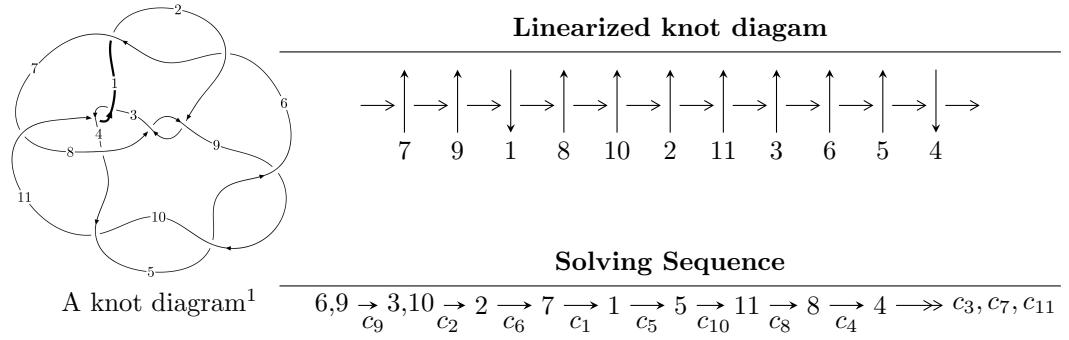


## $11a_{324}$ ( $K11a_{324}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 5u^{20} - 59u^{19} + \dots + 16b + 720, -35u^{20} + 367u^{19} + \dots + 32a - 1520, u^{21} - 11u^{20} + \dots + 368u - 32 \rangle \\
 I_2^u &= \langle -6.48197 \times 10^{26}a^9u^3 - 2.24957 \times 10^{27}a^8u^3 + \dots + 6.21716 \times 10^{28}a + 6.82138 \times 10^{28}, \\
 &\quad 2a^9u^3 - 3a^8u^3 + \dots - 72a + 3, u^4 + u^3 + 3u^2 + 2u + 1 \rangle \\
 I_3^u &= \langle -u^6 - 4u^4 + u^3 - 4u^2 + b + u, -u^6 - u^5 - 4u^4 - 3u^3 - 3u^2 + a - 3u + 1, \\
 &\quad u^{12} + 8u^{10} - u^9 + 24u^8 - 4u^7 + 32u^6 - 4u^5 + 16u^4 + u^2 + 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 73 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 5u^{20} - 59u^{19} + \cdots + 16b + 720, -35u^{20} + 367u^{19} + \cdots + 32a - 1520, u^{21} - 11u^{20} + \cdots + 368u - 32 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1.09375u^{20} - 11.4688u^{19} + \cdots - 488.500u + 47.5000 \\ -\frac{5}{16}u^{20} + \frac{59}{16}u^{19} + \cdots + 425u - 45 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1.40625u^{20} - 15.1563u^{19} + \cdots - 913.500u + 92.5000 \\ -\frac{5}{16}u^{20} + \frac{59}{16}u^{19} + \cdots + 425u - 45 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -\frac{5}{4}u^{20} + \frac{51}{4}u^{19} + \cdots + 360u - \frac{63}{2} \\ u^{20} - \frac{21}{2}u^{19} + \cdots - \frac{855}{2}u + 40 \end{pmatrix} \\ a_1 &= \begin{pmatrix} \frac{27}{16}u^{20} - \frac{139}{8}u^{19} + \cdots - 939u + 95 \\ -\frac{23}{16}u^{20} + \frac{231}{16}u^{19} + \cdots + 456u - 44 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} \frac{1}{4}u^{20} - \frac{9}{4}u^{19} + \cdots + \frac{137}{2}u - \frac{15}{2} \\ -u^{20} + \frac{21}{2}u^{19} + \cdots + \frac{857}{2}u - 40 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -\frac{3}{4}u^{20} + \frac{15}{2}u^{19} + \cdots + \frac{763}{4}u - 16 \\ \frac{1}{4}u^{20} - \frac{9}{4}u^{19} + \cdots - 143u + 16 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -\frac{3}{4}u^{20} + \frac{15}{2}u^{19} + \cdots + \frac{763}{4}u - 16 \\ \frac{1}{4}u^{20} - \frac{9}{4}u^{19} + \cdots - 143u + 16 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** =  $-1$

