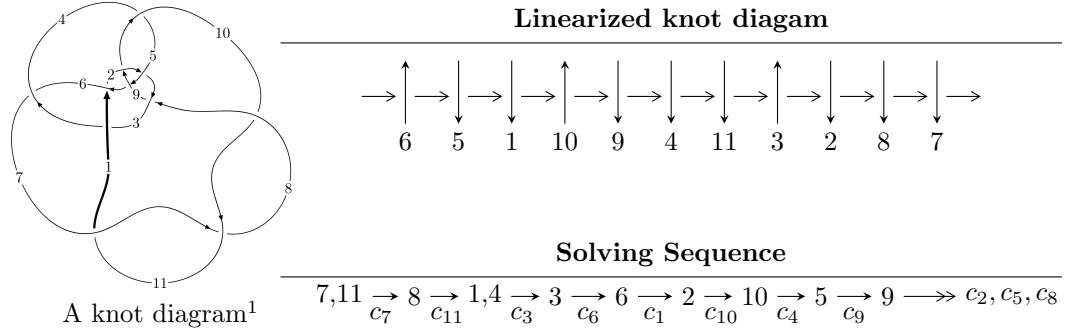


## $11a_{349}$ ( $K11a_{349}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -8794u^{30} - 59427u^{29} + \dots + 14648b - 565817, \\
 &\quad 1207779u^{30} + 10072486u^{29} + \dots + 1069304a - 32922272, u^{31} + 9u^{30} + \dots - 608u - 73 \rangle \\
 I_2^u &= \langle 1245599508u^{14}a^3 + 2019297822u^{14}a^2 + \dots + 2559076525a + 1076862186, \\
 &\quad u^{14}a^2 - 3u^{14} + \dots - a + 8, \\
 &\quad u^{15} - 3u^{14} + 12u^{13} - 25u^{12} + 52u^{11} - 78u^{10} + 104u^9 - 109u^8 + 94u^7 - 58u^6 + 24u^5 + 2u^4 - 8u^3 + 4u^2 - 1 \rangle \\
 I_3^u &= \langle -u^{15} + 5u^{14} + \dots + 2b + 3u, u^{15} - 6u^{14} + \dots + 2a + 3, u^{16} - 4u^{15} + \dots + 2u^2 + 1 \rangle
 \end{aligned}$$

$$I_1^v = \langle a, b^2 - b + 1, v - 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 109 representations.

---

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -8794u^{30} - 59427u^{29} + \dots + 14648b - 565817, 1.21 \times 10^6 u^{30} + 1.01 \times 10^7 u^{29} + \dots + 1.07 \times 10^6 a - 3.29 \times 10^7, u^{31} + 9u^{30} + \dots - 608u - 73 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -1.12950u^{30} - 9.41967u^{29} + \dots + 251.970u + 30.7885 \\ 0.600355u^{30} + 4.05700u^{29} + \dots + 252.304u + 38.6276 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.216690u^{30} + 2.67536u^{29} + \dots - 151.674u - 13.0374 \\ -0.745836u^{30} - 8.03803u^{29} + \dots + 655.948u + 82.4535 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.742167u^{30} + 6.23678u^{29} + \dots - 18.8469u + 1.55985 \\ -0.689719u^{30} - 5.07503u^{29} + \dots - 28.6196u - 3.82871 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -1.15640u^{30} - 8.25807u^{29} + \dots - 113.632u - 15.8600 \\ -0.265838u^{30} - 5.40866u^{29} + \dots + 1150.58u + 154.173 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.757026u^{30} - 7.25316u^{29} + \dots + 294.147u + 32.3085 \\ 1.10930u^{30} + 9.99788u^{29} + \dots - 399.270u - 46.4128 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.261828u^{30} + 1.90356u^{29} + \dots - 25.4736u - 4.38300 \\ 0.0106499u^{30} + 0.585131u^{29} + \dots - 179.751u - 22.5472 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.261828u^{30} + 1.90356u^{29} + \dots - 25.4736u - 4.38300 \\ 0.0106499u^{30} + 0.585131u^{29} + \dots - 179.751u - 22.5472 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{102043}{14648}u^{30} + \frac{113248}{1831}u^{29} + \dots - \frac{59622049}{14648}u - \frac{4091199}{7324}$$

**(iv) u-Polynomials at the component**

| Crossings             | u-Polynomials at each crossing                 |
|-----------------------|--|
| $c_1$                 | $u^{31} - 24u^{30} + \cdots - 360448u + 32768$ |
| $c_2$                 | $u^{31} - 22u^{30} + \cdots + 419u - 73$       |
| $c_3, c_6$            | $u^{31} + u^{30} + \cdots + 14u + 1$           |
| $c_4, c_8$            | $u^{31} - u^{30} + \cdots - 2u + 1$            |
| $c_5, c_9$            | $u^{31} + u^{29} + \cdots + 2u + 1$            |
| $c_7, c_{10}, c_{11}$ | $u^{31} - 9u^{30} + \cdots - 608u + 73$        |

