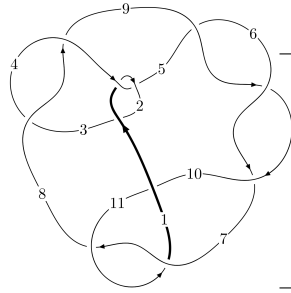
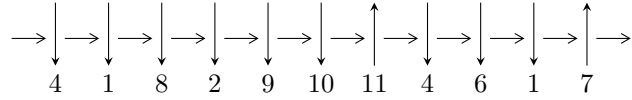


11n₅₇ (K11n₅₇)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$1,7 \xrightarrow{c_{11}} 11 \xrightarrow{c_7} 4,8 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_4} 5 \xrightarrow{c_{10}} 10 \xrightarrow{c_6} 6 \xrightarrow{c_9} 9 \longrightarrow c_1, c_5, c_8$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^5 - u^4 + 2u^3 - u^2 + b + u, u^5 - u^4 + 3u^3 - 2u^2 + a + 2u - 1, u^8 - 2u^7 + 5u^6 - 6u^5 + 7u^4 - 6u^3 + 2u^2 - 1 \rangle$$

$$I_2^u = \langle b - 1, u^3 + u^2 + a + u, u^5 + u^4 + 2u^3 + u^2 + u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 13 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle u^5 - u^4 + 2u^3 - u^2 + b + u, u^5 - u^4 + 3u^3 - 2u^2 + a + 2u - 1, u^8 - 2u^7 + \dots - u - 1 \rangle$$

I. $I_1^u =$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^5 + u^4 - 3u^3 + 2u^2 - 2u + 1 \\ -u^5 + u^4 - 2u^3 + u^2 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^6 + u^5 - 2u^4 + 2u^3 + 2 \\ u^6 + 3u^4 - u^3 + 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 + u^4 + u^3 + 2u^2 + 2 \\ u^6 + 3u^4 - u^3 + 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 3u^5 + u^4 + 6u^3 + u^2 + 3u + 2 \\ -u^7 + 4u^6 - 3u^5 + 9u^4 - 2u^3 + 4u^2 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^5 + 2u^3 + u \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^7 + 2u^6 - 6u^5 + 4u^4 - 6u^3 + 2u^2 - u \\ -2u^7 + 3u^6 - 6u^5 + 5u^4 - 6u^3 + 2u^2 - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^7 + 2u^6 - 6u^5 + 4u^4 - 6u^3 + 2u^2 - u \\ -2u^7 + 3u^6 - 6u^5 + 5u^4 - 6u^3 + 2u^2 - u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $4u^7 - 9u^6 + 18u^5 - 21u^4 + 18u^3 - 14u^2 - 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$u^8 - 6u^7 + 7u^6 + 9u^5 + 6u^4 - 40u^3 - 13u^2 + 5u - 1$
c_2	$u^8 + 22u^7 + 169u^6 + 503u^5 + 632u^4 + 1860u^3 + 557u^2 - u + 1$
c_3, c_8	$u^8 - 7u^7 - 4u^6 + 119u^5 - 212u^4 - 16u^3 + 120u^2 + 64u + 32$
c_5, c_6, c_9	$u^8 + 2u^7 - 7u^6 - 12u^5 + 7u^4 + 2u^3 - 2u^2 - 3u - 1$
c_7, c_{11}	$u^8 - 2u^7 + 5u^6 - 6u^5 + 7u^4 - 6u^3 + 2u^2 - u - 1$
c_{10}	$u^8 + 6u^7 + 15u^6 + 14u^5 - 9u^4 - 30u^3 - 22u^2 - 5u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$y^8 - 22y^7 + 169y^6 - 503y^5 + 632y^4 - 1860y^3 + 557y^2 + y + 1$
c_2	$y^8 - 146y^7 + \dots + 1113y + 1$
c_3, c_8	$y^8 - 57y^7 + \dots + 3584y + 1024$
c_5, c_6, c_9	$y^8 - 18y^7 + 111y^6 - 254y^5 + 135y^4 - 90y^3 + 2y^2 - 5y + 1$
c_7, c_{11}	$y^8 + 6y^7 + 15y^6 + 14y^5 - 9y^4 - 30y^3 - 22y^2 - 5y + 1$
c_{10}	$y^8 - 6y^7 + 39y^6 - 150y^5 + 323y^4 - 334y^3 + 166y^2 - 69y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.09831$ $a = -2.90176$ $b = -2.68486$	16.8590	-9.91680
$u = 0.271970 + 0.836396I$ $a = 0.514998 - 0.132997I$ $b = -0.138100 - 0.151060I$	$-0.50482 + 1.32248I$	$-5.16164 - 4.61817I$
$u = 0.271970 - 0.836396I$ $a = 0.514998 + 0.132997I$ $b = -0.138100 + 0.151060I$	$-0.50482 - 1.32248I$	$-5.16164 + 4.61817I$
$u = -0.198501 + 1.220550I$ $a = -0.186478 + 1.015590I$ $b = 0.944682 + 1.046670I$	$-4.38598 - 2.12062I$	$-13.41968 + 2.09452I$
$u = -0.198501 - 1.220550I$ $a = -0.186478 - 1.015590I$ $b = 0.944682 - 1.046670I$	$-4.38598 + 2.12062I$	$-13.41968 - 2.09452I$
$u = 0.55241 + 1.37610I$ $a = -0.92476 + 1.87326I$ $b = -2.75351 + 0.38295I$	$12.57270 + 5.86054I$	$-12.50168 - 2.57970I$
$u = 0.55241 - 1.37610I$ $a = -0.92476 - 1.87326I$ $b = -2.75351 - 0.38295I$	$12.57270 - 5.86054I$	$-12.50168 + 2.57970I$
$u = -0.350076$ $a = 2.09424$ $b = 0.578712$	-0.969109	-9.91720

