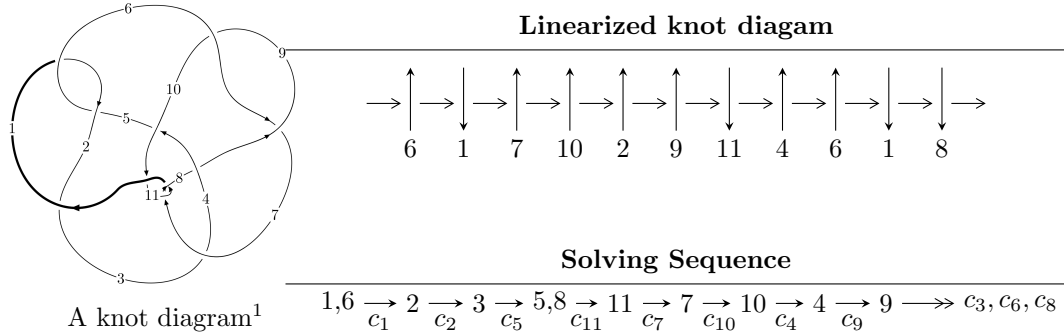


11n₅₀ (K11n₅₀)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 37910139708041u^{19} - 201150163381549u^{18} + \dots + 6011452100077376b - 7292662285169845, \\ - 4.50097 \times 10^{15}u^{19} - 1.28986 \times 10^{16}u^{18} + \dots + 3.00573 \times 10^{15}a - 7.74836 \times 10^{15}, u^{20} + 3u^{19} + \dots + 6u \rangle$$

