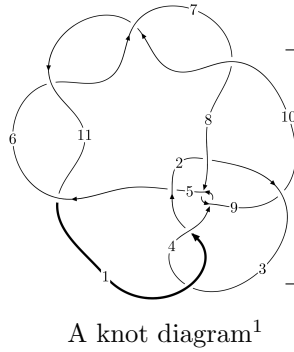
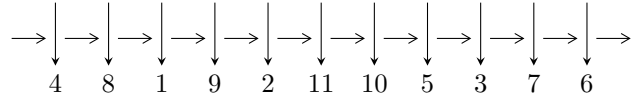


11a₂₉₉ (K11a₂₉₉)



Linearized knot diagram



Solving Sequence

$$6,11 \xrightarrow{c_6} 7 \xrightarrow{c_{11}} 1,4 \xrightarrow{c_1} 2 \xrightarrow{c_3} 3 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \xrightarrow{c_7} 8 \xrightarrow{c_9} 9 \longrightarrow c_2, c_4, c_8$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -3.98094 \times 10^{27} u^{50} + 3.57674 \times 10^{27} u^{49} + \dots + 5.12235 \times 10^{28} b - 4.16694 \times 10^{28}, \\ 4.56338 \times 10^{28} u^{50} + 8.09970 \times 10^{28} u^{49} + \dots + 5.12235 \times 10^{28} a + 2.57618 \times 10^{28}, u^{51} + 2u^{50} + \dots + u^2 - 1 \rangle$$

$$I_2^u = \langle u^2 + 5b + 3u + 4, 4u^2 + 5a - 8u + 6, u^3 - u^2 + 2u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 54 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -3.98 \times 10^{27} u^{50} + 3.58 \times 10^{27} u^{49} + \dots + 5.12 \times 10^{28} b - 4.17 \times 10^{28}, 4.56 \times 10^{28} u^{50} + 8.10 \times 10^{28} u^{49} + \dots + 5.12 \times 10^{28} a + 2.58 \times 10^{28}, u^{51} + 2u^{50} + \dots + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.890878u^{50} - 1.58125u^{49} + \dots + 2.76933u - 0.502929 \\ 0.0777171u^{50} - 0.0698262u^{49} + \dots - 0.830913u + 0.813483 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.911790u^{50} - 1.62215u^{49} + \dots + 3.55461u - 0.444712 \\ 0.00216816u^{50} - 0.149791u^{49} + \dots - 0.143535u + 0.845107 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.848184u^{50} - 1.53135u^{49} + \dots + 1.95617u - 0.527682 \\ 0.0350226u^{50} - 0.119723u^{49} + \dots - 0.0177518u + 0.838236 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.219194u^{50} + 0.0575194u^{49} + \dots - 2.71987u + 0.983462 \\ 0.568042u^{50} + 1.43143u^{49} + \dots - 0.564791u + 0.0862524 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1.21389u^{50} + 2.29120u^{49} + \dots - 2.54183u + 0.639066 \\ -0.214736u^{50} - 0.901043u^{49} + \dots + 1.59632u + 0.327975 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1.21389u^{50} + 2.29120u^{49} + \dots - 2.54183u + 0.639066 \\ -0.214736u^{50} - 0.901043u^{49} + \dots + 1.59632u + 0.327975 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $0.0485520u^{50} - 0.908190u^{49} + \dots - 14.7258u - 8.93442$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_3 | $u^{51} - 4u^{50} + \dots - 49u + 25$ |
| c_2 | $u^{51} + u^{50} + \dots + 380u + 200$ |
| c_4, c_8 | $u^{51} + 2u^{50} + \dots + 4u + 1$ |
| c_5 | $5(5u^{51} - 28u^{50} + \dots - 30u + 857)$ |
