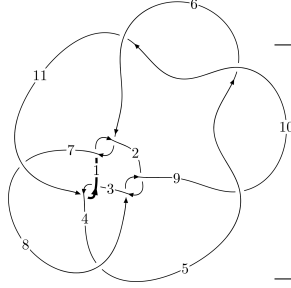
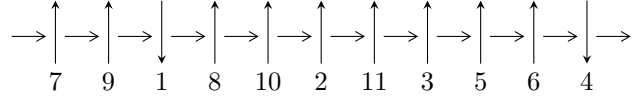


11a₃₂₁ (K11a₃₂₁)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$5,9 \xrightarrow{c_9} 10 \xrightarrow{c_5} 6 \xrightarrow{c_{10}} 3,11 \xrightarrow{c_2} 2 \xrightarrow{c_6} 7 \xrightarrow{c_1} 1 \xrightarrow{c_8} 8 \xrightarrow{c_4} 4 \rightsquigarrow c_3, c_7, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 1073u^{25} + 10099u^{24} + \dots + 16b - 21648, -299u^{25} - 2899u^{24} + \dots + 32a + 7504, \\ u^{26} + 11u^{25} + \dots + 16u - 32 \rangle$$

$$I_2^u = \langle u^3a + u^4 - u^3 - au - u^2 + b - a, u^3a - u^4 + 2u^3 + a^2 - au + 2u^2 - 2a - 4u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

$$I_3^u = \langle -325652548336533a^7u^4 - 216522091497175a^6u^4 + \dots + 461842568426094a - 37300538969198, \\ 2a^7u^4 + 3a^6u^4 + \dots + 63a + 36, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

$$I_4^u = \langle u^{15} - 2u^{14} - 8u^{13} + 16u^{12} + 23u^{11} - 49u^{10} - 30u^9 + 74u^8 + 21u^7 - 63u^6 - 11u^5 + 33u^4 + 3u^3 - 9u^2 + b + \\ - u^{14} + u^{13} + 8u^{12} - 8u^{11} - 24u^{10} + 24u^9 + 36u^8 - 34u^7 - 34u^6 + 25u^5 + 24u^4 - 9u^3 - 10u^2 + a + 3, \\ u^{16} - 9u^{14} + u^{13} + 33u^{12} - 6u^{11} - 64u^{10} + 13u^9 + 73u^8 - 12u^7 - 52u^6 + 4u^5 + 22u^4 - 4u^2 + 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 92 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 1073u^{25} + 10099u^{24} + \dots + 16b - 21648, -299u^{25} - 2899u^{24} + \dots + 32a + 7504, u^{26} + 11u^{25} + \dots + 16u - 32 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{299}{32}u^{25} + \frac{2899}{32}u^{24} + \dots + 301u - \frac{469}{2} \\ -67.0625u^{25} - 631.188u^{24} + \dots - 1534u + 1353 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{2445}{32}u^{25} + \frac{23097}{32}u^{24} + \dots + 1835u - \frac{3175}{2} \\ -67.0625u^{25} - 631.188u^{24} + \dots - 1534u + 1353 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -13.7500u^{25} - 133.250u^{24} + \dots - 383.500u + 320.500 \\ 4u^{25} + 42u^{24} + \dots + \frac{377}{2}u - 136 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1181}{16}u^{25} + \frac{5595}{8}u^{24} + \dots + 1708u - 1515 \\ \frac{107}{16}u^{25} + \frac{871}{16}u^{24} + \dots - 43u - 22 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{39}{4}u^{25} + \frac{365}{4}u^{24} + \dots + 197u - \frac{367}{2} \\ -4u^{25} - 42u^{24} + \dots - \frac{375}{2}u + 136 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{5}{4}u^{25} + \frac{75}{4}u^{24} + \dots + \frac{863}{4}u - 128 \\ \frac{185}{4}u^{25} + \frac{891}{2}u^{24} + \dots + 1245u - 1048 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{5}{4}u^{25} + \frac{75}{4}u^{24} + \dots + \frac{863}{4}u - 128 \\ \frac{185}{4}u^{25} + \frac{891}{2}u^{24} + \dots + 1245u - 1048 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $\frac{333}{2}u^{25} + 1571u^{24} + \dots + 3724u - 3326$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|---|
