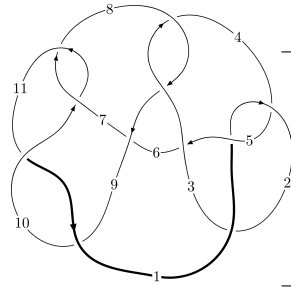
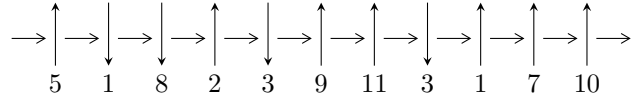


## 11n<sub>3</sub> (K11n<sub>3</sub>)



A knot diagram<sup>1</sup>

### Linearized knot diagram



### Solving Sequence

$$7,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 3,8 \xrightarrow{c_3} 4 \xrightarrow{c_{11}} 1 \xrightarrow{c_2} 2 \xrightarrow{c_9} 9 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \longrightarrow c_1, c_4, c_8$$

### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -5u^{26} + 11u^{25} + \dots + 2b - 5, u^{25} - 2u^{24} + \dots + 2a + 5u, u^{27} - 3u^{26} + \dots + 3u - 1 \rangle$$

$$I_2^u = \langle u^2a + b - a, -u^2a + a^2 - au + u + 1, u^3 + u^2 - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 33 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATSTAILS/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -5u^{26} + 11u^{25} + \dots + 2b - 5, u^{25} - 2u^{24} + \dots + 2a + 5u, u^{27} - 3u^{26} + \dots + 3u - 1 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{2}u^{25} + u^{24} + \dots + \frac{15}{2}u^2 - \frac{5}{2}u \\ \frac{1}{2}u^{26} - \frac{11}{2}u^{25} + \dots - 5u + \frac{3}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{26} + \frac{5}{2}u^{25} + \dots + \frac{3}{2}u - 2 \\ \frac{1}{2}u^{26} - \frac{3}{2}u^{25} + \dots + 5u^2 + \frac{1}{2} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{25} + \frac{3}{2}u^{24} + \dots - \frac{3}{2}u - \frac{1}{2} \\ 2u^{26} - 5u^{25} + \dots - 4u + 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 - u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^9 + 2u^7 - 3u^5 + 2u^3 - u \\ -u^9 + u^7 - u^5 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{2}u^{25} - u^{24} + \dots + \frac{3}{2}u - 1 \\ -\frac{1}{2}u^{26} + \frac{3}{2}u^{25} + \dots + 3u - \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{2}u^{25} - u^{24} + \dots + \frac{3}{2}u - 1 \\ -\frac{1}{2}u^{26} + \frac{3}{2}u^{25} + \dots + 3u - \frac{1}{2} \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $\frac{23}{2}u^{26} - 24u^{25} + \dots - \frac{69}{2}u + \frac{25}{2}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{27} + 4u^{26} + \dots + 4u + 1$
$c_2$	$u^{27} + 6u^{26} + \dots + 4u - 1$
$c_3, c_8$	$u^{27} - u^{26} + \dots - 32u - 64$
$c_5$	$u^{27} - 4u^{26} + \dots + 6988u + 1153$
$c_6$	$u^{27} + 3u^{26} + \dots - u - 1$
$c_7, c_{10}$	$u^{27} - 3u^{26} + \dots + 3u - 1$
$c_9, c_{11}$	$u^{27} - 11u^{26} + \dots - 9u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{27} + 6y^{26} + \dots + 4y - 1$
$c_2$	$y^{27} + 34y^{26} + \dots + 136y - 1$
$c_3, c_8$	$y^{27} + 35y^{26} + \dots + 1024y - 4096$
$c_5$	$y^{27} + 62y^{26} + \dots - 7660244y - 1329409$
$c_6$	$y^{27} - 47y^{26} + \dots - 9y - 1$
$c_7, c_{10}$	$y^{27} - 11y^{26} + \dots - 9y - 1$
$c_9, c_{11}$	$y^{27} + 13y^{26} + \dots + 127y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.456584 + 0.907647I$ $a = -1.48477 - 0.61163I$ $b = -1.25986 + 0.88956I$	$7.22245 + 1.02048I$	$3.69178 - 1.94630I$
$u = 0.456584 - 0.907647I$ $a = -1.48477 + 0.61163I$ $b = -1.25986 - 0.88956I$	$7.22245 - 1.02048I$	$3.69178 + 1.94630I$