**(v) Riley Polynomials at the component**

| Crossings             | Riley Polynomials at each crossing                      |
|-----------------------|---|
| $c_1$                 | $y^{31} + 10y^{30} + \cdots - 2147483648y - 1073741824$ |
| $c_2$                 | $y^{31} + 46y^{29} + \cdots + 42263y - 5329$            |
| $c_3, c_6$            | $y^{31} + 15y^{30} + \cdots + 110y - 1$                 |
| $c_4, c_8$            | $y^{31} + 7y^{30} + \cdots - 40y - 1$                   |
| $c_5, c_9$            | $y^{31} + 2y^{30} + \cdots - 6y - 1$                    |
| $c_7, c_{10}, c_{11}$ | $y^{31} + 31y^{30} + \cdots - 37092y - 5329$            |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.852991 + 0.499323I$ |                                       |                       |
| $a = -0.379018 - 0.633422I$ | $-3.36735 + 13.70180I$                | $-6.58812 - 9.58074I$ |
| $b = -0.994010 + 0.988244I$ |                                       |                       |
| $u = -0.852991 - 0.499323I$ |                                       |                       |
| $a = -0.379018 + 0.633422I$ | $-3.36735 - 13.70180I$                | $-6.58812 + 9.58074I$ |
| $b = -0.994010 - 0.988244I$ |                                       |                       |
| $u = -0.316579 + 0.888214I$ |                                       |                       |
| $a = -1.097970 + 0.312101I$ | $-0.90699 - 1.43155I$                 | $-3.87159 + 9.73821I$ |
| $b = 0.721245 + 0.634191I$  |                                       |                       |
| $u = -0.316579 - 0.888214I$ |                                       |                       |
| $a = -1.097970 - 0.312101I$ | $-0.90699 + 1.43155I$                 | $-3.87159 - 9.73821I$ |
| $b = 0.721245 - 0.634191I$  |                                       |                       |
| $u = -0.886962 + 0.303700I$ |                                       |                       |
| $a = 0.332501 + 0.072745I$  | $1.08264 + 5.12278I$                  | $-0.41195 - 8.68112I$ |
| $b = 0.235798 - 0.956055I$  |                                       |                       |
| $u = -0.886962 - 0.303700I$ |                                       |                       |
| $a = 0.332501 - 0.072745I$  | $1.08264 - 5.12278I$                  | $-0.41195 + 8.68112I$ |
| $b = 0.235798 + 0.956055I$  |                                       |                       |
| $u = -0.844232 + 0.691840I$ |                                       |                       |
| $a = 0.578588 - 0.200674I$  | $-2.87005 - 8.08181I$                 | $-6.17763 + 7.71756I$ |
| $b = -0.675443 - 0.657436I$ |                                       |                       |
| $u = -0.844232 - 0.691840I$ |                                       |                       |
| $a = 0.578588 + 0.200674I$  | $-2.87005 + 8.08181I$                 | $-6.17763 - 7.71756I$ |
| $b = -0.675443 + 0.657436I$ |                                       |                       |
| $u = 1.18811$               |                                       |                       |
| $a = -0.163592$             | $-2.36361$                            | 35.4320               |
| $b = 0.0888281$             |                                       |                       |
| $u = -0.722698 + 0.301514I$ |                                       |                       |
| $a = 0.681450 + 0.287166I$  | $-2.64536 + 5.39096I$                 | $-12.5250 - 11.7577I$ |
| $b = 0.960625 - 1.037040I$  |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.722698 - 0.301514I$ |                                       |                       |
| $a = 0.681450 - 0.287166I$  | $-2.64536 - 5.39096I$                 | $-12.5250 + 11.7577I$ |
| $b = 0.960625 + 1.037040I$  |                                       |                       |
| $u = -0.403264 + 0.649558I$ |                                       |                       |
| $a = -0.871610 - 0.575987I$ | $2.96693 - 0.69018I$                  | $2.10294 + 0.24214I$  |
| $b = -0.277793 + 0.861904I$ |                                       |                       |
| $u = -0.403264 - 0.649558I$ |                                       |                       |
| $a = -0.871610 + 0.575987I$ | $2.96693 + 0.69018I$                  | $2.10294 - 0.24214I$  |
| $b = -0.277793 - 0.861904I$ |                                       |                       |
| $u = -0.281651 + 1.296450I$ |                                       |                       |
| $a = -0.574322 - 0.910235I$ | $3.76674 - 0.82301I$                  | 0                     |
| $b = -0.150654 + 0.951529I$ |                                       |                       |
| $u = -0.281651 - 1.296450I$ |                                       |                       |
| $a = -0.574322 + 0.910235I$ | $3.76674 + 0.82301I$                  | 0                     |
| $b = -0.150654 - 0.951529I$ |                                       |                       |
| $u = 0.013670 + 1.401210I$  |                                       |                       |
| $a = -0.09185 + 1.89114I$   | $4.82828 + 1.90483I$                  | 0                     |
| $b = 0.94670 - 1.20717I$    |                                       |                       |
| $u = 0.013670 - 1.401210I$  |                                       |                       |
| $a = -0.09185 - 1.89114I$   | $4.82828 - 1.90483I$                  | 0                     |
| $b = 0.94670 + 1.20717I$    |                                       |                       |
| $u = 0.297730 + 0.511306I$  |                                       |                       |
| $a = -0.978614 - 0.248724I$ | $-0.38522 - 1.41061I$                 | $-2.90382 + 5.08297I$ |
| $b = 0.260483 + 0.340007I$  |                                       |                       |
| $u = 0.297730 - 0.511306I$  |                                       |                       |
| $a = -0.978614 + 0.248724I$ | $-0.38522 + 1.41061I$                 | $-2.90382 - 5.08297I$ |
| $b = 0.260483 - 0.340007I$  |                                       |                       |
| $u = 0.06166 + 1.42151I$    |                                       |                       |
| $a = -0.130706 - 1.235920I$ | $5.49366 - 2.37184I$                  | 0                     |
| $b = -0.471500 + 0.878105I$ |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.06166 - 1.42151I$    |                                       |            |
| $a = -0.130706 + 1.235920I$ | $5.49366 + 2.37184I$                  | 0          |
| $b = -0.471500 - 0.878105I$ |                                       |            |
| $u = -0.26782 + 1.43933I$   |                                       |            |
| $a = -0.00779 + 1.93679I$   | $2.96780 + 8.97601I$                  | 0          |
| $b = 1.07459 - 1.38869I$    |                                       |            |
| $u = -0.26782 - 1.43933I$   |                                       |            |
| $a = -0.00779 - 1.93679I$   | $2.96780 - 8.97601I$                  | 0          |
| $b = 1.07459 + 1.38869I$    |                                       |            |
| $u = -0.14638 + 1.50740I$   |                                       |            |
| $a = -0.13509 - 1.58317I$   | $9.90733 + 1.39993I$                  | 0          |
| $b = -0.698585 + 1.200690I$ |                                       |            |
| $u = -0.14638 - 1.50740I$   |                                       |            |
| $a = -0.13509 + 1.58317I$   | $9.90733 - 1.39993I$                  | 0          |
| $b = -0.698585 - 1.200690I$ |                                       |            |
| $u = -0.33955 + 1.47960I$   |                                       |            |
| $a = 0.39739 + 1.41421I$    | $6.87874 + 9.56615I$                  | 0          |
| $b = 0.499587 - 1.282410I$  |                                       |            |
| $u = -0.33955 - 1.47960I$   |                                       |            |
| $a = 0.39739 - 1.41421I$    | $6.87874 - 9.56615I$                  | 0          |
| $b = 0.499587 + 1.282410I$  |                                       |            |
| $u = -0.30764 + 1.52681I$   |                                       |            |
| $a = 0.13457 - 1.85476I$    | $3.1915 + 17.9314I$                   | 0          |
| $b = -1.10902 + 1.32474I$   |                                       |            |
| $u = -0.30764 - 1.52681I$   |                                       |            |
| $a = 0.13457 + 1.85476I$    | $3.1915 - 17.9314I$                   | 0          |
| $b = -1.10902 - 1.32474I$   |                                       |            |
| $u = -0.09735 + 1.67029I$   |                                       |            |
| $a = 0.203729 + 0.617797I$  | $5.63925 - 4.20521I$                  | 0          |
| $b = 0.133556 - 0.557496I$  |                                       |            |