| c_1, c_2, c_6 c_8 | $u^{26} + 7u^{24} + \dots + 3u - 1$ |
| c_3, c_{11} | $u^{26} - 12u^{25} + \dots - 448u + 32$ |
| c_4, c_7 | $u^{26} - 9u^{24} + \dots - 16u^2 - 1$ |
| c_5, c_9, c_{10} | $u^{26} + 11u^{25} + \dots + 16u - 32$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|--|
| c_1, c_2, c_6 c_8 | $y^{26} + 14y^{25} + \cdots - y + 1$ |
| c_3, c_{11} | $y^{26} + 10y^{25} + \cdots - 27136y + 1024$ |
| c_4, c_7 | $y^{26} - 18y^{25} + \cdots + 32y + 1$ |
| c_5, c_9, c_{10} | $y^{26} - 23y^{25} + \cdots - 5888y + 1024$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.383322 + 0.913347I$ | $-2.65503 + 11.68360I$ | $5.29865 - 8.17521I$ |
| $a = 0.15913 - 1.78657I$ | | |
| $b = -0.55889 - 1.30495I$ | | |
| $u = 0.383322 - 0.913347I$ | $-2.65503 - 11.68360I$ | $5.29865 + 8.17521I$ |
| $a = 0.15913 + 1.78657I$ | | |
| $b = -0.55889 + 1.30495I$ | | |
| $u = -0.828242 + 0.616056I$ | $-1.85940 - 2.41843I$ | $9.7124 + 14.3057I$ |
| $a = 0.43855 + 1.53930I$ | | |
| $b = -0.081709 + 0.666053I$ | | |
| $u = -0.828242 - 0.616056I$ | $-1.85940 + 2.41843I$ | $9.7124 - 14.3057I$ |
| $a = 0.43855 - 1.53930I$ | | |
| $b = -0.081709 - 0.666053I$ | | |
| $u = 0.317740 + 0.989994I$ | $-5.41034 + 5.29072I$ | $3.13484 - 6.09748I$ |
| $a = -0.13580 + 1.61988I$ | | |
| $b = 0.424496 + 1.163430I$ | | |
| $u = 0.317740 - 0.989994I$ | $-5.41034 - 5.29072I$ | $3.13484 + 6.09748I$ |
| $a = -0.13580 - 1.61988I$ | | |
| $b = 0.424496 - 1.163430I$ | | |
| $u = 0.867391 + 0.763321I$ | $-1.25182 - 6.02050I$ | $5.93358 + 4.78066I$ |
| $a = 0.748452 - 0.780722I$ | | |
| $b = 0.380945 - 1.145790I$ | | |
| $u = 0.867391 - 0.763321I$ | $-1.25182 + 6.02050I$ | $5.93358 - 4.78066I$ |
| $a = 0.748452 + 0.780722I$ | | |
| $b = 0.380945 + 1.145790I$ | | |
| $u = 0.604803 + 0.424043I$ | $3.26437 + 1.57845I$ | $12.40306 - 2.05363I$ |
| $a = 0.576639 + 0.245391I$ | | |
| $b = 0.695203 - 0.396515I$ | | |
| $u = 0.604803 - 0.424043I$ | $3.26437 - 1.57845I$ | $12.40306 + 2.05363I$ |
| $a = 0.576639 - 0.245391I$ | | |
| $b = 0.695203 + 0.396515I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $u = 0.155329 + 0.682857I$ $a = -0.12123 - 1.47536I$ $b = -0.595161 - 0.658480I$ | $1.79534 + 1.92657I$ | $9.32234 - 4.27733I$ |
| $u = 0.155329 - 0.682857I$ $a = -0.12123 + 1.47536I$ $b = -0.595161 + 0.658480I$ | $1.79534 - 1.92657I$ | $9.32234 + 4.27733I$ |
| $u = 1.081110 + 0.752925I$ $a = -0.476440 + 0.754455I$ $b = -0.236698 + 1.023340I$ | $-3.21650 + 0.73193I$ | $6.23274 + 2.78423I$ |
| $u = 1.081110 - 0.752925I$ $a = -0.476440 - 0.754455I$ $b = -0.236698 - 1.023340I$ | $-3.21650 - 0.73193I$ | $6.23274 - 2.78423I$ |
| $u = -1.37365 + 0.35020I$ $a = -0.829144 - 1.069810I$ $b = 0.726167 - 0.875974I$ | $6.54594 - 5.84781I$ | $12.9077 + 6.2870I$ |