$$I_2^u = \langle -au + b - u - 1, a^2 - 2au - u, u^2 + u + 1 \rangle$$

$$I_3^u = \langle au + b + a - u - 1, a^2 - 2a + 2, u^2 + u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 28 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 3.79 \times 10^{13} u^{19} - 2.01 \times 10^{14} u^{18} + \dots + 6.01 \times 10^{15} b - 7.29 \times 10^{15}, -4.50 \times 10^{15} u^{19} - 1.29 \times 10^{16} u^{18} + \dots + 3.01 \times 10^{15} a - 7.75 \times 10^{15}, u^{20} + 3u^{19} + \dots + 6u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1.49747u^{19} + 4.29134u^{18} + \dots + 24.6486u + 2.57787 \\ -0.00630632u^{19} + 0.0334612u^{18} + \dots + 3.09219u + 1.21313 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1.01016u^{19} - 2.81974u^{18} + \dots - 13.1176u + 2.12976 \\ -0.147188u^{19} - 0.390662u^{18} + \dots - 5.99436u - 1.23581 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1.20441u^{19} + 3.56367u^{18} + \dots + 29.2504u + 7.54341 \\ -0.127524u^{19} - 0.273202u^{18} + \dots - 3.26181u + 0.411467 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1.15735u^{19} - 3.21040u^{18} + \dots - 19.1120u + 0.893945 \\ -0.147188u^{19} - 0.390662u^{18} + \dots - 5.99436u - 1.23581 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1.07688u^{19} - 3.29047u^{18} + \dots - 25.9886u - 7.95487 \\ 0.115875u^{19} + 0.263182u^{18} + \dots + 4.66274u - 0.262787 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1.15735u^{19} - 3.21040u^{18} + \dots - 19.1120u + 0.893945 \\ -0.201060u^{19} - 0.575464u^{18} + \dots - 6.40693u - 1.49747 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1.15735u^{19} - 3.21040u^{18} + \dots - 19.1120u + 0.893945 \\ -0.201060u^{19} - 0.575464u^{18} + \dots - 6.40693u - 1.49747 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{4709825960466509}{3005726050038688} u^{19} + \frac{3061022262562929}{751431512509672} u^{18} + \dots + \frac{62732012609244425}{3005726050038688} u + \frac{4116636408312339}{751431512509672}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$u^{20} - 3u^{19} + \dots - 6u + 1$
c_2	$u^{20} + 33u^{19} + \dots - 6u + 1$
c_3	$u^{20} + u^{19} + \dots + 1264u + 517$
c_4	$u^{20} + u^{19} + \dots + 1876u + 647$
c_6, c_9	$u^{20} + u^{19} + \dots + 12u + 4$
c_7, c_{11}	$u^{20} + u^{19} + \dots + 6u + 1$
c_8	$u^{20} + u^{19} + \dots + 4u + 1$
c_{10}	$u^{20} + 15u^{19} + \dots + 22u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5	$y^{20} + 33y^{19} + \dots - 6y + 1$
c_2	$y^{20} - 87y^{19} + \dots + 770y + 1$
c_3	$y^{20} + 27y^{19} + \dots + 842544y + 267289$
c_4	$y^{20} + 55y^{19} + \dots - 892556y + 418609$
c_6, c_9	$y^{20} + 33y^{19} + \dots - 120y + 16$
c_7, c_{11}	$y^{20} - 15y^{19} + \dots - 22y + 1$
c_8	$y^{20} - 3y^{19} + \dots - 6y + 1$
c_{10}	$y^{20} - 15y^{19} + \dots + 50y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.562478 + 0.702926I$ $a = -0.164935 + 1.014010I$ $b = -0.932716 - 0.491902I$	$0.10443 - 4.15417I$	$5.96079 + 7.41844I$
$u = -0.562478 - 0.702926I$ $a = -0.164935 - 1.014010I$ $b = -0.932716 + 0.491902I$	$0.10443 + 4.15417I$	$5.96079 - 7.41844I$
$u = -0.345261 + 0.774594I$ $a = -0.178688 + 1.067020I$ $b = 0.262517 + 0.119217I$	$-1.78458 - 2.08707I$	$-0.67504 + 3.91538I$
$u = -0.345261 - 0.774594I$ $a = -0.178688 - 1.067020I$ $b = 0.262517 - 0.119217I$	$-1.78458 + 2.08707I$	$-0.67504 - 3.91538I$
$u = -0.546407 + 0.261165I$ $a = -0.016518 - 0.458675I$ $b = -0.503419 + 0.405661I$	$1.204440 - 0.232928I$	$9.01931 + 0.79005I$
$u = -0.546407 - 0.261165I$ $a = -0.016518 + 0.458675I$ $b = -0.503419 - 0.405661I$	$1.204440 + 0.232928I$	$9.01931 - 0.79005I$
$u = 0.55309 + 1.41617I$ $a = 0.152667 - 0.289034I$ $b = -1.369770 - 0.179262I$	$-7.00299 - 3.90150I$	$-2.54860 + 3.27736I$
$u = 0.55309 - 1.41617I$ $a = 0.152667 + 0.289034I$ $b = -1.369770 + 0.179262I$	$-7.00299 + 3.90150I$	$-2.54860 - 3.27736I$
$u = 0.368558 + 0.047969I$ $a = -1.78216 + 1.81771I$ $b = 1.053190 - 0.370537I$	$-1.82190 + 1.34830I$	$-1.59816 - 0.61194I$
$u = 0.368558 - 0.047969I$ $a = -1.78216 - 1.81771I$ $b = 1.053190 + 0.370537I$	$-1.82190 - 1.34830I$	$-1.59816 + 0.61194I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.140514 + 0.165365I$ $a = -1.96129 + 4.14993I$ $b = 0.715874 + 0.509667I$	$-1.42072 - 2.15124I$	$1.64791 + 3.40317I$
$u = -0.140514 - 0.165365I$ $a = -1.96129 - 4.14993I$ $b = 0.715874 - 0.509667I$	$-1.42072 + 2.15124I$	$1.64791 - 3.40317I$
$u = -0.93727 + 1.53815I$ $a = -0.097983 - 0.641269I$ $b = 1.281060 + 0.067311I$	$-5.23226 - 2.45917I$	$-1.69714 + 1.89268I$
$u = -0.93727 - 1.53815I$ $a = -0.097983 + 0.641269I$ $b = 1.281060 - 0.067311I$	$-5.23226 + 2.45917I$	$-1.69714 - 1.89268I$
$u = -0.00083 + 2.05851I$ $a = -0.027063 + 1.246070I$ $b = 0.076044 - 1.204780I$	$-13.59470 - 3.72129I$	$0.72655 + 1.99965I$
$u = -0.00083 - 2.05851I$ $a = -0.027063 - 1.246070I$ $b = 0.076044 + 1.204780I$	$-13.59470 + 3.72129I$	$0.72655 - 1.99965I$
$u = 0.48389 + 2.08874I$ $a = 0.342044 - 1.052760I$ $b = -1.48289 + 0.54439I$	$-18.5347 + 2.5424I$	$-1.82827 + 0.I$
$u = 0.48389 - 2.08874I$ $a = 0.342044 + 1.052760I$ $b = -1.48289 - 0.54439I$	$-18.5347 - 2.5424I$	$-1.82827 + 0.I$
$u = -0.37279 + 2.18713I$ $a = -0.266075 - 1.115660I$ $b = 1.40011 + 0.62778I$	$-17.7144 - 10.2068I$	$0. + 4.81283I$
$u = -0.37279 - 2.18713I$ $a = -0.266075 + 1.115660I$ $b = 1.40011 - 0.62778I$	$-17.7144 + 10.2068I$	$0. - 4.81283I$