| Solutions to $I_1^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------------|---------------------------------------|------------|
| $u = -0.09735 - 1.67029I$  |                                       |            |
| $a = 0.203729 - 0.617797I$ | $5.63925 + 4.20521I$                  | 0          |
| $b = 0.133556 + 0.557496I$ |                                       |            |

$$\text{II. } I_2^u = \langle 1.25 \times 10^9 a^3 u^{14} + 2.02 \times 10^9 a^2 u^{14} + \dots + 2.56 \times 10^9 a + 1.08 \times 10^9, u^{14} a^2 - 3u^{14} + \dots - a + 8, u^{15} - 3u^{14} + \dots + 4u^2 - 1 \rangle$$

(i) **Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -0.817912a^3 u^{14} - 1.32595a^2 u^{14} + \dots - 1.68039a - 0.707112 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.471824a^3 u^{14} + 0.346733a^2 u^{14} + \dots + 0.195001a - 0.931134 \\ -0.346088a^3 u^{14} - 1.67269a^2 u^{14} + \dots - 0.875395a + 0.224022 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0699739a^3 u^{14} - 0.319988a^2 u^{14} + \dots + 0.0210967a + 0.491055 \\ -0.0602705a^3 u^{14} - 0.0972240a^2 u^{14} + \dots - 0.701805a + 0.161294 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.548073a^3 u^{14} - 0.225684a^2 u^{14} + \dots - 0.0705041a + 0.0289120 \\ 0.417828a^3 u^{14} - 0.191528a^2 u^{14} + \dots - 0.610204a + 0.623437 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.471824a^3 u^{14} + 0.346733a^2 u^{14} + \dots + 0.195001a - 0.931134 \\ -1.19479a^3 u^{14} - 1.41931a^2 u^{14} + \dots - 1.33430a - 0.154021 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.923492a^3 u^{14} + 0.378846a^2 u^{14} + \dots - 0.912625a - 0.744597 \\ 0.765493a^3 u^{14} - 1.51930a^2 u^{14} + \dots - 0.488395a + 1.38890 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.923492a^3 u^{14} + 0.378846a^2 u^{14} + \dots - 0.912625a - 0.744597 \\ 0.765493a^3 u^{14} - 1.51930a^2 u^{14} + \dots - 0.488395a + 1.38890 \end{pmatrix}$$

(ii) **Obstruction class** = -1

$$(iii) \text{ Cusp Shapes} = \frac{271921296}{138445675} u^{14} a^3 + \frac{88680364}{138445675} u^{14} a^2 + \dots + \frac{17490488}{5537827} a - \frac{1797460618}{138445675}$$

**(iv) u-Polynomials at the component**

| Crossings             | u-Polynomials at each crossing            |
|-----------------------|---|
| $c_1$                 | $(u^2 + u + 1)^{30}$                      |
| $c_2$                 | $(u^{15} + 7u^{14} + \dots - 4u^2 + 1)^4$ |
| $c_3, c_6$            | $u^{60} + u^{59} + \dots + 12u + 7$       |
| $c_4, c_8$            | $u^{60} - u^{59} + \dots - 19478u + 3673$ |
| $c_5, c_9$            | $u^{60} - u^{59} + \dots + 6u + 1$        |
| $c_7, c_{10}, c_{11}$ | $(u^{15} + 3u^{14} + \dots - 4u^2 + 1)^4$ |