| $u = -1.37365 - 0.35020I$ $a = -0.829144 + 1.069810I$ $b = 0.726167 + 0.875974I$ | $6.54594 + 5.84781I$ | $12.9077 - 6.2870I$ |
| $u = -1.47715$ $a = -0.340449$ $b = 0.812944$ | 7.01191 | 13.1000 |
| $u = -1.51143 + 0.09637I$ $a = 0.142803 + 0.338489I$ $b = -0.920008 - 0.217229I$ | $10.23750 - 3.38664I$ | $16.0962 + 0.I$ |
| $u = -1.51143 - 0.09637I$ $a = 0.142803 - 0.338489I$ $b = -0.920008 + 0.217229I$ | $10.23750 + 3.38664I$ | $16.0962 + 0.I$ |
| $u = -1.47229 + 0.38599I$ $a = 0.852447 + 0.991797I$ $b = -0.618131 + 1.238700I$ | $0.31031 - 10.20530I$ | $7.00000 + 6.34949I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -1.47229 - 0.38599I$ $a = 0.852447 - 0.991797I$ $b = -0.618131 - 1.238700I$ | $0.31031 + 10.20530I$ | $7.00000 - 6.34949I$ |
| $u = -1.48560 + 0.35379I$ $a = -0.921287 - 1.008460I$ $b = 0.73457 - 1.37086I$ | $3.3294 - 16.2583I$ | $0. + 8.72442I$ |
| $u = -1.48560 - 0.35379I$ $a = -0.921287 + 1.008460I$ $b = 0.73457 + 1.37086I$ | $3.3294 + 16.2583I$ | $0. - 8.72442I$ |
| $u = 0.423114$ $a = 0.218860$ $b = -0.331232$ | 0.617191 | 16.1820 |
| $u = -1.71146 + 0.07064I$ $a = -0.123322 - 0.123466I$ $b = -0.191640 - 0.759101I$ | $8.12481 + 2.87714I$ | 0 |
| $u = -1.71146 - 0.07064I$ $a = -0.123322 + 0.123466I$ $b = -0.191640 + 0.759101I$ | $8.12481 - 2.87714I$ | 0 |

$$\text{II. } I_2^u = \langle u^3 a + u^4 - u^3 - au - u^2 + b - a, u^3 a - u^4 + 2u^3 + a^2 - au + 2u^2 - 2a - 4u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -u^3 a - u^4 + u^3 + au + u^2 + a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 a + u^4 - u^3 - au - u^2 \\ -u^3 a - u^4 + u^3 + au + u^2 + a \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^4 a - u^3 a - u^2 a - u^3 - u^2 + 3u \\ u^2 - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^4 + u^2 a + u^3 + u^2 - a - u + 1 \\ -u^4 a + 2u^2 a - u^2 + u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 a + au + a + u - 1 \\ -u^4 - u^2 a + 3u^2 - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 a - u^4 + 2au + 2u^2 - 1 \\ -a - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 a - u^4 + 2au + 2u^2 - 1 \\ -a - u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-8u^3 + 16u + 10$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|---|
| c_1, c_2, c_6 c_8 | $u^{10} + 2u^9 + \cdots + 8u + 17$ |
| c_3, c_{11} | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$ |
| c_4, c_7 | $u^{10} + 2u^9 + 3u^8 + 4u^6 + 15u^4 - 16u^3 + 33u^2 - 20u + 7$ |
| c_5, c_9, c_{10} | $(u^5 - u^4 - 2u^3 + u^2 + u + 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|--|
| c_1, c_2, c_6 c_8 | $y^{10} + 6y^9 + \cdots + 786y + 289$ |
| c_3, c_{11} | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$ |
| c_4, c_7 | $y^{10} + 2y^9 + \cdots + 62y + 49$ |
| c_5, c_9, c_{10} | $(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -1.21774$ $a = 1.29401 + 0.59312I$ $b = -0.466896 + 0.941886I$ | -0.132640 | 4.96230 |