$$\begin{aligned} \text{(iii) Cusp Shapes} &= \\ \frac{1}{2}u^{19} - \frac{9}{2}u^{18} + \frac{51}{2}u^{17} - \frac{209}{2}u^{16} + 340u^{15} - \frac{1825}{2}u^{14} + 2073u^{13} - \frac{8087}{2}u^{12} + 6835u^{11} - 10051u^{10} + \\ \frac{25731}{2}u^9 - \frac{28567}{2}u^8 + 13650u^7 - \frac{22155}{2}u^6 + 7480u^5 - 4054u^4 + \frac{3327}{2}u^3 - 455u^2 + 52u + 18 \end{aligned}$$

**(iv) u-Polynomials at the component**

| Crossings                | u-Polynomials at each crossing           |
|--------------------------|--|
| $c_1, c_2, c_6$<br>$c_8$ | $u^{21} + 10u^{19} + \cdots + 2u - 1$    |
| $c_3, c_{11}$            | $u^{21} - 13u^{20} + \cdots + 208u - 16$ |
| $c_4, c_7$               | $u^{21} + u^{19} + \cdots - 2u^2 - 1$    |
| $c_5, c_9, c_{10}$       | $u^{21} - 11u^{20} + \cdots + 368u - 32$ |

**(v) Riley Polynomials at the component**

| Crossings                | Riley Polynomials at each crossing          |
|--------------------------|---|
| $c_1, c_2, c_6$<br>$c_8$ | $y^{21} + 20y^{20} + \cdots + 10y - 1$      |
| $c_3, c_{11}$            | $y^{21} + 13y^{20} + \cdots + 3968y - 256$  |
| $c_4, c_7$               | $y^{21} + 2y^{20} + \cdots - 4y - 1$        |
| $c_5, c_9, c_{10}$       | $y^{21} + 21y^{20} + \cdots + 4864y - 1024$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.833412 + 0.782147I$  |                                       |                       |
| $a = 0.687594 - 0.745251I$  | $-3.62928 + 10.88750I$                | $3.73824 - 7.98574I$  |
| $b = -0.40300 - 1.39208I$   |                                       |                       |
| $u = 0.833412 - 0.782147I$  |                                       |                       |
| $a = 0.687594 + 0.745251I$  | $-3.62928 - 10.88750I$                | $3.73824 + 7.98574I$  |
| $b = -0.40300 + 1.39208I$   |                                       |                       |
| $u = 1.112700 + 0.364278I$  |                                       |                       |
| $a = 0.359904 - 0.202646I$  | $-2.28517 - 4.65043I$                 | $4.06472 + 5.66819I$  |
| $b = 0.131151 - 1.261410I$  |                                       |                       |
| $u = 1.112700 - 0.364278I$  |                                       |                       |
| $a = 0.359904 + 0.202646I$  | $-2.28517 + 4.65043I$                 | $4.06472 - 5.66819I$  |
| $b = 0.131151 + 1.261410I$  |                                       |                       |
| $u = 0.344675 + 0.678605I$  |                                       |                       |
| $a = 0.431309 - 0.926685I$  | $1.84838 + 1.63594I$                  | $8.69775 - 4.82521I$  |
| $b = -0.592900 - 0.573194I$ |                                       |                       |
| $u = 0.344675 - 0.678605I$  |                                       |                       |
| $a = 0.431309 + 0.926685I$  | $1.84838 - 1.63594I$                  | $8.69775 + 4.82521I$  |
| $b = -0.592900 + 0.573194I$ |                                       |                       |
| $u = 0.133089 + 1.297270I$  |                                       |                       |
| $a = 0.112115 + 0.615559I$  | $-3.40974 + 1.83530I$                 | $7.00245 - 4.90716I$  |
| $b = 0.400211 + 0.336613I$  |                                       |                       |
| $u = 0.133089 - 1.297270I$  |                                       |                       |
| $a = 0.112115 - 0.615559I$  | $-3.40974 - 1.83530I$                 | $7.00245 + 4.90716I$  |
| $b = 0.400211 - 0.336613I$  |                                       |                       |
| $u = 0.609486 + 0.268410I$  |                                       |                       |
| $a = -0.040658 + 0.537694I$ | $3.15197 + 1.79452I$                  | $11.79217 - 1.79291I$ |
| $b = 0.672784 - 0.348826I$  |                                       |                       |
| $u = 0.609486 - 0.268410I$  |                                       |                       |
| $a = -0.040658 - 0.537694I$ | $3.15197 - 1.79452I$                  | $11.79217 + 1.79291I$ |
| $b = 0.672784 + 0.348826I$  |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 1.039590 + 0.860809I$  | $-6.77144 + 3.85307I$                 | $-1.71548 - 7.56695I$  |
| $a = -0.542621 + 0.649922I$ |                                       |                        |
| $b = 0.181872 + 1.313600I$  |                                       |                        |
| $u = 1.039590 - 0.860809I$  | $-6.77144 - 3.85307I$                 | $-1.71548 + 7.56695I$  |
| $a = -0.542621 - 0.649922I$ |                                       |                        |
| $b = 0.181872 - 1.313600I$  |                                       |                        |
| $u = 0.221176 + 1.373870I$  | $-2.03502 + 4.78161I$                 | $6.69466 - 0.24839I$   |
| $a = -0.661614 - 0.256686I$ |                                       |                        |
| $b = -0.596408 + 0.187921I$ |                                       |                        |
| $u = 0.221176 - 1.373870I$  | $-2.03502 - 4.78161I$                 | $6.69466 + 0.24839I$   |
| $a = -0.661614 + 0.256686I$ |                                       |                        |
| $b = -0.596408 - 0.187921I$ |                                       |                        |
| $u = 0.400789$              |                                       |                        |
| $a = 0.530955$              | 0.646030                              | 15.4450                |
| $b = -0.355136$             |                                       |                        |
| $u = 0.26372 + 1.64197I$    | $-11.6624 + 15.0339I$                 | $2.04142 - 7.27394I$   |
| $a = -0.42059 + 1.78410I$   |                                       |                        |
| $b = 0.57970 + 1.59171I$    |                                       |                        |
| $u = 0.26372 - 1.64197I$    | $-11.6624 - 15.0339I$                 | $2.04142 + 7.27394I$   |
| $a = -0.42059 - 1.78410I$   |                                       |                        |
| $b = 0.57970 - 1.59171I$    |                                       |                        |
| $u = 0.29003 + 1.67173I$    | $-15.0973 + 8.6991I$                  | $-1.14624 - 4.73883I$  |
| $a = 0.47249 - 1.61270I$    |                                       |                        |
| $b = -0.44648 - 1.50505I$   |                                       |                        |
| $u = 0.29003 - 1.67173I$    | $-15.0973 - 8.6991I$                  | $-1.14624 + 4.73883I$  |
| $a = 0.47249 + 1.61270I$    |                                       |                        |
| $b = -0.44648 + 1.50505I$   |                                       |                        |
| $u = 0.45173 + 1.85181I$    | $-8.95857 + 2.10992I$                 | $-13.39192 - 3.92736I$ |
| $a = -0.413403 + 1.215080I$ |                                       |                        |
| $b = 0.250641 + 1.241720I$  |                                       |                        |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.45173 - 1.85181I$    |                                       |                        |
| $a = -0.413403 - 1.215080I$ | $-8.95857 - 2.10992I$                 | $-13.39192 + 3.92736I$ |
| $b = 0.250641 - 1.241720I$  |                                       |                        |