**(v) Riley Polynomials at the component**

| Crossings             | Riley Polynomials at each crossing                   |
|-----------------------|--|
| $c_1$                 | $(y^2 + y + 1)^{30}$                                 |
| $c_2$                 | $(y^{15} - y^{14} + \cdots + 8y - 1)^4$              |
| $c_3, c_6$            | $y^{60} - 9y^{59} + \cdots - 256y + 49$              |
| $c_4, c_8$            | $y^{60} + 15y^{59} + \cdots + 261046488y + 13490929$ |
| $c_5, c_9$            | $y^{60} - 21y^{59} + \cdots - 228y^2 + 1$            |
| $c_7, c_{10}, c_{11}$ | $(y^{15} + 15y^{14} + \cdots + 8y - 1)^4$            |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.825834 + 0.538674I$  |                                       |                       |
| $a = 0.179032 - 0.898220I$  | $-2.77564 - 4.75250I$                 | $-17.6934 + 11.6845I$ |
| $b = 0.942665 + 0.900730I$  |                                       |                       |
| $u = 0.825834 + 0.538674I$  |                                       |                       |
| $a = 0.064202 + 0.531611I$  | $-2.77564 - 0.69273I$                 | $-17.6934 + 4.7563I$  |
| $b = -0.515882 + 0.190551I$ |                                       |                       |
| $u = 0.825834 + 0.538674I$  |                                       |                       |
| $a = -0.374874 + 0.363480I$ | $-2.77564 - 4.75250I$                 | $-17.6934 + 11.6845I$ |
| $b = -0.924983 - 0.606302I$ |                                       |                       |
| $u = 0.825834 + 0.538674I$  |                                       |                       |
| $a = -0.429379 - 0.094637I$ | $-2.77564 - 0.69273I$                 | $-17.6934 + 4.7563I$  |
| $b = 0.762023 - 0.353078I$  |                                       |                       |
| $u = 0.825834 - 0.538674I$  |                                       |                       |
| $a = 0.179032 + 0.898220I$  | $-2.77564 + 4.75250I$                 | $-17.6934 - 11.6845I$ |
| $b = 0.942665 - 0.900730I$  |                                       |                       |
| $u = 0.825834 - 0.538674I$  |                                       |                       |
| $a = 0.064202 - 0.531611I$  | $-2.77564 + 0.69273I$                 | $-17.6934 - 4.7563I$  |
| $b = -0.515882 - 0.190551I$ |                                       |                       |
| $u = 0.825834 - 0.538674I$  |                                       |                       |
| $a = -0.374874 - 0.363480I$ | $-2.77564 + 4.75250I$                 | $-17.6934 - 11.6845I$ |
| $b = -0.924983 + 0.606302I$ |                                       |                       |
| $u = 0.825834 - 0.538674I$  |                                       |                       |
| $a = -0.429379 + 0.094637I$ | $-2.77564 + 0.69273I$                 | $-17.6934 - 4.7563I$  |
| $b = 0.762023 + 0.353078I$  |                                       |                       |
| $u = -0.000696 + 1.255430I$ |                                       |                       |
| $a = -0.537288 + 0.318620I$ | $0.17890 - 4.56727I$                  | $-8.44510 + 5.18626I$ |
| $b = -1.054520 - 0.277320I$ |                                       |                       |
| $u = -0.000696 + 1.255430I$ |                                       |                       |
| $a = -1.53790 - 0.07369I$   | $0.178899 - 0.507500I$                | $-8.44510 - 1.74195I$ |
| $b = 1.74600 + 0.26986I$    |                                       |                       |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.000696 + 1.255430I$ |                                       |                        |
| $a = -0.46059 + 1.65199I$   | $0.178899 - 0.507500I$                | $-8.44510 - 1.74195I$  |
| $b = 0.246412 - 0.261109I$  |                                       |                        |
| $u = -0.000696 + 1.255430I$ |                                       |                        |
| $a = 0.16969 - 2.83852I$    | $0.17890 - 4.56727I$                  | $-8.44510 + 5.18626I$  |
| $b = 0.05074 + 1.99842I$    |                                       |                        |
| $u = -0.000696 - 1.255430I$ |                                       |                        |
| $a = -0.537288 - 0.318620I$ | $0.17890 + 4.56727I$                  | $-8.44510 - 5.18626I$  |
| $b = -1.054520 + 0.277320I$ |                                       |                        |
| $u = -0.000696 - 1.255430I$ |                                       |                        |
| $a = -1.53790 + 0.07369I$   | $0.178899 + 0.507500I$                | $-8.44510 + 1.74195I$  |
| $b = 1.74600 - 0.26986I$    |                                       |                        |
| $u = -0.000696 - 1.255430I$ |                                       |                        |
| $a = -0.46059 - 1.65199I$   | $0.178899 + 0.507500I$                | $-8.44510 + 1.74195I$  |
| $b = 0.246412 + 0.261109I$  |                                       |                        |
| $u = -0.000696 - 1.255430I$ |                                       |                        |
| $a = 0.16969 + 2.83852I$    | $0.17890 + 4.56727I$                  | $-8.44510 - 5.18626I$  |
| $b = 0.05074 - 1.99842I$    |                                       |                        |
| $u = 0.374558 + 0.641779I$  |                                       |                        |
| $a = -1.242750 - 0.072310I$ | $-0.331160 - 1.366830I$               | $-2.47200 + 4.73263I$  |
| $b = 0.404571 - 0.052904I$  |                                       |                        |
| $u = 0.374558 + 0.641779I$  |                                       |                        |
| $a = -0.211923 + 0.547582I$ | $-0.33116 - 5.42660I$                 | $-2.47200 + 11.66083I$ |
| $b = -1.227140 - 0.690327I$ |                                       |                        |
| $u = 0.374558 + 0.641779I$  |                                       |                        |
| $a = -0.446534 - 0.078718I$ | $-0.331160 - 1.366830I$               | $-2.47200 + 4.73263I$  |
| $b = 0.233588 + 0.584828I$  |                                       |                        |
| $u = 0.374558 + 0.641779I$  |                                       |                        |
| $a = 1.18736 - 1.93503I$    | $-0.33116 - 5.42660I$                 | $-2.47200 + 11.66083I$ |
| $b = 0.447402 + 0.977027I$  |                                       |                        |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.374558 - 0.641779I$  |                                       |                        |
| $a = -1.242750 + 0.072310I$ | $-0.331160 + 1.366830I$               | $-2.47200 - 4.73263I$  |
| $b = 0.404571 + 0.052904I$  |                                       |                        |
| $u = 0.374558 - 0.641779I$  |                                       |                        |
| $a = -0.211923 - 0.547582I$ | $-0.33116 + 5.42660I$                 | $-2.47200 - 11.66083I$ |
| $b = -1.227140 + 0.690327I$ |                                       |                        |
| $u = 0.374558 - 0.641779I$  |                                       |                        |
| $a = -0.446534 + 0.078718I$ | $-0.331160 + 1.366830I$               | $-2.47200 - 4.73263I$  |
| $b = 0.233588 - 0.584828I$  |                                       |                        |
| $u = 0.374558 - 0.641779I$  |                                       |                        |
| $a = 1.18736 + 1.93503I$    | $-0.33116 + 5.42660I$                 | $-2.47200 - 11.66083I$ |
| $b = 0.447402 - 0.977027I$  |                                       |                        |
| $u = 0.678314$              |                                       |                        |
| $a = -0.755171 + 1.008870I$ | $-2.66135 + 2.02988I$                 | $-15.2719 - 3.4641I$   |
| $b = -0.575180 + 0.365490I$ |                                       |                        |
| $u = 0.678314$              |                                       |                        |
| $a = -0.755171 - 1.008870I$ | $-2.66135 - 2.02988I$                 | $-15.2719 + 3.4641I$   |
| $b = -0.575180 - 0.365490I$ |                                       |                        |
| $u = 0.678314$              |                                       |                        |
| $a = -0.054442 + 0.393425I$ | $-2.66135 + 2.02988I$                 | $-15.2719 - 3.4641I$   |
| $b = 0.902396 - 0.932245I$  |                                       |                        |
| $u = 0.678314$              |                                       |                        |
| $a = -0.054442 - 0.393425I$ | $-2.66135 - 2.02988I$                 | $-15.2719 + 3.4641I$   |
| $b = 0.902396 + 0.932245I$  |                                       |                        |
| $u = -0.100337 + 1.375660I$ |                                       |                        |
| $a = -0.339092 + 0.510735I$ | $1.67680 + 3.56562I$                  | $-5.33049 - 4.32935I$  |
| $b = 1.44399 - 0.16542I$    |                                       |                        |