| $u = -1.21774$ $a = 1.29401 - 0.59312I$ $b = -0.466896 - 0.941886I$ | -0.132640 | 4.96230 |
| $u = -0.309916 + 0.549911I$ $a = -0.422523 - 1.226950I$ $b = 0.617609 - 1.263280I$ | $-4.27660 - 3.06116I$ | $3.03023 + 8.86130I$ |
| $u = -0.309916 + 0.549911I$ $a = 1.86122 + 1.78470I$ $b = -0.060281 + 1.331670I$ | $-4.27660 - 3.06116I$ | $3.03023 + 8.86130I$ |
| $u = -0.309916 - 0.549911I$ $a = -0.422523 + 1.226950I$ $b = 0.617609 + 1.263280I$ | $-4.27660 + 3.06116I$ | $3.03023 - 8.86130I$ |
| $u = -0.309916 - 0.549911I$ $a = 1.86122 - 1.78470I$ $b = -0.060281 - 1.331670I$ | $-4.27660 + 3.06116I$ | $3.03023 - 8.86130I$ |
| $u = 1.41878 + 0.21917I$ $a = 1.00071 - 1.33190I$ $b = -0.547449 - 1.293710I$ | $6.81032 + 8.80167I$ | $11.48863 - 6.99717I$ |
| $u = 1.41878 + 0.21917I$ $a = -0.233411 + 0.238092I$ $b = 1.45702 - 0.30917I$ | $6.81032 + 8.80167I$ | $11.48863 - 6.99717I$ |
| $u = 1.41878 - 0.21917I$ $a = 1.00071 + 1.33190I$ $b = -0.547449 + 1.293710I$ | $6.81032 - 8.80167I$ | $11.48863 + 6.99717I$ |
| $u = 1.41878 - 0.21917I$ $a = -0.233411 - 0.238092I$ $b = 1.45702 + 0.30917I$ | $6.81032 - 8.80167I$ | $11.48863 + 6.99717I$ |

$$\text{III. } I_3^u = \langle -3.26 \times 10^{14} a^7 u^4 - 2.17 \times 10^{14} a^6 u^4 + \dots + 4.62 \times 10^{14} a - 3.73 \times 10^{13}, 2a^7 u^4 + 3a^6 u^4 + \dots + 63a + 36, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1.78373a^7 u^4 + 1.18598a^6 u^4 + \dots - 2.52970a + 0.204311 \\ a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.78373a^7 u^4 - 1.18598a^6 u^4 + \dots + 3.52970a - 0.204311 \\ 1.78373a^7 u^4 + 1.18598a^6 u^4 + \dots - 2.52970a + 0.204311 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.513662a^7 u^4 - 0.154648a^6 u^4 + \dots + 1.00013a + 0.425409 \\ 0.452703a^7 u^4 + 0.296357a^6 u^4 + \dots - 0.697071a - 0.200491 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.431150a^7 u^4 - 0.236002a^6 u^4 + \dots + 1.67334a - 0.859074 \\ 1.74389a^7 u^4 + 0.846631a^6 u^4 + \dots - 3.09895a + 1.01675 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.158932a^7 u^4 + 0.0166854a^6 u^4 + \dots + 0.0570178a + 1.29770 \\ 0.0505083a^7 u^4 - 0.709704a^6 u^4 + \dots + 0.671481a + 1.16410 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.381857a^7 u^4 + 0.0243899a^6 u^4 + \dots + 1.70012a + 0.510808 \\ -1.20422a^7 u^4 - 0.158188a^6 u^4 + \dots + 1.44338a - 0.285170 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.381857a^7 u^4 + 0.0243899a^6 u^4 + \dots + 1.70012a + 0.510808 \\ -1.20422a^7 u^4 - 0.158188a^6 u^4 + \dots + 1.44338a - 0.285170 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{52949256522924}{91283920109957} a^7 u^4 + \frac{90213951943262}{91283920109957} a^6 u^4 + \dots + \frac{111428618111312}{91283920109957} a + \frac{970857959574538}{91283920109957}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|---------------------------------------|
