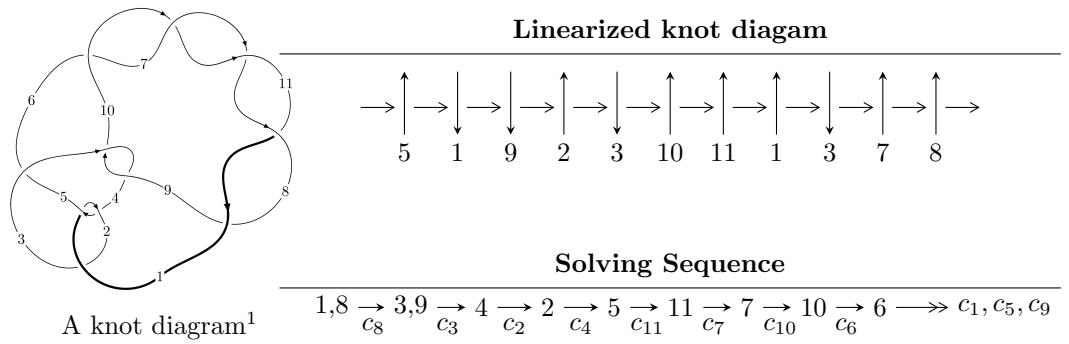


## $11n_{19}$ ( $K11n_{19}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle u^5 + u^4 - 3u^3 - 3u^2 + 2u - 3u - 1, u^4 - 5u^2 + 2u + 3, u^6 + 3u^5 - 2u^4 - 11u^3 - 6u^2 - u - 1 \rangle$$

$$I_2^u = \langle au + b + a, a^2 + au - a - u + 2, u^2 - u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 10 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^5 + u^4 - 3u^3 - 3u^2 + 2u - 1, u^4 - 5u^2 + 2u + 3, u^6 + 3u^5 - 2u^4 - 11u^3 - 6u^2 - u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -\frac{1}{2}u^4 + \frac{5}{2}u^2 - \frac{3}{2} \\ -\frac{1}{2}u^5 - \frac{1}{2}u^4 + \cdots + \frac{3}{2}u + \frac{1}{2} \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^5 - \frac{3}{2}u^4 + 4u^3 + \frac{11}{2}u^2 - u - \frac{3}{2} \\ \frac{7}{2}u^5 + \frac{7}{2}u^4 + \cdots + \frac{1}{2}u - \frac{3}{2} \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{1}{2}u^4 + \frac{5}{2}u^2 - \frac{3}{2} \\ -2u^5 - 2u^4 + 7u^3 + 6u^2 + 2u + 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} \frac{1}{2}u^4 + u^3 - \frac{3}{2}u^2 - 4u - \frac{3}{2} \\ \frac{1}{2}u^5 + \frac{1}{2}u^4 + \cdots + \frac{1}{2}u - \frac{1}{2} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^4 - 3u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^4 - 3u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{3}{2}u^5 - 5u^4 + \frac{7}{2}u^3 + 20u^2 + \frac{15}{2}u + 4$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^6 + 3u^5 + 4u^4 + u^3 + 3u + 1$
$c_2$	$u^6 - u^5 + 10u^4 - 17u^3 + 2u^2 - 9u + 1$
$c_3, c_9$	$u^6 + 6u^5 + 28u^4 + 60u^3 + 20u^2 - 16u - 16$
$c_5$	$u^6 - 3u^5 + 12u^4 + 127u^3 + 52u^2 + 113u + 41$
$c_6, c_7, c_8$ $c_{10}, c_{11}$	$u^6 - 3u^5 - 2u^4 + 11u^3 - 6u^2 + u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^6 - y^5 + 10y^4 - 17y^3 + 2y^2 - 9y + 1$
$c_2$	$y^6 + 19y^5 + 70y^4 - 265y^3 - 282y^2 - 77y + 1$
$c_3, c_9$	$y^6 + 20y^5 + 104y^4 - 2320y^3 + 1424y^2 - 896y + 256$
$c_5$	$y^6 + 15y^5 + 1010y^4 - 14121y^3 - 25014y^2 - 8505y + 1681$
$c_6, c_7, c_8$ $c_{10}, c_{11}$	$y^6 - 13y^5 + 58y^4 - 93y^3 + 18y^2 + 11y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.787648$		
$a = -0.141467$	1.36678	7.32050
$b = -0.524726$		
$u = 0.049860 + 0.377590I$		
$a = -1.85932 + 0.09941I$	0.088081 - 1.387970I	1.39961 + 3.44965I
$b = 0.321306 + 0.548438I$		
$u = 0.049860 - 0.377590I$		
$a = -1.85932 - 0.09941I$	0.088081 + 1.387970I	1.39961 - 3.44965I
$b = 0.321306 - 0.548438I$		
$u = 1.93055$		
$a = 0.872199$	11.1902	8.52400
$b = -0.574576$		
$u = -2.12131 + 0.18327I$		
$a = -0.00604 + 1.52892I$	-11.30140 - 4.76989I	7.67813 + 1.77109I
$b = 0.22835 - 2.85610I$		
$u = -2.12131 - 0.18327I$		
$a = -0.00604 - 1.52892I$	-11.30140 + 4.76989I	7.67813 - 1.77109I
$b = 0.22835 + 2.85610I$		

