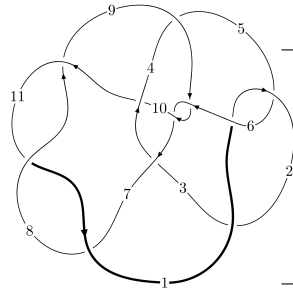
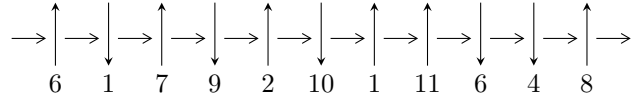


11n<sub>49</sub> (K11n<sub>49</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$1,7 \xrightarrow{c_7} 8,10 \xrightarrow{c_6} 6 \xrightarrow{c_1} 2 \xrightarrow{c_2} 3 \xrightarrow{c_3} 4 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \xrightarrow{c_{11}} 11 \rightsquigarrow c_4, c_8, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^5 + u^4 - 4u^3 + 6b - 6u - 2, u^3 - 2u^2 + 4a + 4u - 2, u^6 - 2u^5 + 8u^4 - 4u^3 + 12u^2 + 8u + 4 \rangle$$

$$I_2^u = \langle b + 1, 2a^2 + au + 4a + u + 1, u^2 + 2 \rangle$$

$$I_1^v = \langle a, b - 1, v^2 - v + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 12 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^5 + u^4 - 4u^3 + 6b - 6u - 2, u^3 - 2u^2 + 4a + 4u - 2, u^6 - 2u^5 + 8u^4 - 4u^3 + 12u^2 + 8u + 4 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{4}u^3 + \frac{1}{2}u^2 - u + \frac{1}{2} \\ \frac{1}{6}u^5 - \frac{1}{6}u^4 + \frac{2}{3}u^3 + u + \frac{1}{3} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{12}u^5 + \frac{1}{3}u^4 + \dots + u^2 + \frac{5}{6} \\ -\frac{1}{3}u^5 + \frac{1}{3}u^4 - \frac{4}{3}u^3 + \frac{1}{3} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{6}u^5 - \frac{2}{3}u^4 + \frac{11}{12}u^3 - u^2 - \frac{1}{6} \\ u^5 - \frac{7}{4}u^4 + 3u^3 - 2u^2 - \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{6}u^5 - \frac{2}{3}u^4 + \frac{11}{12}u^3 - u^2 - \frac{1}{6} \\ -\frac{1}{12}u^5 + \frac{7}{12}u^4 + \dots + \frac{3}{2}u + \frac{1}{3} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{12}u^5 - \frac{1}{12}u^4 + \dots + \frac{3}{2}u + \frac{1}{6} \\ -\frac{1}{12}u^5 + \frac{7}{12}u^4 + \dots + \frac{3}{2}u + \frac{1}{3} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{3}u^5 + \frac{1}{6}u^4 + \frac{13}{12}u^3 - u + \frac{1}{6} \\ -0.416667u^5 + 5.416667u^4 + \dots + 8.50000u + 3.66667 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $u^5 - 2u^4 + 8u^3 - 5u^2 + 12u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^6 - 7u^5 + 30u^4 - 59u^3 + 78u^2 - 23u + 9$
$c_2$	$u^6 + 11u^5 + 230u^4 + 895u^3 + 3910u^2 + 875u + 81$
$c_3$	$u^6 - u^5 + 4u^4 + 203u^3 + 402u^2 - 199u + 127$
$c_4$	$u^6 - 13u^5 + 64u^4 - 127u^3 + 74u^2 + 17u + 41$
$c_6, c_9$	$u^6 + 4u^5 + 9u^4 + 8u^3 + 19u^2 + 4u + 3$
$c_7, c_8, c_{11}$	$u^6 + 2u^5 + 8u^4 + 4u^3 + 12u^2 - 8u + 4$
$c_{10}$	$u^6 + u^5 + 4u^4 + u^3 + 8u^2 + 5u + 3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^6 + 11y^5 + 230y^4 + 895y^3 + 3910y^2 + 875y + 81$
$c_2$	$y^6 + 339y^5 + \dots - 132205y + 6561$
$c_3$	$y^6 + 7y^5 + 1226y^4 - 38137y^3 + 243414y^2 + 62507y + 16129$
$c_4$	$y^6 - 41y^5 + 942y^4 - 6133y^3 + 15042y^2 + 5779y + 1681$
$c_6, c_9$	$y^6 + 2y^5 + 55y^4 + 252y^3 + 351y^2 + 98y + 9$
$c_7, c_8, c_{11}$	$y^6 + 12y^5 + 72y^4 + 216y^3 + 272y^2 + 32y + 16$
$c_{10}$	$y^6 + 7y^5 + 30y^4 + 59y^3 + 78y^2 + 23y + 9$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.327848 + 0.380167I$		
$a = 0.782599 - 0.521714I$	$0.080134 - 1.031470I$	$1.24075 + 6.28341I$
$b = 0.089037 + 0.417324I$		
$u = -0.327848 - 0.380167I$		
$a = 0.782599 + 0.521714I$	$0.080134 + 1.031470I$	$1.24075 - 6.28341I$
$b = 0.089037 - 0.417324I$		
$u = 0.31945 + 1.74021I$		
$a = -0.565198$	$-4.41014 - 1.50896I$	$-1.48189 + 1.11182I$
$b = -0.20409 + 1.44525I$		
$u = 0.31945 - 1.74021I$		
$a = -0.565198$	$-4.41014 + 1.50896I$	$-1.48189 - 1.11182I$
$b = -0.20409 - 1.44525I$		
$u = 1.00840 + 2.01334I$		
$a = 0.782599 + 0.521714I$	$9.26481 + 6.90911I$	$-1.75886 - 2.47219I$
$b = 2.11506 - 1.80559I$		
$u = 1.00840 - 2.01334I$		
$a = 0.782599 - 0.521714I$	$9.26481 - 6.90911I$	$-1.75886 + 2.47219I$
$b = 2.11506 + 1.80559I$		