$$\text{III. } I_2^u = \langle -6.48 \times 10^{26}a^9u^3 - 2.25 \times 10^{27}a^8u^3 + \dots + 6.22 \times 10^{28}a + 6.82 \times 10^{28}, 2a^9u^3 - 3a^8u^3 + \dots - 72a + 3, u^4 + u^3 + 3u^2 + 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ 0.0165355a^9u^3 + 0.0573866a^8u^3 + \dots - 1.58600a - 1.74014 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0165355a^9u^3 - 0.0573866a^8u^3 + \dots + 2.58600a + 1.74014 \\ 0.0165355a^9u^3 + 0.0573866a^8u^3 + \dots - 1.58600a - 1.74014 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.000922235a^9u^3 + 0.0578207a^8u^3 + \dots + 0.0532973a + 0.490016 \\ -0.0143278a^9u^3 + 0.00178663a^8u^3 + \dots - 0.336225a - 0.132170 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0530326a^9u^3 + 0.0145794a^8u^3 + \dots - 2.36649a + 0.337689 \\ 0.0257401a^9u^3 + 0.0549904a^8u^3 + \dots - 2.07867a - 0.923136 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ u^3 + u^2 + 2u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.00177082a^9u^3 - 0.000877393a^8u^3 + \dots + 0.0216790a + 0.476649 \\ -0.0288170a^9u^3 - 0.0447707a^8u^3 + \dots + 0.194187a + 0.627577 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.0109816a^9u^3 - 0.0176154a^8u^3 + \dots + 0.0681560a + 1.02747 \\ -0.0127258a^9u^3 - 0.00892781a^8u^3 + \dots + 0.0628627a + 1.84822 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.0109816a^9u^3 - 0.0176154a^8u^3 + \dots + 0.0681560a + 1.02747 \\ -0.0127258a^9u^3 - 0.00892781a^8u^3 + \dots + 0.0628627a + 1.84822 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-0.0146198a^9u^3 - 0.0649565a^8u^3 + \dots - 0.385084a + 9.99651$

**(iv) u-Polynomials at the component**

| Crossings                | u-Polynomials at each crossing           |
|--------------------------|--|
| $c_1, c_2, c_6$<br>$c_8$ | $u^{40} + u^{39} + \cdots + 2894u + 361$ |
| $c_3, c_{11}$            | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)^8$     |
| $c_4, c_7$               | $u^{40} - 5u^{39} + \cdots - 90u + 19$   |
| $c_5, c_9, c_{10}$       | $(u^4 + u^3 + 3u^2 + 2u + 1)^{10}$       |