| $u = -0.100337 + 1.375660I$ |                                       |                        |
| $a = 0.86553 - 2.02688I$    | $1.67680 + 7.62538I$                  | $-5.33049 - 11.25756I$ |
| $b = -0.113467 + 0.277530I$ |                                       |                        |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.100337 + 1.375660I$ |                                       |                        |
| $a = 2.12438 + 1.14269I$    | $1.67680 + 7.62538I$                  | $-5.33049 - 11.25756I$ |
| $b = -2.33104 - 1.21010I$   |                                       |                        |
| $u = -0.100337 + 1.375660I$ |                                       |                        |
| $a = -0.39013 + 2.52070I$   | $1.67680 + 3.56562I$                  | $-5.33049 - 4.32935I$  |
| $b = 0.58590 - 1.48531I$    |                                       |                        |
| $u = -0.100337 - 1.375660I$ |                                       |                        |
| $a = -0.339092 - 0.510735I$ | $1.67680 - 3.56562I$                  | $-5.33049 + 4.32935I$  |
| $b = 1.44399 + 0.16542I$    |                                       |                        |
| $u = -0.100337 - 1.375660I$ |                                       |                        |
| $a = 0.86553 + 2.02688I$    | $1.67680 - 7.62538I$                  | $-5.33049 + 11.25756I$ |
| $b = -0.113467 - 0.277530I$ |                                       |                        |
| $u = -0.100337 - 1.375660I$ |                                       |                        |
| $a = 2.12438 - 1.14269I$    | $1.67680 - 7.62538I$                  | $-5.33049 + 11.25756I$ |
| $b = -2.33104 + 1.21010I$   |                                       |                        |
| $u = -0.100337 - 1.375660I$ |                                       |                        |
| $a = -0.39013 - 2.52070I$   | $1.67680 - 3.56562I$                  | $-5.33049 + 4.32935I$  |
| $b = 0.58590 + 1.48531I$    |                                       |                        |
| $u = 0.15235 + 1.51729I$    |                                       |                        |
| $a = -0.521531 + 0.526784I$ | $6.67569 - 3.44689I$                  | $2.29813 + 1.92370I$   |
| $b = -0.380642 - 0.366400I$ |                                       |                        |
| $u = 0.15235 + 1.51729I$    |                                       |                        |
| $a = -0.11679 - 1.56879I$   | $6.67569 - 3.44689I$                  | $2.29813 + 1.92370I$   |
| $b = 0.380795 + 1.344430I$  |                                       |                        |
| $u = 0.15235 + 1.51729I$    |                                       |                        |
| $a = 0.36895 - 1.83783I$    | $6.67569 - 7.50666I$                  | $2.29813 + 8.85191I$   |
| $b = 0.665586 + 0.944764I$  |                                       |                        |
| $u = 0.15235 + 1.51729I$    |                                       |                        |
| $a = 0.85260 + 1.80604I$    | $6.67569 - 7.50666I$                  | $2.29813 + 8.85191I$   |
| $b = -1.51266 - 1.43364I$   |                                       |                        |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.15235 - 1.51729I$    |                                       |                       |
| $a = -0.521531 - 0.526784I$ | $6.67569 + 3.44689I$                  | $2.29813 - 1.92370I$  |
| $b = -0.380642 + 0.366400I$ |                                       |                       |
| $u = 0.15235 - 1.51729I$    |                                       |                       |
| $a = -0.11679 + 1.56879I$   | $6.67569 + 3.44689I$                  | $2.29813 - 1.92370I$  |
| $b = 0.380795 - 1.344430I$  |                                       |                       |
| $u = 0.15235 - 1.51729I$    |                                       |                       |
| $a = 0.36895 + 1.83783I$    | $6.67569 + 7.50666I$                  | $2.29813 - 8.85191I$  |
| $b = 0.665586 - 0.944764I$  |                                       |                       |
| $u = 0.15235 - 1.51729I$    |                                       |                       |
| $a = 0.85260 - 1.80604I$    | $6.67569 + 7.50666I$                  | $2.29813 - 8.85191I$  |
| $b = -1.51266 + 1.43364I$   |                                       |                       |
| $u = 0.29798 + 1.53037I$    |                                       |                       |
| $a = -0.206885 + 1.025480I$ | $3.91480 - 4.81769I$                  | $-7.00546 + 6.81035I$ |
| $b = -0.293963 - 0.641758I$ |                                       |                       |
| $u = 0.29798 + 1.53037I$    |                                       |                       |
| $a = -0.296418 - 0.758545I$ | $3.91480 - 4.81769I$                  | $-7.00546 + 6.81035I$ |
| $b = 0.736482 + 0.652145I$  |                                       |                       |
| $u = 0.29798 + 1.53037I$    |                                       |                       |
| $a = 0.201484 + 1.364530I$  | $3.91480 - 8.87745I$                  | $-7.0055 + 13.7386I$  |
| $b = -1.14931 - 0.94853I$   |                                       |                       |
| $u = 0.29798 + 1.53037I$    |                                       |                       |
| $a = -0.18100 - 1.93387I$   | $3.91480 - 8.87745I$                  | $-7.0055 + 13.7386I$  |
| $b = 0.91906 + 1.32657I$    |                                       |                       |
| $u = 0.29798 - 1.53037I$    |                                       |                       |
| $a = -0.206885 - 1.025480I$ | $3.91480 + 4.81769I$                  | $-7.00546 - 6.81035I$ |
| $b = -0.293963 + 0.641758I$ |                                       |                       |
| $u = 0.29798 - 1.53037I$    |                                       |                       |
| $a = -0.296418 + 0.758545I$ | $3.91480 + 4.81769I$                  | $-7.00546 - 6.81035I$ |
| $b = 0.736482 - 0.652145I$  |                                       |                       |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.29798 - 1.53037I$    |                                       |                       |
| $a = 0.201484 - 1.364530I$  | $3.91480 + 8.87745I$                  | $-7.0055 - 13.7386I$  |
| $b = -1.14931 + 0.94853I$   |                                       |                       |
| $u = 0.29798 - 1.53037I$    |                                       |                       |
| $a = -0.18100 + 1.93387I$   | $3.91480 + 8.87745I$                  | $-7.0055 - 13.7386I$  |
| $b = 0.91906 - 1.32657I$    |                                       |                       |
| $u = -0.388845 + 0.104061I$ |                                       |                       |
| $a = -0.406304 + 1.016400I$ | $-3.07391 + 5.95948I$                 | $-15.7157 - 11.4516I$ |
| $b = -1.21864 - 1.27940I$   |                                       |                       |
| $u = -0.388845 + 0.104061I$ |                                       |                       |
| $a = 1.27388 + 1.26165I$    | $-3.07391 + 1.89972I$                 | $-15.7157 - 4.5234I$  |
| $b = 1.049420 - 0.913569I$  |                                       |                       |
| $u = -0.388845 + 0.104061I$ |                                       |                       |
| $a = 2.16554 - 1.41204I$    | $-3.07391 + 1.89972I$                 | $-15.7157 - 4.5234I$  |
| $b = 0.939626 - 0.106413I$  |                                       |                       |
| $u = -0.388845 + 0.104061I$ |                                       |                       |
| $a = -1.44365 - 3.91984I$   | $-3.07391 + 5.95948I$                 | $-15.7157 - 11.4516I$ |
| $b = -0.659218 + 0.066827I$ |                                       |                       |
| $u = -0.388845 - 0.104061I$ |                                       |                       |
| $a = -0.406304 - 1.016400I$ | $-3.07391 - 5.95948I$                 | $-15.7157 + 11.4516I$ |
| $b = -1.21864 + 1.27940I$   |                                       |                       |
| $u = -0.388845 - 0.104061I$ |                                       |                       |
| $a = 1.27388 - 1.26165I$    | $-3.07391 - 1.89972I$                 | $-15.7157 + 4.5234I$  |
| $b = 1.049420 + 0.913569I$  |                                       |                       |
| $u = -0.388845 - 0.104061I$ |                                       |                       |
| $a = 2.16554 + 1.41204I$    | $-3.07391 - 1.89972I$                 | $-15.7157 + 4.5234I$  |
| $b = 0.939626 + 0.106413I$  |                                       |                       |
| $u = -0.388845 - 0.104061I$ |                                       |                       |
| $a = -1.44365 + 3.91984I$   | $-3.07391 - 5.95948I$                 | $-15.7157 + 11.4516I$ |
| $b = -0.659218 - 0.066827I$ |                                       |                       |

