16)$
$c_3, c_4$	$((u + 1)^4)(u^{41} - 5u^{40} + \cdots - 3u + 1)$
$c_5, c_6$	$(u^4 + u^3 + 3u^2 + 2u + 1)(u^{41} + 2u^{40} + \cdots - 3u - 1)$
$c_8$	$(u^4 - u^3 + u^2 + 1)(u^{41} + 2u^{40} + \cdots - 20u - 100)$
$c_9, c_{10}$	$(u^4 - u^3 + 3u^2 - 2u + 1)(u^{41} + 2u^{40} + \cdots - 3u - 1)$
$c_{11}$	$(u^4 - u^3 + u^2 + 1)(u^{41} - 12u^{40} + \cdots + 549u - 131)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$	$((y - 1)^4)(y^{41} - 41y^{40} + \cdots - 13y - 1)$
$c_2, c_7$	$y^4(y^{41} + 27y^{40} + \cdots - 960y - 256)$
$c_5, c_6, c_9$ $c_{10}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^{41} + 48y^{40} + \cdots - 7y - 1)$
$c_8$	$(y^4 + y^3 + 3y^2 + 2y + 1)(y^{41} - 24y^{40} + \cdots - 163800y - 10000)$
$c_{11}$	$(y^4 + y^3 + 3y^2 + 2y + 1)(y^{41} - 12y^{40} + \cdots + 112237y - 17161)$