$$\text{II. } I_2^u = \langle -au + b - u - 1, a^2 - 2au - u, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a \\ au + u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} au + a + u + 2 \\ -u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u + 1 \\ au + a + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} au + a + 1 \\ -u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -au - a - u - 2 \\ -a + 3u + 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} au + a + 1 \\ -au - 2u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} au + a + 1 \\ -au - 2u - 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $8u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u^2 + u + 1)^2$
c_3	$u^4 - 2u^3 + 5u^2 - 4u + 1$
c_4	$u^4 + 4u^3 + 5u^2 + 2u + 1$
c_5, c_{10}	$(u^2 - u + 1)^2$
c_6, c_9	$(u^2 + 1)^2$
c_7, c_8, c_{11}	$u^4 - u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5 c_{10}	$(y^2 + y + 1)^2$
c_3	$y^4 + 6y^3 + 11y^2 - 6y + 1$
c_4	$y^4 - 6y^3 + 11y^2 + 6y + 1$
c_6, c_9	$(y + 1)^4$
c_7, c_8, c_{11}	$(y^2 - y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = -0.500000 - 0.133975I$	$-1.64493 - 4.05977I$	$0. + 6.92820I$
$b = 0.866025 + 0.500000I$		
$u = -0.500000 + 0.866025I$		
$a = -0.500000 + 1.86603I$	$-1.64493 - 4.05977I$	$0. + 6.92820I$
$b = -0.866025 - 0.500000I$		
$u = -0.500000 - 0.866025I$		
$a = -0.500000 + 0.133975I$	$-1.64493 + 4.05977I$	$0. - 6.92820I$
$b = 0.866025 - 0.500000I$		
$u = -0.500000 - 0.866025I$		
$a = -0.500000 - 1.86603I$	$-1.64493 + 4.05977I$	$0. - 6.92820I$
$b = -0.866025 + 0.500000I$		

$$\text{III. } I_3^u = \langle au + b + a - u - 1, a^2 - 2a + 2, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a \\ -au - a + u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} au + a - 2u - 1 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u + 1 \\ -au + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} au + a - u - 1 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} au - 2u - 1 \\ au + a - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} au + a - u - 1 \\ -au + 2u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} au + a - u - 1 \\ -au + 2u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u^2 + u + 1)^2$
c_3, c_4	$u^4 - 2u^3 + 2u^2 + 2u + 1$
c_5, c_{10}	$(u^2 - u + 1)^2$
c_6, c_9	$(u^2 + 1)^2$
c_7, c_8, c_{11}	$u^4 - u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5 c_{10}	$(y^2 + y + 1)^2$
c_3, c_4	$y^4 + 14y^2 + 1$
c_6, c_9	$(y + 1)^4$
c_7, c_8, c_{11}	$(y^2 - y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$	-1.64493	0
$a = 1.00000 + 1.00000I$		
$b = 0.866025 - 0.500000I$		
$u = -0.500000 + 0.866025I$	-1.64493	0
$a = 1.00000 - 1.00000I$		
$b = -0.866025 + 0.500000I$		
$u = -0.500000 - 0.866025I$	-1.64493	0
$a = 1.00000 + 1.00000I$		
$b = -0.866025 - 0.500000I$		
$u = -0.500000 - 0.866025I$	-1.64493	0
$a = 1.00000 - 1.00000I$		
$b = 0.866025 + 0.500000I$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u^2 + u + 1)^4)(u^{20} - 3u^{19} + \dots - 6u + 1)$
c_2	$((u^2 + u + 1)^4)(u^{20} + 33u^{19} + \dots - 6u + 1)$
c_3	$(u^4 - 2u^3 + 2u^2 + 2u + 1)(u^4 - 2u^3 + 5u^2 - 4u + 1)$ $\cdot (u^{20} + u^{19} + \dots + 1264u + 517)$
c_4	$(u^4 - 2u^3 + 2u^2 + 2u + 1)(u^4 + 4u^3 + 5u^2 + 2u + 1)$ $\cdot (u^{20} + u^{19} + \dots + 1876u + 647)$
c_5	$((u^2 - u + 1)^4)(u^{20} - 3u^{19} + \dots - 6u + 1)$
c_6, c_9	$((u^2 + 1)^4)(u^{20} + u^{19} + \dots + 12u + 4)$
c_7, c_{11}	$((u^4 - u^2 + 1)^2)(u^{20} + u^{19} + \dots + 6u + 1)$
c_8	$((u^4 - u^2 + 1)^2)(u^{20} + u^{19} + \dots + 4u + 1)$
c_{10}	$((u^2 - u + 1)^4)(u^{20} + 15u^{19} + \dots + 22u + 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_5	$((y^2 + y + 1)^4)(y^{20} + 33y^{19} + \dots - 6y + 1)$
c_2	$((y^2 + y + 1)^4)(y^{20} - 87y^{19} + \dots + 770y + 1)$
c_3	$(y^4 + 14y^2 + 1)(y^4 + 6y^3 + 11y^2 - 6y + 1)$ $\cdot (y^{20} + 27y^{19} + \dots + 842544y + 267289)$
c_4	$(y^4 + 14y^2 + 1)(y^4 - 6y^3 + 11y^2 + 6y + 1)$ $\cdot (y^{20} + 55y^{19} + \dots - 892556y + 418609)$
c_6, c_9	$((y + 1)^8)(y^{20} + 33y^{19} + \dots - 120y + 16)$
c_7, c_{11}	$((y^2 - y + 1)^4)(y^{20} - 15y^{19} + \dots - 22y + 1)$
c_8	$((y^2 - y + 1)^4)(y^{20} - 3y^{19} + \dots - 6y + 1)$
c_{10}	$((y^2 + y + 1)^4)(y^{20} - 15y^{19} + \dots + 50y + 1)$