$$\text{III. } I_3^u = \langle -u^{15} + 5u^{14} + \dots + 2b + 3u, u^{15} - 6u^{14} + \dots + 2a + 3, u^{16} - 4u^{15} + \dots + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{2}u^{15} + 3u^{14} + \dots + 2u - \frac{3}{2} \\ \frac{1}{2}u^{15} - \frac{5}{2}u^{14} + \dots + \frac{1}{2}u^2 - \frac{3}{2}u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{15} + 4u^{14} + \dots + 2u - 2 \\ u^{15} - \frac{7}{2}u^{14} + \dots - \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^{15} - \frac{3}{2}u^{14} + \dots - \frac{9}{2}u + 3 \\ -\frac{1}{2}u^{14} + \frac{3}{2}u^{13} + \dots + \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{15} - \frac{11}{2}u^{14} + \dots + \frac{15}{2}u - \frac{5}{2} \\ -u^{15} + 4u^{14} + \dots + 4u^2 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{15} + \frac{9}{2}u^{14} + \dots + \frac{3}{2}u - \frac{3}{2} \\ u^{15} - \frac{7}{2}u^{14} + \dots - \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^9 + 3u^8 - 9u^7 + 17u^6 - 25u^5 + 30u^4 - 26u^3 + 18u^2 - 9u + 3 \\ \frac{1}{2}u^{15} - \frac{3}{2}u^{14} + \dots - \frac{15}{2}u^2 + \frac{5}{2}u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^9 + 3u^8 - 9u^7 + 17u^6 - 25u^5 + 30u^4 - 26u^3 + 18u^2 - 9u + 3 \\ \frac{1}{2}u^{15} - \frac{3}{2}u^{14} + \dots - \frac{15}{2}u^2 + \frac{5}{2}u \end{pmatrix}$$