| c_1, c_2, c_6 c_8 | $u^{40} - u^{39} + \dots + 112u + 32$ |
| c_3, c_{11} | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)^8$ |
| c_4, c_7 | $u^{40} - 7u^{39} + \dots + 80u + 32$ |
| c_5, c_9, c_{10} | $(u^5 - u^4 - 2u^3 + u^2 + u + 1)^8$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|---|
| c_1, c_2, c_6 c_8 | $y^{40} + 29y^{39} + \cdots + 8960y + 1024$ |
| c_3, c_{11} | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^8$ |
| c_4, c_7 | $y^{40} + 5y^{39} + \cdots + 9984y + 1024$ |
| c_5, c_9, c_{10} | $(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^8$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -1.21774$ $a = -1.207790 + 0.238764I$ $b = 1.020160 + 0.833032I$ | $3.33884 + 4.40083I$ | $8.22546 - 3.49859I$ |
| $u = -1.21774$ $a = -1.207790 - 0.238764I$ $b = 1.020160 - 0.833032I$ | $3.33884 - 4.40083I$ | $8.22546 + 3.49859I$ |
| $u = -1.21774$ $a = 0.256260 + 0.476517I$ $b = -0.23486 + 1.89553I$ | $-2.20462 - 1.53058I$ | $3.99626 + 4.43065I$ |
| $u = -1.21774$ $a = 0.256260 - 0.476517I$ $b = -0.23486 - 1.89553I$ | $-2.20462 + 1.53058I$ | $3.99626 - 4.43065I$ |
| $u = -1.21774$ $a = 0.40240 + 1.64523I$ $b = -0.00279 + 1.47385I$ | $-2.20462 + 1.53058I$ | $3.99626 - 4.43065I$ |
| $u = -1.21774$ $a = 0.40240 - 1.64523I$ $b = -0.00279 - 1.47385I$ | $-2.20462 - 1.53058I$ | $3.99626 + 4.43065I$ |
| $u = -1.21774$ $a = -1.80751 + 0.70455I$ $b = 0.067800 + 0.664970I$ | $3.33884 - 4.40083I$ | $8.22546 + 3.49859I$ |
| $u = -1.21774$ $a = -1.80751 - 0.70455I$ $b = 0.067800 - 0.664970I$ | $3.33884 + 4.40083I$ | $8.22546 - 3.49859I$ |
| $u = -0.309916 + 0.549911I$ $a = -0.614210 - 0.356072I$ $b = -1.112460 - 0.022805I$ | $1.26686 - 5.93141I$ | $7.25943 + 7.92923I$ |
| $u = -0.309916 + 0.549911I$ $a = -0.077663 + 0.645448I$ $b = 0.540737 - 0.024289I$ | $-2.20462 - 1.53058I$ | $3.99626 + 4.43065I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.309916 + 0.549911I$ $a = -0.69063 - 1.44845I$ $b = -0.631776 - 0.881136I$ | $1.26686 + 2.87025I$ | $7.25943 + 0.93206I$ |
| $u = -0.309916 + 0.549911I$ $a = 0.72433 + 1.72452I$ $b = -0.28691 + 1.51546I$ | -4.27660 | $3.03023 + 0.I$ |
| $u = -0.309916 + 0.549911I$ $a = -1.94655 - 0.78265I$ $b = -0.060228 - 1.074110I$ | -4.27660 | $3.03023 + 0.I$ |
| $u = -0.309916 + 0.549911I$ $a = 0.72536 - 2.06070I$ $b = 0.330888 - 0.359958I$ | $1.26686 + 2.87025I$ | $7.25943 + 0.93206I$ |
| $u = -0.309916 + 0.549911I$ $a = 0.50296 + 2.30075I$ $b = -0.127790 + 1.025730I$ | $-2.20462 - 1.53058I$ | $3.99626 + 4.43065I$ |
| $u = -0.309916 + 0.549911I$ $a = -0.41156 - 2.99999I$ $b = 0.451097 - 1.069650I$ | $1.26686 - 5.93141I$ | $7.25943 + 7.92923I$ |
| $u = -0.309916 - 0.549911I$ $a = -0.614210 + 0.356072I$ $b = -1.112460 + 0.022805I$ | $1.26686 + 5.93141I$ | $7.25943 - 7.92923I$ |
| $u = -0.309916 - 0.549911I$ $a = -0.077663 - 0.645448I$ $b = 0.540737 + 0.024289I$ | $-2.20462 + 1.53058I$ | $3.99626 - 4.43065I$ |