**(v) Riley Polynomials at the component**

| Crossings                | Riley Polynomials at each crossing              |
|--------------------------|---|
| $c_1, c_2, c_6$<br>$c_8$ | $y^{40} + 35y^{39} + \cdots - 529984y + 130321$ |
| $c_3, c_{11}$            | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^8$           |
| $c_4, c_7$               | $y^{40} + 7y^{39} + \cdots + 9304y + 361$       |
| $c_5, c_9, c_{10}$       | $(y^4 + 5y^3 + 7y^2 + 2y + 1)^{10}$             |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = -0.825694 + 0.761391I$ | $-2.32272 - 1.41510I$                 | $3.30788 + 4.90874I$ |
| $b = 0.486624 - 0.146803I$  |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = -1.176830 - 0.099414I$ | $-4.39470 - 2.94568I$                 | $2.34185 + 9.33939I$ |
| $b = 0.56198 - 1.34282I$    |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = 1.124900 + 0.392414I$  | $-4.39470 + 0.11547I$                 | $2.34185 + 0.47809I$ |
| $b = -0.22676 + 1.56517I$   |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = -0.093009 - 0.749116I$ | $1.14877 + 2.98573I$                  | $6.57105 + 1.41016I$ |
| $b = -0.618982 - 0.887013I$ |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = 0.582300 - 0.394023I$  | $1.14877 - 5.81594I$                  | $6.57105 + 8.40733I$ |
| $b = -1.069750 + 0.079546I$ |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = 0.58749 + 1.48072I$    | $-2.32272 - 1.41510I$                 | $3.30788 + 4.90874I$ |
| $b = -0.058215 + 1.023990I$ |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = 0.77408 - 1.82030I$    | $1.14877 + 2.98573I$                  | $6.57105 + 1.41016I$ |
| $b = 0.277716 - 0.212100I$  |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = -2.19803 + 0.07064I$   | $-4.39470 + 0.11547I$                 | $2.34185 + 0.47809I$ |
| $b = -0.060334 - 1.148470I$ |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = 2.12871 + 0.77761I$    | $-4.39470 - 2.94568I$                 | $2.34185 + 9.33939I$ |
| $b = -0.056830 + 1.372610I$ |                                       |                      |
| $u = -0.395123 + 0.506844I$ |                                       |                      |
| $a = -0.70829 - 2.26113I$   | $1.14877 - 5.81594I$                  | $6.57105 + 8.40733I$ |
| $b = 0.412739 - 1.024450I$  |                                       |                      |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = -0.825694 - 0.761391I$ | $-2.32272 + 1.41510I$                 | $3.30788 - 4.90874I$ |
| $b = 0.486624 + 0.146803I$  |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = -1.176830 + 0.099414I$ | $-4.39470 + 2.94568I$                 | $2.34185 - 9.33939I$ |
| $b = 0.56198 + 1.34282I$    |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = 1.124900 - 0.392414I$  | $-4.39470 - 0.11547I$                 | $2.34185 - 0.47809I$ |
| $b = -0.22676 - 1.56517I$   |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = -0.093009 + 0.749116I$ | $1.14877 - 2.98573I$                  | $6.57105 - 1.41016I$ |
| $b = -0.618982 + 0.887013I$ |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = 0.582300 + 0.394023I$  | $1.14877 + 5.81594I$                  | $6.57105 - 8.40733I$ |
| $b = -1.069750 - 0.079546I$ |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = 0.58749 - 1.48072I$    | $-2.32272 + 1.41510I$                 | $3.30788 - 4.90874I$ |
| $b = -0.058215 - 1.023990I$ |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = 0.77408 + 1.82030I$    | $1.14877 - 2.98573I$                  | $6.57105 - 1.41016I$ |
| $b = 0.277716 + 0.212100I$  |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = -2.19803 - 0.07064I$   | $-4.39470 - 0.11547I$                 | $2.34185 - 0.47809I$ |
| $b = -0.060334 + 1.148470I$ |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = 2.12871 - 0.77761I$    | $-4.39470 + 2.94568I$                 | $2.34185 - 9.33939I$ |
| $b = -0.056830 - 1.372610I$ |                                       |                      |
| $u = -0.395123 - 0.506844I$ |                                       |                      |
