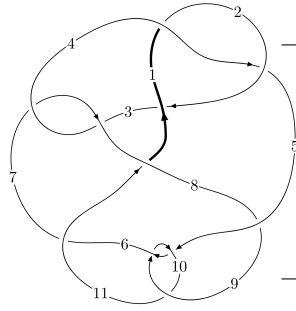
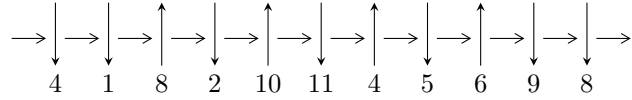


11n₅₂ (K11n₅₂)

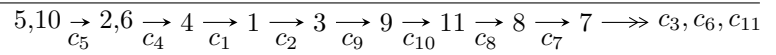


A knot diagram¹

Linearized knot diagram



Solving Sequence



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -u^{32} - u^{31} + \dots + b + u, -u^{32} - u^{31} + \dots + a - 1, u^{34} + 2u^{33} + \dots - 2u - 1 \rangle$$

$$I_2^u = \langle b + 1, -u^3 + u^2 + a - u + 2, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 39 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{32} - u^{31} + \dots + b + u, -u^{32} - u^{31} + \dots + a - 1, u^{34} + 2u^{33} + \dots - 2u - 1 \rangle \quad \mathbf{I.}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{32} + u^{31} + \dots - 5u^3 + 1 \\ u^{32} + u^{31} + \dots - u^2 - u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u^{32} - 2u^{31} + \dots + u^2 + u \\ -u^{32} - u^{31} + \dots + u^2 + 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{11} - 2u^9 - 2u^7 - u^3 \\ -u^{11} - 3u^9 - 4u^7 - u^5 + u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 4u^{32} + 4u^{31} + \dots - 3u - 1 \\ 2u^{32} + u^{31} + \dots - u^2 - 3u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^8 + 2u^6 + 2u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^8 + 2u^6 + 2u^4 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -4u^{33} - 11u^{32} - 46u^{31} - 97u^{30} - 238u^{29} - 421u^{28} - 758u^{27} - \\ &1154u^{26} - 1651u^{25} - 2191u^{24} - 2586u^{23} - 2978u^{22} - 2933u^{21} - 2856u^{20} - 2304u^{19} - \\ &1728u^{18} - 973u^{17} - 263u^{16} + 258u^{15} + 646u^{14} + 764u^{13} + 710u^{12} + 560u^{11} + 314u^{10} + \\ &160u^9 + 16u^8 - 52u^7 - 64u^6 - 51u^5 - 4u^4 + 16u^3 + 18u^2 + 15u + 3 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$u^{34} - 6u^{33} + \dots + 4u - 1$
c_2	$u^{34} + 10u^{33} + \dots + 2u^2 + 1$
c_3, c_7	$u^{34} - u^{33} + \dots + 32u + 32$
c_5, c_9	$u^{34} - 2u^{33} + \dots + 2u - 1$
c_6, c_8	$u^{34} + 2u^{33} + \dots - 58u - 17$
c_{10}	$u^{34} + 18u^{33} + \dots + 2u + 1$
c_{11}	$u^{34} - 2u^{33} + \dots + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$y^{34} - 10y^{33} + \dots + 2y^2 + 1$
c_2	$y^{34} + 34y^{33} + \dots + 4y + 1$
c_3, c_7	$y^{34} - 33y^{33} + \dots - 11776y + 1024$
c_5, c_9	$y^{34} + 18y^{33} + \dots + 2y + 1$
c_6, c_8	$y^{34} - 22y^{33} + \dots + 682y + 289$
c_{10}	$y^{34} - 2y^{33} + \dots - 18y + 1$
c_{11}	$y^{34} + 38y^{33} + \dots + 2y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.392064 + 0.911772I$	$-0.33123 - 1.99737I$	$-1.04171 + 3.94659I$
$a = -1.220400 + 0.149546I$		
$b = -0.151137 - 0.378084I$		
$u = -0.392064 - 0.911772I$	$-0.33123 + 1.99737I$	$-1.04171 - 3.94659I$
$a = -1.220400 - 0.149546I$		
$b = -0.151137 + 0.378084I$		
$u = 0.643857 + 0.740919I$	$7.32303 - 1.01150I$	$0.462803 - 0.538404I$
$a = 0.444510 + 0.058747I$		
$b = -0.919309 - 0.963610I$		
$u = 0.643857 - 0.740919I$	$7.32303 + 1.01150I$	$0.462803 + 0.538404I$
$a = 0.444510 - 0.058747I$		
$b = -0.919309 + 0.963610I$		
$u = 0.631061 + 0.814143I$	$7.11131 + 5.93371I$	$-0.19300 - 5.69756I$
$a = -1.09866 - 1.38992I$		
$b = -0.986984 + 0.934448I$		
$u = 0.631061 - 0.814143I$	$7.11131 - 5.93371I$	$-0.19300 + 5.69756I$
$a = -1.09866 + 1.38992I$		
$b = -0.986984 - 0.934448I$		
$u = -0.820098 + 0.217356I$	$3.98565 + 7.54944I$	$-1.73478 - 4.55602I$
$a = -1.021230 - 0.783883I$		
$b = -1.088070 + 0.833628I$		
$u = -0.820098 - 0.217356I$	$3.98565 - 7.54944I$	$-1.73478 + 4.55602I$