| c_6, c_7, c_{10} c_{11} | $u^{51} - 2u^{50} + \dots - u^2 + 1$ |
| c_9 | $5(5u^{51} - 9u^{50} + \dots + 1703u + 239)$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_3 | $y^{51} - 26y^{50} + \dots + 17851y - 625$ |
| c_2 | $y^{51} + 21y^{50} + \dots - 118000y - 40000$ |
| c_4, c_8 | $y^{51} + 28y^{50} + \dots + 2y - 1$ |
| c_5 | $25(25y^{51} + 176y^{50} + \dots - 1375442y - 734449)$ |
| c_6, c_7, c_{10} c_{11} | $y^{51} + 60y^{50} + \dots + 2y - 1$ |
| c_9 | $25(25y^{51} + 739y^{50} + \dots - 637947y - 57121)$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.552527 + 0.820307I$ $a = 0.48391 - 1.52868I$ $b = -1.72817 + 0.85216I$ | $2.62483 + 11.59540I$ | $-7.79067 - 8.85645I$ |
| $u = -0.552527 - 0.820307I$ $a = 0.48391 + 1.52868I$ $b = -1.72817 - 0.85216I$ | $2.62483 - 11.59540I$ | $-7.79067 + 8.85645I$ |
| $u = 0.589306 + 0.788540I$ $a = -0.51919 - 1.38595I$ $b = 1.55822 + 0.77897I$ | $-0.80955 - 5.70999I$ | $-10.32903 + 7.24097I$ |
| $u = 0.589306 - 0.788540I$ $a = -0.51919 + 1.38595I$ $b = 1.55822 - 0.77897I$ | $-0.80955 + 5.70999I$ | $-10.32903 - 7.24097I$ |
| $u = -0.433100 + 0.988087I$ $a = 0.85921 - 1.15463I$ $b = -0.784864 + 0.164197I$ | $3.75291 - 3.24873I$ | $-11.00000 + 0.I$ |
| $u = -0.433100 - 0.988087I$ $a = 0.85921 + 1.15463I$ $b = -0.784864 - 0.164197I$ | $3.75291 + 3.24873I$ | $-11.00000 + 0.I$ |
| $u = -0.376973 + 0.809467I$ $a = 1.031830 - 0.475824I$ $b = -0.043546 - 0.349975I$ | $5.59371 + 5.41403I$ | $-4.14016 - 6.52359I$ |
| $u = -0.376973 - 0.809467I$ $a = 1.031830 + 0.475824I$ $b = -0.043546 + 0.349975I$ | $5.59371 - 5.41403I$ | $-4.14016 + 6.52359I$ |
| $u = 0.249787 + 0.812726I$ $a = -0.469781 - 0.492664I$ $b = -0.095865 + 0.184201I$ | $1.73380 - 1.81855I$ | $-6.35906 + 4.36354I$ |
| $u = 0.249787 - 0.812726I$ $a = -0.469781 + 0.492664I$ $b = -0.095865 - 0.184201I$ | $1.73380 + 1.81855I$ | $-6.35906 - 4.36354I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.493565 + 0.692270I$ $a = 0.247144 - 1.224100I$ $b = -1.21189 + 1.00104I$ | $4.68147 + 1.04951I$ | $-4.16172 - 4.32794I$ |
| $u = -0.493565 - 0.692270I$ $a = 0.247144 + 1.224100I$ $b = -1.21189 - 1.00104I$ | $4.68147 - 1.04951I$ | $-4.16172 + 4.32794I$ |
| $u = 0.773905 + 0.191317I$ $a = -0.320071 - 0.624747I$ $b = 1.381640 - 0.030498I$ | $-2.64708 + 1.15805I$ | $-10.73331 - 5.02870I$ |
| $u = 0.773905 - 0.191317I$ $a = -0.320071 + 0.624747I$ $b = 1.381640 + 0.030498I$ | $-2.64708 - 1.15805I$ | $-10.73331 + 5.02870I$ |
| $u = -0.744224 + 0.089987I$ $a = 0.047354 - 0.638462I$ $b = -1.47794 - 0.27354I$ | $0.42114 - 7.27131I$ | $-10.81656 + 5.67006I$ |