| $u = -0.309916 - 0.549911I$ $a = -0.69063 + 1.44845I$ $b = -0.631776 + 0.881136I$ | $1.26686 - 2.87025I$ | $7.25943 - 0.93206I$ |
| $u = -0.309916 - 0.549911I$ $a = 0.72433 - 1.72452I$ $b = -0.28691 - 1.51546I$ | -4.27660 | $3.03023 + 0.I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.309916 - 0.549911I$ $a = -1.94655 + 0.78265I$ $b = -0.060228 + 1.074110I$ | -4.27660 | $3.03023 + 0.I$ |
| $u = -0.309916 - 0.549911I$ $a = 0.72536 + 2.06070I$ $b = 0.330888 + 0.359958I$ | $1.26686 - 2.87025I$ | $7.25943 - 0.93206I$ |
| $u = -0.309916 - 0.549911I$ $a = 0.50296 - 2.30075I$ $b = -0.127790 - 1.025730I$ | $-2.20462 + 1.53058I$ | $3.99626 - 4.43065I$ |
| $u = -0.309916 - 0.549911I$ $a = -0.41156 + 2.99999I$ $b = 0.451097 + 1.069650I$ | $1.26686 + 5.93141I$ | $7.25943 - 7.92923I$ |
| $u = 1.41878 + 0.21917I$ $a = -0.862919 + 0.408494I$ $b = 0.68021 + 1.39772I$ | $1.26686 + 2.87025I$ | $7.25943 + 0.93206I$ |
| $u = 1.41878 + 0.21917I$ $a = 0.787041 - 0.329401I$ $b = -1.02988 - 1.04062I$ | $1.26686 + 5.93141I$ | $7.25943 - 7.92923I$ |
| $u = 1.41878 + 0.21917I$ $a = 1.194210 + 0.076658I$ $b = -0.161461 - 0.775177I$ | $1.26686 + 2.87025I$ | $7.25943 + 0.93206I$ |
| $u = 1.41878 + 0.21917I$ $a = 0.407015 - 1.193670I$ $b = -0.464952 - 0.997444I$ | 6.81032 | $11.48863 + 0.I$ |
| $u = 1.41878 + 0.21917I$ $a = -0.808970 + 1.033880I$ $b = 0.427482 + 1.218940I$ | $3.33884 + 4.40083I$ | $8.22546 - 3.49859I$ |
| $u = 1.41878 + 0.21917I$ $a = -1.37363 + 0.36155I$ $b = 0.228681 + 1.161970I$ | $1.26686 + 5.93141I$ | $7.25943 - 7.92923I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = 1.41878 + 0.21917I$ $a = 0.307395 - 0.017583I$ $b = -0.982401 + 0.242528I$ | $3.33884 + 4.40083I$ | $8.22546 - 3.49859I$ |
| $u = 1.41878 + 0.21917I$ $a = -0.0055411 - 0.0806818I$ $b = 0.848456 - 0.805185I$ | 6.81032 | $11.48863 + 0.I$ |
| $u = 1.41878 - 0.21917I$ $a = -0.862919 - 0.408494I$ $b = 0.68021 - 1.39772I$ | $1.26686 - 2.87025I$ | $7.25943 - 0.93206I$ |
| $u = 1.41878 - 0.21917I$ $a = 0.787041 + 0.329401I$ $b = -1.02988 + 1.04062I$ | $1.26686 - 5.93141I$ | $7.25943 + 7.92923I$ |
| $u = 1.41878 - 0.21917I$ $a = 1.194210 - 0.076658I$ $b = -0.161461 + 0.775177I$ | $1.26686 - 2.87025I$ | $7.25943 - 0.93206I$ |
| $u = 1.41878 - 0.21917I$ $a = 0.407015 + 1.193670I$ $b = -0.464952 + 0.997444I$ | 6.81032 | $11.48863 + 0.I$ |
| $u = 1.41878 - 0.21917I$ $a = -0.808970 - 1.033880I$ $b = 0.427482 - 1.218940I$ | $3.33884 - 4.40083I$ | $8.22546 + 3.49859I$ |
| $u = 1.41878 - 0.21917I$ $a = -1.37363 - 0.36155I$ $b = 0.228681 - 1.161970I$ | $1.26686 - 5.93141I$ | $7.25943 + 7.92923I$ |
| $u = 1.41878 - 0.21917I$ $a = 0.307395 + 0.017583I$ $b = -0.982401 - 0.242528I$ | $3.33884 - 4.40083I$ | $8.22546 + 3.49859I$ |
| $u = 1.41878 - 0.21917I$ $a = -0.0055411 + 0.0806818I$ $b = 0.848456 + 0.805185I$ | 6.81032 | $11.48863 + 0.I$ |

IV.

