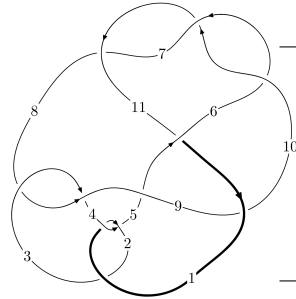
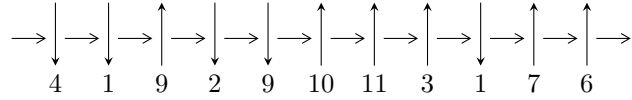


11n₅₈ (K11n₅₈)

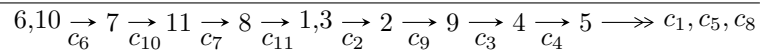


A knot diagram¹

Linearized knot diagram



Solving Sequence



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -u^{21} - u^{20} + \dots + 5u^2 + b, -u^{14} + 7u^{12} - 18u^{10} + 19u^8 - 6u^6 + 2u^4 + 2u^3 - 4u^2 + a - 4u - 1, u^{22} + 2u^{21} + \dots - 4u^2 - 1 \rangle$$

$$I_2^u = \langle b + 1, u^3 + a - 2u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 27 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -u^{21} - u^{20} + \dots + 5u^2 + b, -u^{14} + 7u^{12} + \dots + a - 1, u^{22} + 2u^{21} + \dots - 4u^2 - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{14} - 7u^{12} + 18u^{10} - 19u^8 + 6u^6 - 2u^4 - 2u^3 + 4u^2 + 4u + 1 \\ u^{21} + u^{20} + \dots - 9u^3 - 5u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{21} + u^{20} + \dots + 5u + 1 \\ 3u^{21} + 2u^{20} + \dots + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^7 - 4u^5 + 4u^3 \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u^{21} - 2u^{20} + \dots + 4u + 2 \\ u^{21} + u^{20} + \dots - 5u^2 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^{14} - 7u^{12} + 18u^{10} - 19u^8 + 4u^6 + 4u^4 - 1 \\ u^{14} - 6u^{12} + 13u^{10} - 10u^8 - 2u^6 + 4u^4 + u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^{14} - 7u^{12} + 18u^{10} - 19u^8 + 4u^6 + 4u^4 - 1 \\ u^{14} - 6u^{12} + 13u^{10} - 10u^8 - 2u^6 + 4u^4 + u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -2u^{21} - 4u^{20} + 20u^{19} + 37u^{18} - 87u^{17} - 136u^{16} + 219u^{15} + 241u^{14} - 359u^{13} - 186u^{12} + 398u^{11} + 17u^{10} - 277u^9 + 14u^8 + 98u^7 + 38u^6 - 34u^5 - 18u^4 + 36u^3 + 13u^2 - u - 2$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|---|
| c_1, c_4 | $u^{22} - 6u^{21} + \dots + 6u - 1$ |
| c_2 | $u^{22} + 2u^{21} + \dots + 2u + 1$ |
| c_3, c_8 | $u^{22} - u^{21} + \dots - 64u + 32$ |
| c_5 | $u^{22} + 2u^{21} + \dots + 2996u - 1960$ |
| c_6, c_7, c_{10} | $u^{22} - 2u^{21} + \dots - 4u^2 - 1$ |
| c_9 | $u^{22} - 2u^{21} + \dots - 2u + 1$ |
| c_{11} | $u^{22} + 6u^{21} + \dots - 64u - 17$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------|---|
| c_1, c_4 | $y^{22} - 2y^{21} + \dots - 2y + 1$ |
| c_2 | $y^{22} + 42y^{21} + \dots - 62y + 1$ |
| c_3, c_8 | $y^{22} - 33y^{21} + \dots - 7680y + 1024$ |
| c_5 | $y^{22} + 66y^{21} + \dots + 61827024y + 3841600$ |
| c_6, c_7, c_{10} | $y^{22} - 22y^{21} + \dots + 8y + 1$ |
| c_9 | $y^{22} + 30y^{21} + \dots + 8y + 1$ |
| c_{11} | $y^{22} - 14y^{21} + \dots - 2056y + 289$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = 0.547451 + 0.687554I$ $a = -1.64917 + 1.79616I$ $b = -0.18168 + 2.30378I$ | $10.04630 - 1.61926I$ | $3.79117 - 0.60262I$ |