(ii) Obstruction class = 1

$$(iii) \text{ Cusp Shapes} = \frac{3}{2}u^{15} - 4u^{14} + \frac{35}{2}u^{13} - 37u^{12} + \frac{171}{2}u^{11} - 150u^{10} + 239u^9 - \frac{683}{2}u^8 + 402u^7 - \frac{863}{2}u^6 + \frac{727}{2}u^5 - \frac{503}{2}u^4 + \frac{255}{2}u^3 - \frac{71}{2}u^2 - \frac{19}{2}$$

**(iv) u-Polynomials at the component**

| Crossings        | u-Polynomials at each crossing         |
|------------------|--|
| $c_1$            | $u^{16} + 5u^{14} + \cdots - u + 1$    |
| $c_2$            | $u^{16} - 9u^{15} + \cdots - 3u + 1$   |
| $c_3, c_6$       | $u^{16} + 4u^{15} + \cdots + 4u + 1$   |
| $c_4, c_8$       | $u^{16} + 2u^{14} + \cdots - 4u + 1$   |
| $c_5, c_9$       | $u^{16} + u^{15} + \cdots - 2u + 1$    |
| $c_7$            | $u^{16} - 4u^{15} + \cdots + 2u^2 + 1$ |
| $c_{10}, c_{11}$ | $u^{16} + 4u^{15} + \cdots + 2u^2 + 1$ |

**(v) Riley Polynomials at the component**

| Crossings             | Riley Polynomials at each crossing    |
|-----------------------|---------------------------------------|
| $c_1$                 | $y^{16} + 10y^{15} + \cdots - y + 1$  |
| $c_2$                 | $y^{16} + y^{15} + \cdots - 7y + 1$   |
| $c_3, c_6$            | $y^{16} - 4y^{15} + \cdots - 10y + 1$ |
| $c_4, c_8$            | $y^{16} + 4y^{15} + \cdots - 4y + 1$  |
| $c_5, c_9$            | $y^{16} - 9y^{15} + \cdots - 14y + 1$ |
| $c_7, c_{10}, c_{11}$ | $y^{16} + 16y^{15} + \cdots + 4y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|------------------------------|---------------------------------------|-----------------------|
| $u = 0.952498 + 0.131115I$   |                                       |                       |
| $a = 0.0033545 + 0.0725748I$ | $-2.50830 + 0.01138I$                 | $-21.2199 - 7.8586I$  |
| $b = -0.484458 + 0.127312I$  |                                       |                       |
| $u = 0.952498 - 0.131115I$   |                                       |                       |
| $a = 0.0033545 - 0.0725748I$ | $-2.50830 - 0.01138I$                 | $-21.2199 + 7.8586I$  |
| $b = -0.484458 - 0.127312I$  |                                       |                       |
| $u = 0.125713 + 0.947117I$   |                                       |                       |
| $a = 1.200340 + 0.568422I$   | $-1.31298 + 1.09614I$                 | $-16.2051 - 0.8717I$  |
| $b = -0.892721 + 0.414975I$  |                                       |                       |
| $u = 0.125713 - 0.947117I$   |                                       |                       |
| $a = 1.200340 - 0.568422I$   | $-1.31298 - 1.09614I$                 | $-16.2051 + 0.8717I$  |
| $b = -0.892721 - 0.414975I$  |                                       |                       |
| $u = 0.714113 + 0.457971I$   |                                       |                       |
| $a = -0.502410 + 0.579452I$  | $-2.01872 - 4.33323I$                 | $-6.23875 + 5.22511I$ |
| $b = -0.900844 - 0.800511I$  |                                       |                       |
| $u = 0.714113 - 0.457971I$   |                                       |                       |
| $a = -0.502410 - 0.579452I$  | $-2.01872 + 4.33323I$                 | $-6.23875 - 5.22511I$ |
| $b = -0.900844 + 0.800511I$  |                                       |                       |
| $u = 0.054385 + 1.271360I$   |                                       |                       |
| $a = 0.45585 + 1.52893I$     | $0.41258 - 2.25313I$                  | $-9.04909 + 3.10995I$ |
| $b = -1.058410 - 0.722202I$  |                                       |                       |
| $u = 0.054385 - 1.271360I$   |                                       |                       |
| $a = 0.45585 - 1.52893I$     | $0.41258 + 2.25313I$                  | $-9.04909 - 3.10995I$ |
| $b = -1.058410 + 0.722202I$  |                                       |                       |
| $u = -0.063174 + 1.362500I$  |                                       |                       |
| $a = -0.48160 - 1.76041I$    | $1.66646 + 6.43037I$                  | $-4.55872 - 3.61803I$ |
| $b = 1.11324 + 0.91407I$     |                                       |                       |
| $u = -0.063174 - 1.362500I$  |                                       |                       |
| $a = -0.48160 + 1.76041I$    | $1.66646 - 6.43037I$                  | $-4.55872 + 3.61803I$ |
| $b = 1.11324 - 0.91407I$     |                                       |                       |

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.27182 + 1.50460I$    | $4.36105 - 7.99836I$                  | $-2.22876 + 4.36122I$ |
| $a = 0.13400 + 1.67219I$    |                                       |                       |
| $b = -0.99955 - 1.16424I$   |                                       |                       |
| $u = 0.27182 - 1.50460I$    | $4.36105 + 7.99836I$                  | $-2.22876 - 4.36122I$ |
| $a = 0.13400 - 1.67219I$    |                                       |                       |
| $b = -0.99955 + 1.16424I$   |                                       |                       |
| $u = 0.14710 + 1.63403I$    | $5.13996 - 4.97309I$                  | $-0.40575 + 9.40850I$ |
| $a = -0.154905 - 0.738372I$ |                                       |                       |
| $b = 0.471140 + 0.478511I$  |                                       |                       |
| $u = 0.14710 - 1.63403I$    | $5.13996 + 4.97309I$                  | $-0.40575 - 9.40850I$ |
| $a = -0.154905 + 0.738372I$ |                                       |                       |
| $b = 0.471140 - 0.478511I$  |                                       |                       |
| $u = -0.202461 + 0.214174I$ | $-2.45018 - 5.54449I$                 | $-4.59390 + 4.01193I$ |
| $a = -3.65462 - 0.29825I$   |                                       |                       |
| $b = 0.751612 - 0.466846I$  |                                       |                       |
| $u = -0.202461 - 0.214174I$ | $-2.45018 + 5.54449I$                 | $-4.59390 - 4.01193I$ |
| $a = -3.65462 + 0.29825I$   |                                       |                       |
| $b = 0.751612 + 0.466846I$  |                                       |                       |

$$\text{IV. } I_1^v = \langle a, b^2 - b + 1, v - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -b + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -b + 2 \\ -b + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -b + 2 \\ -b + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4b - 2$