$$\text{III. } I_2^u = \langle au + b + a, \ a^2 + au - a - u + 2, \ u^2 - u - 1 \rangle$$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -au - a \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -au - a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -2au - 2a \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a + u - 1 \\ -au - a - 2u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-3au + 2a + u + 4$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$(u^2 + u + 1)^2$
$c_3, c_9$	$u^4$
$c_4$	$(u^2 - u + 1)^2$
$c_6, c_7, c_8$	$(u^2 - u - 1)^2$
$c_{10}, c_{11}$	$(u^2 + u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5$	$(y^2 + y + 1)^2$
$c_3, c_9$	$y^4$
$c_6, c_7, c_8$ $c_{10}, c_{11}$	$(y^2 - 3y + 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$		
$a = 0.80902 + 1.40126I$	$0.98696 - 2.02988I$	$6.50000 + 5.40059I$
$b = -0.309017 - 0.535233I$		
$u = -0.618034$		
$a = 0.80902 - 1.40126I$	$0.98696 + 2.02988I$	$6.50000 - 5.40059I$
$b = -0.309017 + 0.535233I$		
$u = 1.61803$		
$a = -0.309017 + 0.535233I$	$8.88264 + 2.02988I$	$6.50000 - 1.52761I$
$b = 0.80902 - 1.40126I$		
$u = 1.61803$		
$a = -0.309017 - 0.535233I$	$8.88264 - 2.02988I$	$6.50000 + 1.52761I$
$b = 0.80902 + 1.40126I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 + u + 1)^2(u^6 + 3u^5 + 4u^4 + u^3 + 3u + 1)$
$c_2$	$(u^2 + u + 1)^2(u^6 - u^5 + 10u^4 - 17u^3 + 2u^2 - 9u + 1)$
$c_3, c_9$	$u^4(u^6 + 6u^5 + 28u^4 + 60u^3 + 20u^2 - 16u - 16)$
$c_4$	$(u^2 - u + 1)^2(u^6 + 3u^5 + 4u^4 + u^3 + 3u + 1)$
$c_5$	$(u^2 + u + 1)^2(u^6 - 3u^5 + 12u^4 + 127u^3 + 52u^2 + 113u + 41)$
$c_6, c_7, c_8$	$(u^2 - u - 1)^2(u^6 - 3u^5 - 2u^4 + 11u^3 - 6u^2 + u - 1)$
$c_{10}, c_{11}$	$(u^2 + u - 1)^2(u^6 - 3u^5 - 2u^4 + 11u^3 - 6u^2 + u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^2 + y + 1)^2(y^6 - y^5 + 10y^4 - 17y^3 + 2y^2 - 9y + 1)$
$c_2$	$(y^2 + y + 1)^2(y^6 + 19y^5 + 70y^4 - 265y^3 - 282y^2 - 77y + 1)$
$c_3, c_9$	$y^4(y^6 + 20y^5 + 104y^4 - 2320y^3 + 1424y^2 - 896y + 256)$
$c_5$	$(y^2 + y + 1)^2 \cdot (y^6 + 15y^5 + 1010y^4 - 14121y^3 - 25014y^2 - 8505y + 1681)$
$c_6, c_7, c_8$ $c_{10}, c_{11}$	$(y^2 - 3y + 1)^2(y^6 - 13y^5 + 58y^4 - 93y^3 + 18y^2 + 11y + 1)$