| $a = -0.70829 + 2.26113I$   | $1.14877 + 5.81594I$                  | $6.57105 - 8.40733I$ |
| $b = 0.412739 + 1.024450I$  |                                       |                      |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = 0.768262 - 0.287452I$  | $-5.85298 - 7.56480I$                 | $2.91758 + 6.06338I$  |
| $b = 1.62038 - 0.20838I$    |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = -0.098548 + 0.494298I$ | $-5.85298 + 1.23687I$                 | $2.91758 - 0.93379I$  |
| $b = 0.686422 + 0.233614I$  |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = -0.159807 + 0.282979I$ | $-9.32446 - 3.16396I$                 | $-0.34560 + 2.56480I$ |
| $b = -1.077640 + 0.318986I$ |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = 0.20232 + 1.69625I$    | $-5.85298 + 1.23687I$                 | $2.91758 - 0.93379I$  |
| $b = 0.322385 + 1.246000I$  |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = 0.95740 + 1.43668I$    | $-11.39640 - 1.63338I$                | $-1.31162 - 1.86585I$ |
| $b = -0.300846 + 1.175150I$ |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = -0.08180 + 1.73380I$   | $-11.39640 - 4.69454I$                | $-1.31162 + 6.99545I$ |
| $b = -1.02050 + 1.63272I$   |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = -0.22855 - 2.06799I$   | $-11.39640 - 1.63338I$                | $-1.31162 - 1.86585I$ |
| $b = 0.53799 - 1.92599I$    |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = -0.21085 - 2.10586I$   | $-9.32446 - 3.16396I$                 | $-0.34560 + 2.56480I$ |
| $b = 0.04036 - 1.42870I$    |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = -0.83572 - 2.03035I$   | $-11.39640 - 4.69454I$                | $-1.31162 + 6.99545I$ |
| $b = 0.25538 - 1.44672I$    |                                       |                       |
| $u = -0.10488 + 1.55249I$   |                                       |                       |
| $a = -0.00833 + 2.34458I$   | $-5.85298 - 7.56480I$                 | $2.91758 + 6.06338I$  |
| $b = -0.212128 + 1.314620I$ |                                       |                       |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = 0.768262 + 0.287452I$  | $-5.85298 + 7.56480I$                 | $2.91758 - 6.06338I$  |
| $b = 1.62038 + 0.20838I$    |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = -0.098548 - 0.494298I$ | $-5.85298 - 1.23687I$                 | $2.91758 + 0.93379I$  |
| $b = 0.686422 - 0.233614I$  |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = -0.159807 - 0.282979I$ | $-9.32446 + 3.16396I$                 | $-0.34560 - 2.56480I$ |
| $b = -1.077640 - 0.318986I$ |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = 0.20232 - 1.69625I$    | $-5.85298 - 1.23687I$                 | $2.91758 + 0.93379I$  |
| $b = 0.322385 - 1.246000I$  |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = 0.95740 - 1.43668I$    | $-11.39640 + 1.63338I$                | $-1.31162 + 1.86585I$ |
| $b = -0.300846 - 1.175150I$ |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = -0.08180 - 1.73380I$   | $-11.39640 + 4.69454I$                | $-1.31162 - 6.99545I$ |
| $b = -1.02050 - 1.63272I$   |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = -0.22855 + 2.06799I$   | $-11.39640 + 1.63338I$                | $-1.31162 + 1.86585I$ |
| $b = 0.53799 + 1.92599I$    |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = -0.21085 + 2.10586I$   | $-9.32446 + 3.16396I$                 | $-0.34560 - 2.56480I$ |
| $b = 0.04036 + 1.42870I$    |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = -0.83572 + 2.03035I$   | $-11.39640 + 4.69454I$                | $-1.31162 - 6.99545I$ |
| $b = 0.25538 + 1.44672I$    |                                       |                       |
| $u = -0.10488 - 1.55249I$   |                                       |                       |
| $a = -0.00833 - 2.34458I$   | $-5.85298 + 7.56480I$                 | $2.91758 - 6.06338I$  |
| $b = -0.212128 - 1.314620I$ |                                       |                       |