| $u = -0.744224 - 0.089987I$ $a = 0.047354 + 0.638462I$ $b = -1.47794 + 0.27354I$ | $0.42114 + 7.27131I$ | $-10.81656 - 5.67006I$ |
| $u = 0.128736 + 0.681128I$ $a = 1.63090 - 0.76962I$ $b = -1.72989 + 2.00427I$ | $1.377800 + 0.247335I$ | $-11.41702 + 6.59841I$ |
| $u = 0.128736 - 0.681128I$ $a = 1.63090 + 0.76962I$ $b = -1.72989 - 2.00427I$ | $1.377800 - 0.247335I$ | $-11.41702 - 6.59841I$ |
| $u = 0.328726 + 0.602476I$ $a = -0.683354 + 0.933926I$ $b = -1.027660 - 0.198210I$ | $0.09032 - 4.00238I$ | $-9.47119 + 9.47766I$ |
| $u = 0.328726 - 0.602476I$ $a = -0.683354 - 0.933926I$ $b = -1.027660 + 0.198210I$ | $0.09032 + 4.00238I$ | $-9.47119 - 9.47766I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = 0.309159 + 1.281950I$ $a = -0.53813 - 1.48328I$ $b = 0.630951 + 0.896457I$ | $1.88408 - 2.74356I$ | 0 |
| $u = 0.309159 - 1.281950I$ $a = -0.53813 + 1.48328I$ $b = 0.630951 - 0.896457I$ | $1.88408 + 2.74356I$ | 0 |
| $u = -0.235448 + 0.507844I$ $a = 0.06586 + 1.89337I$ $b = 1.226960 - 0.240501I$ | $-1.46138 + 0.98661I$ | $-12.15795 - 1.22039I$ |
| $u = -0.235448 - 0.507844I$ $a = 0.06586 - 1.89337I$ $b = 1.226960 + 0.240501I$ | $-1.46138 - 0.98661I$ | $-12.15795 + 1.22039I$ |
| $u = -0.535402 + 0.073202I$ $a = 0.434598 - 1.044040I$ $b = -0.708461 - 0.403158I$ | $3.00953 + 2.35838I$ | $-8.15249 - 2.65728I$ |
| $u = -0.535402 - 0.073202I$ $a = 0.434598 + 1.044040I$ $b = -0.708461 + 0.403158I$ | $3.00953 - 2.35838I$ | $-8.15249 + 2.65728I$ |
| $u = -0.271262 + 0.396700I$ $a = 0.75415 + 2.38170I$ $b = 0.944727 - 0.152860I$ | $-1.67074 + 1.07820I$ | $-12.01082 - 5.84608I$ |
| $u = -0.271262 - 0.396700I$ $a = 0.75415 - 2.38170I$ $b = 0.944727 + 0.152860I$ | $-1.67074 - 1.07820I$ | $-12.01082 + 5.84608I$ |
| $u = -0.01718 + 1.55667I$ $a = -0.37477 + 2.03786I$ $b = 0.552519 - 1.004140I$ | $5.04838 + 1.69001I$ | 0 |
| $u = -0.01718 - 1.55667I$ $a = -0.37477 - 2.03786I$ $b = 0.552519 + 1.004140I$ | $5.04838 - 1.69001I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.04180 + 1.57969I$ $a = -1.09580 + 1.51782I$ $b = 1.49270 - 0.77222I$ | $5.80181 + 1.83329I$ | 0 |
| $u = -0.04180 - 1.57969I$ $a = -1.09580 - 1.51782I$ $b = 1.49270 + 0.77222I$ | $5.80181 - 1.83329I$ | 0 |
| $u = 0.06969 + 1.58540I$ $a = 0.646529 + 0.973357I$ $b = -1.354660 - 0.387992I$ | $7.57583 - 5.34940I$ | 0 |
| $u = 0.06969 - 1.58540I$ $a = 0.646529 - 0.973357I$ $b = -1.354660 + 0.387992I$ | $7.57583 + 5.34940I$ | 0 |
| $u = 0.339596 + 0.188204I$ $a = -1.55128 + 2.09918I$ $b = -0.402028 + 0.283631I$ | $-1.01423 + 1.50344I$ | $-14.02114 - 0.26378I$ |
| $u = 0.339596 - 0.188204I$ $a = -1.55128 - 2.09918I$ $b = -0.402028 - 0.283631I$ | $-1.01423 - 1.50344I$ | $-14.02114 + 0.26378I$ |