$u = 0.964922 + 0.396644I$ $a = -0.252553 + 0.564190I$ $b = 1.21469 + 1.07115I$	$2.07980 + 1.34949I$	$7.85827 - 1.99966I$
$u = 0.964922 - 0.396644I$ $a = -0.252553 - 0.564190I$ $b = 1.21469 - 1.07115I$	$2.07980 - 1.34949I$	$7.85827 + 1.99966I$
$u = 0.524863 + 0.914721I$ $a = 1.55069 + 0.62247I$ $b = 1.39313 - 0.99095I$	$6.79111 - 5.64536I$	$3.12437 + 2.66728I$
$u = 0.524863 - 0.914721I$ $a = 1.55069 - 0.62247I$ $b = 1.39313 + 0.99095I$	$6.79111 + 5.64536I$	$3.12437 - 2.66728I$
$u = -0.974186 + 0.462885I$ $a = 0.529071 - 0.939257I$ $b = 0.169302 - 0.547843I$	$1.69325 - 4.38642I$	$5.48340 + 6.16823I$
$u = -0.974186 - 0.462885I$ $a = 0.529071 + 0.939257I$ $b = 0.169302 + 0.547843I$	$1.69325 + 4.38642I$	$5.48340 - 6.16823I$
$u = -0.838777 + 0.356107I$ $a = -1.00459 + 1.02558I$ $b = -0.373891 + 0.589972I$	$0.942185 + 1.033980I$	$3.86006 + 2.18156I$
$u = -0.838777 - 0.356107I$ $a = -1.00459 - 1.02558I$ $b = -0.373891 - 0.589972I$	$0.942185 - 1.033980I$	$3.86006 - 2.18156I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.685911 + 0.573005I$		
$a = 1.282770 - 0.152453I$	$-1.54191 - 1.16661I$	$0.74423 + 1.49202I$
$b = 0.13458 - 1.76175I$		
$u = 0.685911 - 0.573005I$		
$a = 1.282770 + 0.152453I$	$-1.54191 + 1.16661I$	$0.74423 - 1.49202I$
$b = 0.13458 + 1.76175I$		
$u = -0.821117 + 0.748475I$		
$a = -0.420089 - 0.037335I$	$-3.44772 - 1.77523I$	$-1.86458 + 4.75426I$
$b = -0.229956 + 0.061310I$		
$u = -0.821117 - 0.748475I$		
$a = -0.420089 + 0.037335I$	$-3.44772 + 1.77523I$	$-1.86458 - 4.75426I$
$b = -0.229956 - 0.061310I$		
$u = 0.960749 + 0.570989I$		
$a = 0.404574 - 1.204920I$	$-0.68885 + 5.76088I$	$3.34925 - 6.52520I$
$b = -1.74421 - 1.76576I$		
$u = 0.960749 - 0.570989I$		
$a = 0.404574 + 1.204920I$	$-0.68885 - 5.76088I$	$3.34925 + 6.52520I$
$b = -1.74421 + 1.76576I$		
$u = 0.866757$		
$a = -0.0957077$	$1.43125$	$6.84050$
$b = 0.622584$		
$u = -0.922854 + 0.737156I$		
$a = 0.035124 - 0.374638I$	$-3.14099 - 3.86941I$	$0.026459 + 0.626604I$
$b = -0.045924 - 0.210874I$		
$u = -0.922854 - 0.737156I$		
$a = 0.035124 + 0.374638I$	$-3.14099 + 3.86941I$	$0.026459 - 0.626604I$
$b = -0.045924 + 0.210874I$		
$u = -1.242910 + 0.029552I$		
$a = 0.02740 - 1.50043I$	$13.47880 - 3.52700I$	$8.35802 + 2.34346I$
$b = 0.006371 - 0.831742I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.242910 - 0.029552I$ $a = 0.02740 + 1.50043I$ $b = 0.006371 + 0.831742I$	$13.47880 + 3.52700I$	$8.35802 - 2.34346I$
$u = 1.135150 + 0.655354I$ $a = 0.445958 + 1.202700I$ $b = 2.34089 + 0.91299I$	$9.30444 + 4.72653I$	$5.93859 - 2.37138I$
$u = 1.135150 - 0.655354I$ $a = 0.445958 - 1.202700I$ $b = 2.34089 - 0.91299I$	$9.30444 - 4.72653I$	$5.93859 + 2.37138I$
$u = 1.118230 + 0.692002I$ $a = -0.51886 - 1.31753I$ $b = -2.49328 - 0.90508I$	$8.6132 + 11.5634I$	$4.87720 - 6.78953I$
$u = 1.118230 - 0.692002I$ $a = -0.51886 + 1.31753I$ $b = -2.49328 + 0.90508I$	$8.6132 - 11.5634I$	$4.87720 + 6.78953I$
$u = 0.020052 + 0.347458I$ $a = -1.54687 - 0.86649I$ $b = -0.423137 + 0.416168I$	$-0.075638 + 1.377020I$	$-0.36727 - 4.75192I$
$u = 0.020052 - 0.347458I$ $a = -1.54687 + 0.86649I$ $b = -0.423137 - 0.416168I$	$-0.075638 - 1.377020I$	$-0.36727 + 4.75192I$