$$I_4^u = \langle u^{15} - 2u^{14} + \dots + b + 2, -u^{14} + u^{13} + \dots + a + 3, u^{16} - 9u^{14} + \dots - 4u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{14} - u^{13} + \dots + 10u^2 - 3 \\ -u^{15} + 2u^{14} + \dots + 9u^2 - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{15} - u^{14} + \dots + u^2 - 1 \\ -u^{15} + 2u^{14} + \dots + 9u^2 - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{14} - u^{13} + \dots - u + 2 \\ u^{13} - 7u^{11} + \dots + 3u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^{15} - u^{14} + \dots - 3u + 1 \\ 2u^{15} - 2u^{14} + \dots - u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{14} + 8u^{12} + \dots - 12u^2 + 2 \\ u^{13} - 7u^{11} + \dots + 2u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{13} + 7u^{11} - u^{10} - 18u^9 + 4u^8 + 21u^7 - 4u^6 - 12u^5 + 2u^3 + u^2 + 3u \\ -u^{15} + 2u^{14} + \dots + 3u - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{13} + 7u^{11} - u^{10} - 18u^9 + 4u^8 + 21u^7 - 4u^6 - 12u^5 + 2u^3 + u^2 + 3u \\ -u^{15} + 2u^{14} + \dots + 3u - 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $u^{15} - 5u^{14} - 11u^{13} + 38u^{12} + 42u^{11} - 112u^{10} - 77u^9 + 161u^8 + 82u^7 - 122u^6 - 63u^5 + 48u^4 + 28u^3 + 2u + 5$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1, c_8 | $u^{16} + 8u^{14} + \dots - u + 1$ |
| c_2, c_6 | $u^{16} + 8u^{14} + \dots + u + 1$ |
| c_3 | $u^{16} + 3u^{15} + \dots + 5u^2 + 1$ |
| c_4, c_7 | $u^{16} - 3u^{13} - u^{12} - u^{11} + 8u^8 + 2u^7 + 6u^6 + 3u^5 + 10u^4 + 3u^2 + 1$ |
| c_5 | $u^{16} - 9u^{14} + \dots - 4u^2 + 1$ |
| c_9, c_{10} | $u^{16} - 9u^{14} + \dots - 4u^2 + 1$ |
| c_{11} | $u^{16} - 3u^{15} + \dots + 5u^2 + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|--|
| c_1, c_2, c_6 c_8 | $y^{16} + 16y^{15} + \cdots + 13y + 1$ |
| c_3, c_{11} | $y^{16} + 7y^{15} + \cdots + 10y + 1$ |
| c_4, c_7 | $y^{16} - 2y^{14} + \cdots + 6y + 1$ |
| c_5, c_9, c_{10} | $y^{16} - 18y^{15} + \cdots - 8y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.932576 + 0.558604I$ $a = 0.83677 - 1.43673I$ $b = -0.031814 - 0.697076I$ | $-2.00312 + 2.11071I$ | $-0.36261 + 5.84578I$ |
| $u = 0.932576 - 0.558604I$ $a = 0.83677 + 1.43673I$ $b = -0.031814 + 0.697076I$ | $-2.00312 - 2.11071I$ | $-0.36261 - 5.84578I$ |
| $u = -0.758635 + 0.439917I$ $a = -0.543641 - 0.719000I$ $b = 0.033972 - 1.283280I$ | $-4.35479 - 2.08547I$ | $2.28739 + 3.71145I$ |
| $u = -0.758635 - 0.439917I$ $a = -0.543641 + 0.719000I$ $b = 0.033972 + 1.283280I$ | $-4.35479 + 2.08547I$ | $2.28739 - 3.71145I$ |
| $u = -1.270170 + 0.042100I$ $a = -0.117828 - 1.114430I$ $b = -0.13344 - 1.70790I$ | $-1.36561 + 1.03179I$ | $13.09233 + 0.83056I$ |
| $u = -1.270170 - 0.042100I$ $a = -0.117828 + 1.114430I$ $b = -0.13344 + 1.70790I$ | $-1.36561 - 1.03179I$ | $13.09233 - 0.83056I$ |
| $u = 1.299950 + 0.158892I$ $a = -1.49957 + 0.33616I$ $b = 0.717514 + 0.694169I$ | $4.26074 + 5.75964I$ | $11.30648 - 7.65537I$ |
| $u = 1.299950 - 0.158892I$ $a = -1.49957 - 0.33616I$ $b = 0.717514 - 0.694169I$ | $4.26074 - 5.75964I$ | $11.30648 + 7.65537I$ |