| $u = 0.02693 + 1.61334I$ $a = 3.90639 - 0.28673I$ $b = -3.98695 + 0.78800I$ | $9.33157 - 0.28182I$ | 0 |
| $u = 0.02693 - 1.61334I$ $a = 3.90639 + 0.28673I$ $b = -3.98695 - 0.78800I$ | $9.33157 + 0.28182I$ | 0 |
| $u = -0.15866 + 1.61313I$ $a = 0.90457 - 2.22903I$ $b = -1.33704 + 1.71038I$ | $12.51670 + 3.55318I$ | 0 |
| $u = -0.15866 - 1.61313I$ $a = 0.90457 + 2.22903I$ $b = -1.33704 - 1.71038I$ | $12.51670 - 3.55318I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.10468 + 1.64228I$ | | |
| $a = 0.285194 + 0.100077I$ | $14.0417 + 7.2484I$ | 0 |
| $b = 0.495111 - 0.386510I$ | | |
| $u = -0.10468 - 1.64228I$ | | |
| $a = 0.285194 - 0.100077I$ | $14.0417 - 7.2484I$ | 0 |
| $b = 0.495111 + 0.386510I$ | | |
| $u = 0.08123 + 1.64771I$ | | |
| $a = 0.021744 - 0.179863I$ | $10.29890 - 3.16367I$ | 0 |
| $b = -0.560164 + 0.015522I$ | | |
| $u = 0.08123 - 1.64771I$ | | |
| $a = 0.021744 + 0.179863I$ | $10.29890 + 3.16367I$ | 0 |
| $b = -0.560164 - 0.015522I$ | | |
| $u = 0.17216 + 1.64138I$ | | |
| $a = -1.15226 - 2.05629I$ | $7.44997 - 8.60283I$ | 0 |
| $b = 1.58595 + 1.37531I$ | | |
| $u = 0.17216 - 1.64138I$ | | |
| $a = -1.15226 + 2.05629I$ | $7.44997 + 8.60283I$ | 0 |
| $b = 1.58595 - 1.37531I$ | | |
| $u = -0.16225 + 1.65033I$ | | |
| $a = 1.31880 - 2.12033I$ | $11.0558 + 14.3418I$ | 0 |
| $b = -1.83667 + 1.38127I$ | | |
| $u = -0.16225 - 1.65033I$ | | |
| $a = 1.31880 + 2.12033I$ | $11.0558 - 14.3418I$ | 0 |
| $b = -1.83667 - 1.38127I$ | | |
| $u = -0.08999 + 1.68712I$ | | |
| $a = 0.334351 - 0.580821I$ | $13.10850 - 1.33730I$ | 0 |
| $b = 0.022884 + 0.143685I$ | | |
| $u = -0.08999 - 1.68712I$ | | |
| $a = 0.334351 + 0.580821I$ | $13.10850 + 1.33730I$ | 0 |
| $b = 0.022884 - 0.143685I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = 0.295696$ | | |
| $a = -0.935819$ | -0.590385 | -17.0960 |
| $b = 0.188257$ | | |

$$\text{II. } I_2^u = \langle u^2 + 5b + 3u + 4, 4u^2 + 5a - 8u + 6, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{4}{5}u^2 + \frac{8}{5}u - \frac{6}{5} \\ -\frac{1}{5}u^2 - \frac{1}{5}u - \frac{1}{5} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{4}{5}u^2 + \frac{3}{5}u - \frac{6}{5} \\ -\frac{1}{5}u^2 + \frac{1}{5}u - \frac{1}{5} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{4}{5}u^2 + \frac{3}{5}u - \frac{6}{5} \\ -\frac{1}{5}u^2 + \frac{3}{5}u - \frac{1}{5} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{13}{25}u^2 + \frac{6}{25}u + \frac{8}{25} \\ -\frac{7}{25}u^2 + \frac{9}{25}u - \frac{13}{25} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^2 - u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{4}{25}u^2 + \frac{27}{25}u + \frac{11}{25} \\ \frac{31}{25}u^2 - \frac{22}{25}u + \frac{29}{25} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{4}{25}u^2 + \frac{27}{25}u + \frac{11}{25} \\ \frac{31}{25}u^2 - \frac{22}{25}u + \frac{29}{25} \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -\frac{12}{25}u^2 + \frac{69}{25}u - \frac{408}{25}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------|--------------------------------|
| c_1 | $(u - 1)^3$ |
| c_2 | u^3 |
| c_3 | $(u + 1)^3$ |
| c_4 | $u^3 + u^2 - 1$ |
| c_5 | $5(5u^3 + 7u^2 + 4u + 1)$ |
| c_6, c_7 | $u^3 - u^2 + 2u - 1$ |
| c_8 | $u^3 - u^2 + 1$ |
| c_9 | $5(5u^3 + 4u^2 - u - 1)$ |
| c_{10}, c_{11} | $u^3 + u^2 + 2u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|------------------------------------|
| c_1, c_3 | $(y - 1)^3$ |
| c_2 | y^3 |
| c_4, c_8 | $y^3 - y^2 + 2y - 1$ |
| c_5 | $25(25y^3 - 9y^2 + 2y - 1)$ |
| c_6, c_7, c_{10} c_{11} | $y^3 + 3y^2 + 2y - 1$ |
| c_9 | $25(25y^3 - 26y^2 + 9y - 1)$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = 0.215080 + 1.307140I$ $a = 0.47401 + 1.64160I$ $b = -0.596576 - 0.896741I$ | $1.37919 - 2.82812I$ | $-14.9284 + 3.3378I$ |
| $u = 0.215080 - 1.307140I$ $a = 0.47401 - 1.64160I$ $b = -0.596576 + 0.896741I$ | $1.37919 + 2.82812I$ | $-14.9284 - 3.3378I$ |
| $u = 0.569840$ $a = -0.548030$ $b = -1.20685$ | -2.75839 | -14.9030 |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------------|--|
| c_1 | $((u-1)^3)(u^{51} - 4u^{50} + \dots - 49u + 25)$ |
| c_2 | $u^3(u^{51} + u^{50} + \dots + 380u + 200)$ |
| c_3 | $((u+1)^3)(u^{51} - 4u^{50} + \dots - 49u + 25)$ |
| c_4 | $(u^3 + u^2 - 1)(u^{51} + 2u^{50} + \dots + 4u + 1)$ |
| c_5 | $25(5u^3 + 7u^2 + 4u + 1)(5u^{51} - 28u^{50} + \dots - 30u + 857)$ |
| c_6, c_7 | $(u^3 - u^2 + 2u - 1)(u^{51} - 2u^{50} + \dots - u^2 + 1)$ |
| c_8 | $(u^3 - u^2 + 1)(u^{51} + 2u^{50} + \dots + 4u + 1)$ |
| c_9 | $25(5u^3 + 4u^2 - u - 1)(5u^{51} - 9u^{50} + \dots + 1703u + 239)$ |
| c_{10}, c_{11} | $(u^3 + u^2 + 2u + 1)(u^{51} - 2u^{50} + \dots - u^2 + 1)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_3 | $((y - 1)^3)(y^{51} - 26y^{50} + \dots + 17851y - 625)$ |
| c_2 | $y^3(y^{51} + 21y^{50} + \dots - 118000y - 40000)$ |
| c_4, c_8 | $(y^3 - y^2 + 2y - 1)(y^{51} + 28y^{50} + \dots + 2y - 1)$ |
| c_5 | $625(25y^3 - 9y^2 + 2y - 1)$ $\cdot (25y^{51} + 176y^{50} + \dots - 1375442y - 734449)$ |
| c_6, c_7, c_{10} c_{11} | $(y^3 + 3y^2 + 2y - 1)(y^{51} + 60y^{50} + \dots + 2y - 1)$ |
| c_9 | $625(25y^3 - 26y^2 + 9y - 1)(25y^{51} + 739y^{50} + \dots - 637947y - 57121)$ |