$a = -1.021230 + 0.783883I$		
$b = -1.088070 - 0.833628I$		
$u = -0.775445 + 0.276843I$	$5.05465 + 0.88184I$	$-0.0341976 + 0.1167760I$
$a = -0.000113 + 0.147223I$		
$b = -0.749373 - 0.980750I$		
$u = -0.775445 - 0.276843I$	$5.05465 - 0.88184I$	$-0.0341976 - 0.1167760I$
$a = -0.000113 - 0.147223I$		
$b = -0.749373 + 0.980750I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.255241 + 1.154760I$ $a = -1.63194 - 0.61364I$ $b = -0.719802 - 0.838712I$	$0.59034 - 2.20193I$	$-5.39762 + 2.89255I$
$u = -0.255241 - 1.154760I$ $a = -1.63194 + 0.61364I$ $b = -0.719802 + 0.838712I$	$0.59034 + 2.20193I$	$-5.39762 - 2.89255I$
$u = 0.401589 + 1.121620I$ $a = 0.740490 + 0.229483I$ $b = 0.867707 + 0.523486I$	$-4.35229 + 1.60461I$	$-8.26502 - 1.09622I$
$u = 0.401589 - 1.121620I$ $a = 0.740490 - 0.229483I$ $b = 0.867707 - 0.523486I$	$-4.35229 - 1.60461I$	$-8.26502 + 1.09622I$
$u = 0.803313$ $a = -1.12207$ $b = -0.598522$	-3.18504	0.914630
$u = -0.421626 + 0.667896I$ $a = -0.457995 - 0.776702I$ $b = 0.257061 + 0.435953I$	$0.37642 - 1.53920I$	$0.52977 + 5.14051I$
$u = -0.421626 - 0.667896I$ $a = -0.457995 + 0.776702I$ $b = 0.257061 - 0.435953I$	$0.37642 + 1.53920I$	$0.52977 - 5.14051I$
$u = -0.449017 + 1.136970I$ $a = 2.83048 - 1.35162I$ $b = 1.307530 + 0.065436I$	$-5.63834 - 3.94702I$	$-6.39479 + 3.36113I$
$u = -0.449017 - 1.136970I$ $a = 2.83048 + 1.35162I$ $b = 1.307530 - 0.065436I$	$-5.63834 + 3.94702I$	$-6.39479 - 3.36113I$
$u = 0.490186 + 1.136270I$ $a = 1.31533 + 1.01208I$ $b = 0.706452 - 0.661902I$	$-3.70744 + 6.19607I$	$-6.22304 - 6.67245I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.490186 - 1.136270I$		
$a = 1.31533 - 1.01208I$	$-3.70744 - 6.19607I$	$-6.22304 + 6.67245I$
$b = 0.706452 + 0.661902I$		
$u = -0.316626 + 1.211300I$		
$a = -1.82873 + 0.86114I$	$-0.44863 + 3.88868I$	$-6.63703 - 2.26154I$
$b = -1.058350 + 0.773720I$		
$u = -0.316626 - 1.211300I$		
$a = -1.82873 - 0.86114I$	$-0.44863 - 3.88868I$	$-6.63703 + 2.26154I$
$b = -1.058350 - 0.773720I$		
$u = -0.548880 + 1.145350I$		
$a = 0.412467 + 1.244140I$	$2.49823 - 5.83735I$	$-3.10039 + 3.72465I$
$b = -0.692953 + 1.024120I$		
$u = -0.548880 - 1.145350I$		
$a = 0.412467 - 1.244140I$	$2.49823 + 5.83735I$	$-3.10039 - 3.72465I$
$b = -0.692953 - 1.024120I$		
$u = 0.456179 + 1.214870I$		
$a = -1.73132 - 0.47368I$	$-6.76337 + 4.50518I$	$-1.87945 - 4.07859I$
$b = -0.649218 + 0.049959I$		
$u = 0.456179 - 1.214870I$		
$a = -1.73132 + 0.47368I$	$-6.76337 - 4.50518I$	$-1.87945 + 4.07859I$
$b = -0.649218 - 0.049959I$		
$u = -0.544284 + 1.179770I$		
$a = -2.56097 + 1.10413I$	$1.13195 - 12.58770I$	$-4.92167 + 7.87699I$
$b = -1.127080 - 0.824983I$		
$u = -0.544284 - 1.179770I$		
$a = -2.56097 - 1.10413I$	$1.13195 + 12.58770I$	$-4.92167 - 7.87699I$
$b = -1.127080 + 0.824983I$		
$u = 0.157297 + 0.676103I$		
$a = 1.45465 + 1.84751I$	$-2.09473 + 0.78471I$	$-6.87662 + 2.65408I$
$b = 1.034700 - 0.173788I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.157297 - 0.676103I$		
$a = 1.45465 - 1.84751I$	$-2.09473 - 0.78471I$	$-6.87662 - 2.65408I$
$b = 1.034700 + 0.173788I$		
$u = 0.637571 + 0.171045I$		
$a = -0.049058 - 1.073020I$	$-0.99883 - 1.83078I$	$-2.95289 + 3.76618I$
$b = 0.658221 + 0.529258I$		
$u = 0.637571 - 0.171045I$		
$a = -0.049058 + 1.073020I$	$-0.99883 + 1.83078I$	$-2.95289 - 3.76618I$
$b = 0.658221 - 0.529258I$		
$u = -0.592232$		
$a = 1.92705$	-2.64346	-1.59530
$b = 1.21971$		