$$\text{II. } I_2^u = \langle b + 1, 2a^2 + au + 4a + u + 1, u^2 + 2 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a + 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + \frac{1}{2}u + 1 \\ -au \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a + \frac{1}{2}u + 1 \\ -au - 2a - u - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -au - a - \frac{1}{2}u - 1 \\ -au - 2a - u - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a + \frac{1}{2}u + 1 \\ -au - 2a - u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4au - 4u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_{10}$	$(u^2 + u + 1)^2$
$c_3$	$u^4 - 2u^3 + u^2 - 6u + 9$
$c_4$	$u^4 + 2u^3 + u^2 + 6u + 9$
$c_5$	$(u^2 - u + 1)^2$
$c_6$	$(u + 1)^4$
$c_7, c_8, c_{11}$	$(u^2 + 2)^2$
$c_9$	$(u - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_{10}$	$(y^2 + y + 1)^2$
$c_3, c_4$	$y^4 - 2y^3 - 5y^2 - 18y + 81$
$c_6, c_9$	$(y - 1)^4$
$c_7, c_8, c_{11}$	$(y + 2)^4$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.414210I$ $a = -0.387628 - 0.353553I$ $b = -1.00000$	$-6.57974 + 2.02988I$	$-6.00000 - 3.46410I$
$u = 1.414210I$ $a = -1.61237 - 0.35355I$ $b = -1.00000$	$-6.57974 - 2.02988I$	$-6.00000 + 3.46410I$
$u = -1.414210I$ $a = -0.387628 + 0.353553I$ $b = -1.00000$	$-6.57974 - 2.02988I$	$-6.00000 + 3.46410I$
$u = -1.414210I$ $a = -1.61237 + 0.35355I$ $b = -1.00000$	$-6.57974 + 2.02988I$	$-6.00000 - 3.46410I$