$$\text{III. } I_3^u = \langle -u^6 - 4u^4 + u^3 - 4u^2 + b + u, -u^6 - u^5 - 4u^4 - 3u^3 - 3u^2 + a - 3u + 1, u^{12} + 8u^{10} + \dots + u^2 + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^6 + u^5 + 4u^4 + 3u^3 + 3u^2 + 3u - 1 \\ u^6 + 4u^4 - u^3 + 4u^2 - u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^5 + 4u^3 - u^2 + 4u - 1 \\ u^6 + 4u^4 - u^3 + 4u^2 - u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^{11} + 8u^9 - 2u^8 + 24u^7 - 10u^6 + 33u^5 - 16u^4 + 18u^3 - 8u^2 + u \\ -u^9 - 6u^7 + u^6 - 12u^5 + 2u^4 - 8u^3 + u - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^{11} + 7u^9 - u^8 + 18u^7 - 3u^6 + 20u^5 - u^4 + 8u^3 + 3u^2 + 2 \\ -u^{10} - 6u^8 + 2u^7 - 12u^6 + 7u^5 - 9u^4 + 7u^3 - 2u^2 + 2u - 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^{11} + 7u^9 - 2u^8 + 18u^7 - 9u^6 + 21u^5 - 14u^4 + 10u^3 - 8u^2 + u \\ -u^9 - 6u^7 + u^6 - 12u^5 + 2u^4 - 8u^3 - 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^{10} - 7u^8 + u^7 - 17u^6 + 4u^5 - 16u^4 + 5u^3 - 5u^2 + 3u - 1 \\ -u^{11} - 7u^9 + u^8 - 18u^7 + 4u^6 - 20u^5 + 6u^4 - 8u^3 + 4u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^{10} - 7u^8 + u^7 - 17u^6 + 4u^5 - 16u^4 + 5u^3 - 5u^2 + 3u - 1 \\ -u^{11} - 7u^9 + u^8 - 18u^7 + 4u^6 - 20u^5 + 6u^4 - 8u^3 + 4u^2 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes**