$$\text{II. } I_2^u = \langle u^2a + b - a, -u^2a + a^2 - au + u + 1, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -u^2a + a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -u^2a + a \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2a + au \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 - 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a - u - 1 \\ -u^2a + a \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a - u - 1 \\ -u^2a + a \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $u^2a + 6au - u^2 + 2u + 1$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$(u^2 + u + 1)^3$
$c_3, c_8$	$u^6$
$c_4$	$(u^2 - u + 1)^3$
$c_6, c_9$	$(u^3 + u^2 + 2u + 1)^2$
$c_7$	$(u^3 - u^2 + 1)^2$
$c_{10}$	$(u^3 + u^2 - 1)^2$
$c_{11}$	$(u^3 - u^2 + 2u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5$	$(y^2 + y + 1)^3$
$c_3, c_8$	$y^6$
$c_6, c_9, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_7, c_{10}$	$(y^3 - y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$ $a = -0.818128 + 0.292480I$ $b = -1.024480 - 0.839835I$	$-3.02413 - 4.85801I$	$0.94625 + 7.60556I$
$u = -0.877439 + 0.744862I$ $a = 0.155769 - 0.854759I$ $b = 1.239560 - 0.467306I$	$-3.02413 - 0.79824I$	$2.23639 - 1.26697I$
$u = -0.877439 - 0.744862I$ $a = -0.818128 - 0.292480I$ $b = -1.024480 + 0.839835I$	$-3.02413 + 4.85801I$	$0.94625 - 7.60556I$
$u = -0.877439 - 0.744862I$ $a = 0.155769 + 0.854759I$ $b = 1.239560 + 0.467306I$	$-3.02413 + 0.79824I$	$2.23639 + 1.26697I$
$u = 0.754878$ $a = 0.662359 + 1.147240I$ $b = 0.284920 + 0.493496I$	$1.11345 - 2.02988I$	$5.31735 + 5.84990I$
$u = 0.754878$ $a = 0.662359 - 1.147240I$ $b = 0.284920 - 0.493496I$	$1.11345 + 2.02988I$	$5.31735 - 5.84990I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 + u + 1)^3)(u^{27} + 4u^{26} + \dots + 4u + 1)$
$c_2$	$((u^2 + u + 1)^3)(u^{27} + 6u^{26} + \dots + 4u - 1)$
$c_3, c_8$	$u^6(u^{27} - u^{26} + \dots - 32u - 64)$
$c_4$	$((u^2 - u + 1)^3)(u^{27} + 4u^{26} + \dots + 4u + 1)$
$c_5$	$((u^2 + u + 1)^3)(u^{27} - 4u^{26} + \dots + 6988u + 1153)$
$c_6$	$((u^3 + u^2 + 2u + 1)^2)(u^{27} + 3u^{26} + \dots - u - 1)$
$c_7$	$((u^3 - u^2 + 1)^2)(u^{27} - 3u^{26} + \dots + 3u - 1)$
$c_9$	$((u^3 + u^2 + 2u + 1)^2)(u^{27} - 11u^{26} + \dots - 9u - 1)$
$c_{10}$	$((u^3 + u^2 - 1)^2)(u^{27} - 3u^{26} + \dots + 3u - 1)$
$c_{11}$	$((u^3 - u^2 + 2u - 1)^2)(u^{27} - 11u^{26} + \dots - 9u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y^2 + y + 1)^3)(y^{27} + 6y^{26} + \dots + 4y - 1)$
$c_2$	$((y^2 + y + 1)^3)(y^{27} + 34y^{26} + \dots + 136y - 1)$
$c_3, c_8$	$y^6(y^{27} + 35y^{26} + \dots + 1024y - 4096)$
$c_5$	$((y^2 + y + 1)^3)(y^{27} + 62y^{26} + \dots - 7660244y - 1329409)$
$c_6$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{27} - 47y^{26} + \dots - 9y - 1)$
$c_7, c_{10}$	$((y^3 - y^2 + 2y - 1)^2)(y^{27} - 11y^{26} + \dots - 9y - 1)$
$c_9, c_{11}$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{27} + 13y^{26} + \dots + 127y - 1)$