$$\text{II. } I_2^u = \langle b - 1, u^3 + u^2 + a + u, u^5 + u^4 + 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - u^2 - u \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 - u^2 - u \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 - u^2 - u + 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^4 - u^2 - 1 \\ -u^4 - u^3 - u^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $2u^4 - u^3 - 2u - 12$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$(u - 1)^5$
c_2, c_4	$(u + 1)^5$
c_3, c_8	u^5
c_5, c_6	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
c_7	$u^5 - u^4 + 2u^3 - u^2 + u - 1$
c_9	$u^5 - u^4 - 2u^3 + u^2 + u + 1$
c_{10}	$u^5 - 3u^4 + 4u^3 - u^2 - u + 1$
c_{11}	$u^5 + u^4 + 2u^3 + u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^5$
c_3, c_8	y^5
c_5, c_6, c_9	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$
c_7, c_{11}	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$
c_{10}	$y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.339110 + 0.822375I$ $a = 0.871221 - 1.107660I$ $b = 1.00000$	$-1.97403 + 1.53058I$	$-12.02124 - 2.62456I$
$u = 0.339110 - 0.822375I$ $a = 0.871221 + 1.107660I$ $b = 1.00000$	$-1.97403 - 1.53058I$	$-12.02124 + 2.62456I$
$u = -0.766826$ $a = 0.629714$ $b = 1.00000$	-4.04602	-9.32390
$u = -0.455697 + 1.200150I$ $a = -0.186078 + 0.874646I$ $b = 1.00000$	$-7.51750 - 4.40083I$	$-12.31681 + 3.97407I$
$u = -0.455697 - 1.200150I$ $a = -0.186078 - 0.874646I$ $b = 1.00000$	$-7.51750 + 4.40083I$	$-12.31681 - 3.97407I$

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u-1)^5(u^8 - 6u^7 + 7u^6 + 9u^5 + 6u^4 - 40u^3 - 13u^2 + 5u - 1)$
c_2	$(u+1)^5 \cdot (u^8 + 22u^7 + 169u^6 + 503u^5 + 632u^4 + 1860u^3 + 557u^2 - u + 1)$
c_3, c_8	$u^5(u^8 - 7u^7 - 4u^6 + 119u^5 - 212u^4 - 16u^3 + 120u^2 + 64u + 32)$
c_4	$(u+1)^5(u^8 - 6u^7 + 7u^6 + 9u^5 + 6u^4 - 40u^3 - 13u^2 + 5u - 1)$
c_5, c_6	$(u^5 + u^4 - 2u^3 - u^2 + u - 1) \cdot (u^8 + 2u^7 - 7u^6 - 12u^5 + 7u^4 + 2u^3 - 2u^2 - 3u - 1)$
c_7	$(u^5 - u^4 + 2u^3 - u^2 + u - 1) \cdot (u^8 - 2u^7 + 5u^6 - 6u^5 + 7u^4 - 6u^3 + 2u^2 - u - 1)$
c_9	$(u^5 - u^4 - 2u^3 + u^2 + u + 1) \cdot (u^8 + 2u^7 - 7u^6 - 12u^5 + 7u^4 + 2u^3 - 2u^2 - 3u - 1)$
c_{10}	$(u^5 - 3u^4 + 4u^3 - u^2 - u + 1) \cdot (u^8 + 6u^7 + 15u^6 + 14u^5 - 9u^4 - 30u^3 - 22u^2 - 5u + 1)$
c_{11}	$(u^5 + u^4 + 2u^3 + u^2 + u + 1) \cdot (u^8 - 2u^7 + 5u^6 - 6u^5 + 7u^4 - 6u^3 + 2u^2 - u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_4	$(y - 1)^5$ $\cdot (y^8 - 22y^7 + 169y^6 - 503y^5 + 632y^4 - 1860y^3 + 557y^2 + y + 1)$
c_2	$((y - 1)^5)(y^8 - 146y^7 + \dots + 1113y + 1)$
c_3, c_8	$y^5(y^8 - 57y^7 + \dots + 3584y + 1024)$
c_5, c_6, c_9	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)$ $\cdot (y^8 - 18y^7 + 111y^6 - 254y^5 + 135y^4 - 90y^3 + 2y^2 - 5y + 1)$
c_7, c_{11}	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)$ $\cdot (y^8 + 6y^7 + 15y^6 + 14y^5 - 9y^4 - 30y^3 - 22y^2 - 5y + 1)$
c_{10}	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)$ $\cdot (y^8 - 6y^7 + 39y^6 - 150y^5 + 323y^4 - 334y^3 + 166y^2 - 69y + 1)$