$$= u^{11} + 3u^{10} + 8u^9 + 18u^8 + 20u^7 + 38u^6 + 22u^5 + 35u^4 + 17u^3 + 13u^2 + 8u + 5$$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing  |
|---------------|---|
| $c_1, c_8$    | $u^{12} + 6u^{10} - u^9 + 15u^8 - 4u^7 + 17u^6 - 5u^5 + 9u^4 - 4u^3 + 4u^2 - u + 1$ |
| $c_2, c_6$    | $u^{12} + 6u^{10} + u^9 + 15u^8 + 4u^7 + 17u^6 + 5u^5 + 9u^4 + 4u^3 + 4u^2 + u + 1$ |
| $c_3$         | $u^{12} + 2u^{11} + \dots + 3u + 2$   |
| $c_4, c_7$    | $u^{12} + u^{10} + u^9 + 7u^8 + 5u^6 + 4u^5 + 7u^4 + u^3 + 3u^2 + 3u + 1$           |
| $c_5$         | $u^{12} + 8u^{10} + u^9 + 24u^8 + 4u^7 + 32u^6 + 4u^5 + 16u^4 + u^2 + 1$            |
| $c_9, c_{10}$ | $u^{12} + 8u^{10} - u^9 + 24u^8 - 4u^7 + 32u^6 - 4u^5 + 16u^4 + u^2 + 1$            |
| $c_{11}$      | $u^{12} - 2u^{11} + \dots - 3u + 2$   |

**(v) Riley Polynomials at the component**

| Crossings                | Riley Polynomials at each crossing     |
|--------------------------|--|
| $c_1, c_2, c_6$<br>$c_8$ | $y^{12} + 12y^{11} + \cdots + 7y + 1$  |
| $c_3, c_{11}$            | $y^{12} + 10y^{11} + \cdots + 27y + 4$ |
| $c_4, c_7$               | $y^{12} + 2y^{11} + \cdots - 3y + 1$   |
| $c_5, c_9, c_{10}$       | $y^{12} + 16y^{11} + \cdots + 2y + 1$  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.230605 + 1.156080I$  |                                       |                       |
| $a = -0.567331 - 0.745762I$ | $-4.31667 + 1.17027I$                 | $-1.62350 - 1.30347I$ |
| $b = -0.020024 - 0.653910I$ |                                       |                       |
| $u = 0.230605 - 1.156080I$  |                                       |                       |
| $a = -0.567331 + 0.745762I$ | $-4.31667 - 1.17027I$                 | $-1.62350 + 1.30347I$ |
| $b = -0.020024 + 0.653910I$ |                                       |                       |
| $u = 0.140093 + 1.297660I$  |                                       |                       |
| $a = 0.853374 + 0.043040I$  | $-2.44663 + 5.70307I$                 | $2.68049 - 6.99360I$  |
| $b = 0.508580 + 0.397736I$  |                                       |                       |
| $u = 0.140093 - 1.297660I$  |                                       |                       |
| $a = 0.853374 - 0.043040I$  | $-2.44663 - 5.70307I$                 | $2.68049 + 6.99360I$  |
| $b = 0.508580 - 0.397736I$  |                                       |                       |
| $u = 0.378668 + 0.342829I$  |                                       |                       |
| $a = -0.32614 + 2.14787I$   | $0.94072 - 3.94879I$                  | $4.00078 + 7.18659I$  |
| $b = -0.468199 + 0.625265I$ |                                       |                       |
| $u = 0.378668 - 0.342829I$  |                                       |                       |
| $a = -0.32614 - 2.14787I$   | $0.94072 + 3.94879I$                  | $4.00078 - 7.18659I$  |
| $b = -0.468199 - 0.625265I$ |                                       |                       |
| $u = -0.365297 + 0.317056I$ |                                       |                       |
| $a = -2.00440 + 0.48099I$   | $-4.41748 - 1.96789I$                 | $2.03835 + 0.71750I$  |
| $b = 0.219991 - 1.387990I$  |                                       |                       |
| $u = -0.365297 - 0.317056I$ |                                       |                       |
| $a = -2.00440 - 0.48099I$   | $-4.41748 + 1.96789I$                 | $2.03835 - 0.71750I$  |
| $b = 0.219991 + 1.387990I$  |                                       |                       |
| $u = -0.09322 + 1.52595I$   |                                       |                       |
| $a = 0.48519 + 1.85935I$    | $-10.83690 - 3.47795I$                | $2.93008 + 1.05575I$  |
| $b = -0.55494 + 1.55922I$   |                                       |                       |
| $u = -0.09322 - 1.52595I$   |                                       |                       |
| $a = 0.48519 - 1.85935I$    | $-10.83690 + 3.47795I$                | $2.93008 - 1.05575I$  |
| $b = -0.55494 - 1.55922I$   |                                       |                       |