| $u = 1.44241 + 0.18942I$ $a = 0.942839 - 0.151798I$ $b = -0.559613 - 1.118820I$ | $1.52375 + 4.32708I$ | $9.46348 - 3.89019I$ |
| $u = 1.44241 - 0.18942I$ $a = 0.942839 + 0.151798I$ $b = -0.559613 + 1.118820I$ | $1.52375 - 4.32708I$ | $9.46348 + 3.89019I$ |

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.389768 + 0.361348I$ | | |
| $a = -1.42793 - 0.61604I$ | $-4.35506 - 1.95343I$ | $2.10403 + 1.81382I$ |
| $b = 0.199143 - 1.346600I$ | | |
| $u = -0.389768 - 0.361348I$ | | |
| $a = -1.42793 + 0.61604I$ | $-4.35506 + 1.95343I$ | $2.10403 - 1.81382I$ |
| $b = 0.199143 + 1.346600I$ | | |
| $u = 0.380311 + 0.321242I$ | | |
| $a = -1.37704 + 2.58113I$ | $1.00222 - 3.96560I$ | $4.29089 + 5.86867I$ |
| $b = -0.462275 + 0.600749I$ | | |
| $u = 0.380311 - 0.321242I$ | | |
| $a = -1.37704 - 2.58113I$ | $1.00222 + 3.96560I$ | $4.29089 - 5.86867I$ |
| $b = -0.462275 - 0.600749I$ | | |
| $u = -1.63668 + 0.04505I$ | | |
| $a = 0.186402 + 0.341093I$ | $8.58175 + 2.59504I$ | $15.8180 + 1.0523I$ |
| $b = 0.236509 + 0.446950I$ | | |
| $u = -1.63668 - 0.04505I$ | | |
| $a = 0.186402 - 0.341093I$ | $8.58175 - 2.59504I$ | $15.8180 - 1.0523I$ |
| $b = 0.236509 - 0.446950I$ | | |

V. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1, c_8 | $(u^{10} + 2u^9 + \dots + 8u + 17)(u^{16} + 8u^{14} + \dots - u + 1)$ $\cdot (u^{26} + 7u^{24} + \dots + 3u - 1)(u^{40} - u^{39} + \dots + 112u + 32)$ |
| c_2, c_6 | $(u^{10} + 2u^9 + \dots + 8u + 17)(u^{16} + 8u^{14} + \dots + u + 1)$ $\cdot (u^{26} + 7u^{24} + \dots + 3u - 1)(u^{40} - u^{39} + \dots + 112u + 32)$ |
| c_3 | $((u^5 + u^4 + 2u^3 + u^2 + u + 1)^{10})(u^{16} + 3u^{15} + \dots + 5u^2 + 1)$ $\cdot (u^{26} - 12u^{25} + \dots - 448u + 32)$ |
| c_4, c_7 | $(u^{10} + 2u^9 + 3u^8 + 4u^6 + 15u^4 - 16u^3 + 33u^2 - 20u + 7)$ $\cdot (u^{16} - 3u^{13} - u^{12} - u^{11} + 8u^8 + 2u^7 + 6u^6 + 3u^5 + 10u^4 + 3u^2 + 1)$ $\cdot (u^{26} - 9u^{24} + \dots - 16u^2 - 1)(u^{40} - 7u^{39} + \dots + 80u + 32)$ |
| c_5 | $((u^5 - u^4 - 2u^3 + u^2 + u + 1)^{10})(u^{16} - 9u^{14} + \dots - 4u^2 + 1)$ $\cdot (u^{26} + 11u^{25} + \dots + 16u - 32)$ |
| c_9, c_{10} | $((u^5 - u^4 - 2u^3 + u^2 + u + 1)^{10})(u^{16} - 9u^{14} + \dots - 4u^2 + 1)$ $\cdot (u^{26} + 11u^{25} + \dots + 16u - 32)$ |
| c_{11} | $((u^5 + u^4 + 2u^3 + u^2 + u + 1)^{10})(u^{16} - 3u^{15} + \dots + 5u^2 + 1)$ $\cdot (u^{26} - 12u^{25} + \dots - 448u + 32)$ |

VI. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------|---|
| c_1, c_2, c_6 c_8 | $(y^{10} + 6y^9 + \dots + 786y + 289)(y^{16} + 16y^{15} + \dots + 13y + 1)$ $\cdot (y^{26} + 14y^{25} + \dots - y + 1)(y^{40} + 29y^{39} + \dots + 8960y + 1024)$ |
| c_3, c_{11} | $((y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^{10})(y^{16} + 7y^{15} + \dots + 10y + 1)$ $\cdot (y^{26} + 10y^{25} + \dots - 27136y + 1024)$ |
| c_4, c_7 | $(y^{10} + 2y^9 + \dots + 62y + 49)(y^{16} - 2y^{14} + \dots + 6y + 1)$ $\cdot (y^{26} - 18y^{25} + \dots + 32y + 1)(y^{40} + 5y^{39} + \dots + 9984y + 1024)$ |
| c_5, c_9, c_{10} | $((y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^{10})(y^{16} - 18y^{15} + \dots - 8y + 1)$ $\cdot (y^{26} - 23y^{25} + \dots - 5888y + 1024)$ |