**(iv) u-Polynomials at the component**

| Crossings                          | u-Polynomials at each crossing |
|------------------------------------|--------------------------------|
| $c_1$                              | $u^2 - u + 1$                  |
| $c_2, c_7, c_{10}$<br>$c_{11}$     | $u^2$                          |
| $c_3, c_4, c_5$<br>$c_6, c_8, c_9$ | $u^2 + u + 1$                  |

**(v) Riley Polynomials at the component**

| Crossings                                   | Riley Polynomials at each crossing |
|---|------------------------------------|
| $c_1, c_3, c_4$<br>$c_5, c_6, c_8$<br>$c_9$ | $y^2 + y + 1$                      |
| $c_2, c_7, c_{10}$<br>$c_{11}$              | $y^2$                              |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_1^v$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape      |
|----------------------------|---------------------------------------|-----------------|
| $v = 1.00000$              |                                       |                 |
| $a = 0$                    | $- 2.02988I$                          | $0. + 3.46410I$ |
| $b = 0.500000 + 0.866025I$ |                                       |                 |
| $v = 1.00000$              |                                       |                 |
| $a = 0$                    | $2.02988I$                            | $0. - 3.46410I$ |
| $b = 0.500000 - 0.866025I$ |                                       |                 |

## V. u-Polynomials

| Crossings        | u-Polynomials at each crossing  |
|------------------|---|
| $c_1$            | $(u^2 - u + 1)(u^2 + u + 1)^{30}(u^{16} + 5u^{14} + \dots - u + 1)$<br>$\cdot (u^{31} - 24u^{30} + \dots - 360448u + 32768)$              |
| $c_2$            | $u^2(u^{15} + 7u^{14} + \dots - 4u^2 + 1)^4(u^{16} - 9u^{15} + \dots - 3u + 1)$<br>$\cdot (u^{31} - 22u^{30} + \dots + 419u - 73)$        |
| $c_3, c_6$       | $(u^2 + u + 1)(u^{16} + 4u^{15} + \dots + 4u + 1)(u^{31} + u^{30} + \dots + 14u + 1)$<br>$\cdot (u^{60} + u^{59} + \dots + 12u + 7)$      |
| $c_4, c_8$       | $(u^2 + u + 1)(u^{16} + 2u^{14} + \dots - 4u + 1)(u^{31} - u^{30} + \dots - 2u + 1)$<br>$\cdot (u^{60} - u^{59} + \dots - 19478u + 3673)$ |
| $c_5, c_9$       | $(u^2 + u + 1)(u^{16} + u^{15} + \dots - 2u + 1)(u^{31} + u^{29} + \dots + 2u + 1)$<br>$\cdot (u^{60} - u^{59} + \dots + 6u + 1)$         |
| $c_7$            | $u^2(u^{15} + 3u^{14} + \dots - 4u^2 + 1)^4(u^{16} - 4u^{15} + \dots + 2u^2 + 1)$<br>$\cdot (u^{31} - 9u^{30} + \dots - 608u + 73)$       |
| $c_{10}, c_{11}$ | $u^2(u^{15} + 3u^{14} + \dots - 4u^2 + 1)^4(u^{16} + 4u^{15} + \dots + 2u^2 + 1)$<br>$\cdot (u^{31} - 9u^{30} + \dots - 608u + 73)$       |

## VI. Riley Polynomials

| Crossings             | Riley Polynomials at each crossing  |
|-----------------------|---|
| $c_1$                 | $((y^2 + y + 1)^{31})(y^{16} + 10y^{15} + \dots - y + 1)$<br>$\cdot (y^{31} + 10y^{30} + \dots - 2147483648y - 1073741824)$                           |
| $c_2$                 | $y^2(y^{15} - y^{14} + \dots + 8y - 1)^4(y^{16} + y^{15} + \dots - 7y + 1)$<br>$\cdot (y^{31} + 46y^{29} + \dots + 42263y - 5329)$                    |
| $c_3, c_6$            | $(y^2 + y + 1)(y^{16} - 4y^{15} + \dots - 10y + 1)(y^{31} + 15y^{30} + \dots + 110y - 1)$<br>$\cdot (y^{60} - 9y^{59} + \dots - 256y + 49)$           |
| $c_4, c_8$            | $(y^2 + y + 1)(y^{16} + 4y^{15} + \dots - 4y + 1)(y^{31} + 7y^{30} + \dots - 40y - 1)$<br>$\cdot (y^{60} + 15y^{59} + \dots + 261046488y + 13490929)$ |
| $c_5, c_9$            | $(y^2 + y + 1)(y^{16} - 9y^{15} + \dots - 14y + 1)(y^{31} + 2y^{30} + \dots - 6y - 1)$<br>$\cdot (y^{60} - 21y^{59} + \dots - 228y^2 + 1)$            |
| $c_7, c_{10}, c_{11}$ | $y^2(y^{15} + 15y^{14} + \dots + 8y - 1)^4(y^{16} + 16y^{15} + \dots + 4y + 1)$<br>$\cdot (y^{31} + 31y^{30} + \dots - 37092y - 5329)$                |