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.29085 + 1.69584I$   |                                       |                      |
| $a = -0.440697 - 1.320550I$ | $-8.53189 - 1.98164I$                 | $5.47380 - 1.06952I$ |
| $b = 0.314595 - 1.264580I$  |                                       |                      |
| $u = -0.29085 - 1.69584I$   |                                       |                      |
| $a = -0.440697 + 1.320550I$ | $-8.53189 + 1.98164I$                 | $5.47380 + 1.06952I$ |
| $b = 0.314595 + 1.264580I$  |                                       |                      |

#### IV. u-Polynomials

| Crossings     | u-Polynomials at each crossing  |
|---------------|---|
| $c_1, c_8$    | $(u^{12} + 6u^{10} - u^9 + 15u^8 - 4u^7 + 17u^6 - 5u^5 + 9u^4 - 4u^3 + 4u^2 - u + 1) \cdot (u^{21} + 10u^{19} + \dots + 2u - 1)(u^{40} + u^{39} + \dots + 2894u + 361)$ |
| $c_2, c_6$    | $(u^{12} + 6u^{10} + u^9 + 15u^8 + 4u^7 + 17u^6 + 5u^5 + 9u^4 + 4u^3 + 4u^2 + u + 1) \cdot (u^{21} + 10u^{19} + \dots + 2u - 1)(u^{40} + u^{39} + \dots + 2894u + 361)$ |
| $c_3$         | $((u^5 + u^4 + 2u^3 + u^2 + u + 1)^8)(u^{12} + 2u^{11} + \dots + 3u + 2) \cdot (u^{21} - 13u^{20} + \dots + 208u - 16)$   |
| $c_4, c_7$    | $(u^{12} + u^{10} + u^9 + 7u^8 + 5u^6 + 4u^5 + 7u^4 + u^3 + 3u^2 + 3u + 1) \cdot (u^{21} + u^{19} + \dots - 2u^2 - 1)(u^{40} - 5u^{39} + \dots - 90u + 19)$             |
| $c_5$         | $(u^4 + u^3 + 3u^2 + 2u + 1)^{10} \cdot (u^{12} + 8u^{10} + u^9 + 24u^8 + 4u^7 + 32u^6 + 4u^5 + 16u^4 + u^2 + 1) \cdot (u^{21} - 11u^{20} + \dots + 368u - 32)$         |
| $c_9, c_{10}$ | $(u^4 + u^3 + 3u^2 + 2u + 1)^{10} \cdot (u^{12} + 8u^{10} - u^9 + 24u^8 - 4u^7 + 32u^6 - 4u^5 + 16u^4 + u^2 + 1) \cdot (u^{21} - 11u^{20} + \dots + 368u - 32)$         |
| $c_{11}$      | $((u^5 + u^4 + 2u^3 + u^2 + u + 1)^8)(u^{12} - 2u^{11} + \dots - 3u + 2) \cdot (u^{21} - 13u^{20} + \dots + 208u - 16)$   |

## V. Riley Polynomials

| Crossings                | Riley Polynomials at each crossing   |
|--------------------------|--|
| $c_1, c_2, c_6$<br>$c_8$ | $(y^{12} + 12y^{11} + \dots + 7y + 1)(y^{21} + 20y^{20} + \dots + 10y - 1)$ $\cdot (y^{40} + 35y^{39} + \dots - 529984y + 130321)$ |
| $c_3, c_{11}$            | $((y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^8)(y^{12} + 10y^{11} + \dots + 27y + 4)$ $\cdot (y^{21} + 13y^{20} + \dots + 3968y - 256)$     |
| $c_4, c_7$               | $(y^{12} + 2y^{11} + \dots - 3y + 1)(y^{21} + 2y^{20} + \dots - 4y - 1)$ $\cdot (y^{40} + 7y^{39} + \dots + 9304y + 361)$          |
| $c_5, c_9, c_{10}$       | $((y^4 + 5y^3 + 7y^2 + 2y + 1)^{10})(y^{12} + 16y^{11} + \dots + 2y + 1)$ $\cdot (y^{21} + 21y^{20} + \dots + 4864y - 1024)$       |