| $u = 0.547451 - 0.687554I$ $a = -1.64917 - 1.79616I$ $b = -0.18168 - 2.30378I$ | $10.04630 + 1.61926I$ | $3.79117 + 0.60262I$ |
| $u = 0.477782 + 0.730631I$ $a = 1.68752 - 2.10270I$ $b = 0.07337 - 2.34864I$ | $9.80847 + 6.35147I$ | $3.22096 - 4.88727I$ |
| $u = 0.477782 - 0.730631I$ $a = 1.68752 + 2.10270I$ $b = 0.07337 + 2.34864I$ | $9.80847 - 6.35147I$ | $3.22096 + 4.88727I$ |
| $u = -1.15891$ $a = -0.585194$ $b = 0.132093$ | 1.97038 | 6.11980 |
| $u = -0.253735 + 0.636077I$ $a = -0.333427 + 0.841858I$ $b = -0.032077 + 0.372929I$ | $0.10442 - 2.33425I$ | $2.92732 + 5.10863I$ |
| $u = -0.253735 - 0.636077I$ $a = -0.333427 - 0.841858I$ $b = -0.032077 - 0.372929I$ | $0.10442 + 2.33425I$ | $2.92732 - 5.10863I$ |
| $u = 1.33846$ $a = 1.06516$ $b = 1.56525$ | 1.80329 | 6.37870 |
| $u = -1.374360 + 0.085773I$ $a = -0.046048 - 1.048570I$ $b = 0.632067 + 0.872611I$ | $3.07940 - 2.15283I$ | $3.96233 + 2.53077I$ |
| $u = -1.374360 - 0.085773I$ $a = -0.046048 + 1.048570I$ $b = 0.632067 - 0.872611I$ | $3.07940 + 2.15283I$ | $3.96233 - 2.53077I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.458175 + 0.412746I$ $a = -1.044590 - 0.139124I$ $b = -0.311064 - 0.023201I$ | $1.10436 - 0.93215I$ | $5.59687 + 3.71705I$ |
| $u = -0.458175 - 0.412746I$ $a = -1.044590 + 0.139124I$ $b = -0.311064 + 0.023201I$ | $1.10436 + 0.93215I$ | $5.59687 - 3.71705I$ |
| $u = 1.384260 + 0.250179I$ $a = 0.084137 - 0.456690I$ $b = 0.043050 - 0.643455I$ | $5.30289 + 5.58097I$ | $6.98899 - 5.83204I$ |
| $u = 1.384260 - 0.250179I$ $a = 0.084137 + 0.456690I$ $b = 0.043050 + 0.643455I$ | $5.30289 - 5.58097I$ | $6.98899 + 5.83204I$ |
| $u = 1.46039 + 0.14631I$ $a = -0.589431 - 0.029298I$ $b = -0.810187 + 0.008550I$ | $7.28227 + 3.02618I$ | $8.05288 - 2.57798I$ |
| $u = 1.46039 - 0.14631I$ $a = -0.589431 + 0.029298I$ $b = -0.810187 - 0.008550I$ | $7.28227 - 3.02618I$ | $8.05288 + 2.57798I$ |
| $u = -1.50300 + 0.26177I$ $a = 1.77777 + 0.03837I$ $b = 0.23595 + 2.50634I$ | $16.2359 - 9.9783I$ | $6.35264 + 4.88027I$ |
| $u = -1.50300 - 0.26177I$ $a = 1.77777 - 0.03837I$ $b = 0.23595 - 2.50634I$ | $16.2359 + 9.9783I$ | $6.35264 - 4.88027I$ |
| $u = -1.52245 + 0.22649I$ $a = -1.49085 + 0.18083I$ $b = -0.42745 - 2.45052I$ | $16.8152 - 1.7067I$ | $7.03198 + 0.67482I$ |
| $u = -1.52245 - 0.22649I$ $a = -1.49085 - 0.18083I$ $b = -0.42745 + 2.45052I$ | $16.8152 + 1.7067I$ | $7.03198 - 0.67482I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------------|---------------------------------------|-----------------------|
| $u = 0.152064 + 0.338601I$ | $-1.75639 + 0.64723I$ | $-5.17438 + 1.08919I$ |
| $a = 1.36411 + 1.84123I$ | | |
| $b = 0.929357 - 0.322994I$ | | |
| $u = 0.152064 - 0.338601I$ | $-1.75639 - 0.64723I$ | $-5.17438 - 1.08919I$ |
| $a = 1.36411 - 1.84123I$ | | |
| $b = 0.929357 + 0.322994I$ | | |