$$\text{III. } I_1^v = \langle a, b - 1, v^2 - v + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2v \\ -v \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2v - 1 \\ -v \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v - 1 \\ -v \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2v - 1 \\ -v \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4v + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$u^2 + u + 1$
$c_3, c_4, c_5$ $c_{10}$	$u^2 - u + 1$
$c_6$	$(u - 1)^2$
$c_7, c_8, c_{11}$	$u^2$
$c_9$	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_{10}$	$y^2 + y + 1$
$c_6, c_9$	$(y - 1)^2$
$c_7, c_8, c_{11}$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.500000 + 0.866025I$ $a = 0$ $b = 1.00000$	$-1.64493 + 2.02988I$	$0. - 3.46410I$
$v = 0.500000 - 0.866025I$ $a = 0$ $b = 1.00000$	$-1.64493 - 2.02988I$	$0. + 3.46410I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 + u + 1)^3(u^6 - 7u^5 + 30u^4 - 59u^3 + 78u^2 - 23u + 9)$
$c_2$	$(u^2 + u + 1)^3(u^6 + 11u^5 + 230u^4 + 895u^3 + 3910u^2 + 875u + 81)$
$c_3$	$(u^2 - u + 1)(u^4 - 2u^3 + u^2 - 6u + 9)$ $\cdot (u^6 - u^5 + 4u^4 + 203u^3 + 402u^2 - 199u + 127)$
$c_4$	$(u^2 - u + 1)(u^4 + 2u^3 + u^2 + 6u + 9)$ $\cdot (u^6 - 13u^5 + 64u^4 - 127u^3 + 74u^2 + 17u + 41)$
$c_5$	$(u^2 - u + 1)^3(u^6 - 7u^5 + 30u^4 - 59u^3 + 78u^2 - 23u + 9)$
$c_6$	$(u - 1)^2(u + 1)^4(u^6 + 4u^5 + 9u^4 + 8u^3 + 19u^2 + 4u + 3)$
$c_7, c_8, c_{11}$	$u^2(u^2 + 2)^2(u^6 + 2u^5 + 8u^4 + 4u^3 + 12u^2 - 8u + 4)$
$c_9$	$(u - 1)^4(u + 1)^2(u^6 + 4u^5 + 9u^4 + 8u^3 + 19u^2 + 4u + 3)$
$c_{10}$	$(u^2 - u + 1)(u^2 + u + 1)^2(u^6 + u^5 + 4u^4 + u^3 + 8u^2 + 5u + 3)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$(y^2 + y + 1)^3(y^6 + 11y^5 + 230y^4 + 895y^3 + 3910y^2 + 875y + 81)$
$c_2$	$((y^2 + y + 1)^3)(y^6 + 339y^5 + \dots - 132205y + 6561)$
$c_3$	$(y^2 + y + 1)(y^4 - 2y^3 - 5y^2 - 18y + 81)$ $\cdot (y^6 + 7y^5 + 1226y^4 - 38137y^3 + 243414y^2 + 62507y + 16129)$
$c_4$	$(y^2 + y + 1)(y^4 - 2y^3 - 5y^2 - 18y + 81)$ $\cdot (y^6 - 41y^5 + 942y^4 - 6133y^3 + 15042y^2 + 5779y + 1681)$
$c_6, c_9$	$(y - 1)^6(y^6 + 2y^5 + 55y^4 + 252y^3 + 351y^2 + 98y + 9)$
$c_7, c_8, c_{11}$	$y^2(y + 2)^4(y^6 + 12y^5 + 72y^4 + 216y^3 + 272y^2 + 32y + 16)$
$c_{10}$	$(y^2 + y + 1)^3(y^6 + 7y^5 + 30y^4 + 59y^3 + 78y^2 + 23y + 9)$