$$\text{II. } I_2^u = \langle b + 1, -u^3 + u^2 + a - u + 2, u^5 - u^4 + 2u^3 - u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 - u^2 + u - 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 - u^2 + u - 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 - u^2 + u - 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 \\ u^4 - u^3 + u^2 + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-2u^4 + 7u^3 - 8u^2 + 6u - 12$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$(u - 1)^5$
c_2, c_4	$(u + 1)^5$
c_3, c_7	u^5
c_5	$u^5 - u^4 + 2u^3 - u^2 + u - 1$
c_6	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
c_8, c_{11}	$u^5 - u^4 - 2u^3 + u^2 + u + 1$
c_9	$u^5 + u^4 + 2u^3 + u^2 + u + 1$
c_{10}	$u^5 + 3u^4 + 4u^3 + u^2 - u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^5$
c_3, c_7	y^5
c_5, c_9	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$
c_6, c_8, c_{11}	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$
c_{10}	$y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.339110 + 0.822375I$ $a = -1.12878 + 1.10766I$ $b = -1.00000$	$-1.97403 - 1.53058I$	$-5.00899 + 6.23673I$
$u = -0.339110 - 0.822375I$ $a = -1.12878 - 1.10766I$ $b = -1.00000$	$-1.97403 + 1.53058I$	$-5.00899 - 6.23673I$
$u = 0.766826$ $a = -1.37029$ $b = -1.00000$	-4.04602	-9.63840
$u = 0.455697 + 1.200150I$ $a = -2.18608 - 0.87465I$ $b = -1.00000$	$-7.51750 + 4.40083I$	$-13.17182 - 3.02310I$
$u = 0.455697 - 1.200150I$ $a = -2.18608 + 0.87465I$ $b = -1.00000$	$-7.51750 - 4.40083I$	$-13.17182 + 3.02310I$

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^5)(u^{34} - 6u^{33} + \dots + 4u - 1)$
c_2	$((u + 1)^5)(u^{34} + 10u^{33} + \dots + 2u^2 + 1)$
c_3, c_7	$u^5(u^{34} - u^{33} + \dots + 32u + 32)$
c_4	$((u + 1)^5)(u^{34} - 6u^{33} + \dots + 4u - 1)$
c_5	$(u^5 - u^4 + 2u^3 - u^2 + u - 1)(u^{34} - 2u^{33} + \dots + 2u - 1)$
c_6	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)(u^{34} + 2u^{33} + \dots - 58u - 17)$
c_8	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)(u^{34} + 2u^{33} + \dots - 58u - 17)$
c_9	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)(u^{34} - 2u^{33} + \dots + 2u - 1)$
c_{10}	$(u^5 + 3u^4 + 4u^3 + u^2 - u - 1)(u^{34} + 18u^{33} + \dots + 2u + 1)$
c_{11}	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)(u^{34} - 2u^{33} + \dots + 2u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_4	$((y - 1)^5)(y^{34} - 10y^{33} + \dots + 2y^2 + 1)$
c_2	$((y - 1)^5)(y^{34} + 34y^{33} + \dots + 4y + 1)$
c_3, c_7	$y^5(y^{34} - 33y^{33} + \dots - 11776y + 1024)$
c_5, c_9	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)(y^{34} + 18y^{33} + \dots + 2y + 1)$
c_6, c_8	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)(y^{34} - 22y^{33} + \dots + 682y + 289)$
c_{10}	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)(y^{34} - 2y^{33} + \dots - 18y + 1)$
c_{11}	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)(y^{34} + 38y^{33} + \dots + 2y + 1)$