$$\text{II. } I_2^u = \langle b + 1, u^3 + a - 2u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 + 2u \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^3 + 4u \\ -u^3 + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 + 2u \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 - 2u \\ u^3 - u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 - 2u \\ u^3 - u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-3u^3 - u^2 + 8u + 3$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------|-----------------------------------|
| c_1 | $(u - 1)^5$ |
| c_2, c_4 | $(u + 1)^5$ |
| c_3, c_8 | u^5 |
| c_5, c_9 | $u^5 + u^4 + 2u^3 + u^2 + u + 1$ |
| c_6, c_7 | $u^5 - u^4 - 2u^3 + u^2 + u + 1$ |
| c_{10} | $u^5 + u^4 - 2u^3 - u^2 + u - 1$ |
| c_{11} | $u^5 - 3u^4 + 4u^3 - u^2 - u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------|------------------------------------|
| c_1, c_2, c_4 | $(y - 1)^5$ |
| c_3, c_8 | y^5 |
| c_5, c_9 | $y^5 + 3y^4 + 4y^3 + y^2 - y - 1$ |
| c_6, c_7, c_{10} | $y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$ |
| c_{11} | $y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -1.21774$ $a = -0.629714$ $b = -1.00000$ | 0.756147 | -2.80750 |
| $u = -0.309916 + 0.549911I$ $a = -0.871221 + 1.107660I$ $b = -1.00000$ | $-1.31583 - 1.53058I$ | $-0.02714 + 4.76366I$ |
| $u = -0.309916 - 0.549911I$ $a = -0.871221 - 1.107660I$ $b = -1.00000$ | $-1.31583 + 1.53058I$ | $-0.02714 - 4.76366I$ |
| $u = 1.41878 + 0.21917I$ $a = 0.186078 - 0.874646I$ $b = -1.00000$ | $4.22763 + 4.40083I$ | $4.43089 - 2.80751I$ |
| $u = 1.41878 - 0.21917I$ $a = 0.186078 + 0.874646I$ $b = -1.00000$ | $4.22763 - 4.40083I$ | $4.43089 + 2.80751I$ |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------|---|
| c_1 | $((u - 1)^5)(u^{22} - 6u^{21} + \dots + 6u - 1)$ |
| c_2 | $((u + 1)^5)(u^{22} + 2u^{21} + \dots + 2u + 1)$ |
| c_3, c_8 | $u^5(u^{22} - u^{21} + \dots - 64u + 32)$ |
| c_4 | $((u + 1)^5)(u^{22} - 6u^{21} + \dots + 6u - 1)$ |
| c_5 | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)(u^{22} + 2u^{21} + \dots + 2996u - 1960)$ |
| c_6, c_7 | $(u^5 - u^4 - 2u^3 + u^2 + u + 1)(u^{22} - 2u^{21} + \dots - 4u^2 - 1)$ |
| c_9 | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)(u^{22} - 2u^{21} + \dots - 2u + 1)$ |
| c_{10} | $(u^5 + u^4 - 2u^3 - u^2 + u - 1)(u^{22} - 2u^{21} + \dots - 4u^2 - 1)$ |
| c_{11} | $(u^5 - 3u^4 + 4u^3 - u^2 - u + 1)(u^{22} + 6u^{21} + \dots - 64u - 17)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------|--|
| c_1, c_4 | $((y - 1)^5)(y^{22} - 2y^{21} + \dots - 2y + 1)$ |
| c_2 | $((y - 1)^5)(y^{22} + 42y^{21} + \dots - 62y + 1)$ |
| c_3, c_8 | $y^5(y^{22} - 33y^{21} + \dots - 7680y + 1024)$ |
| c_5 | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)$ $\cdot (y^{22} + 66y^{21} + \dots + 61827024y + 3841600)$ |
| c_6, c_7, c_{10} | $(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)(y^{22} - 22y^{21} + \dots + 8y + 1)$ |
| c_9 | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)(y^{22} + 30y^{21} + \dots + 8y + 1)$ |
| c_{11} | $(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)(y^{22} - 14y^{21} + \dots - 2056y + 289)$ |