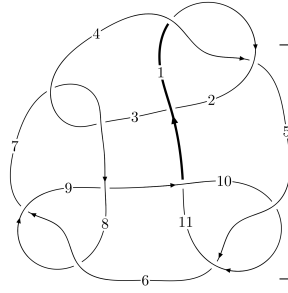
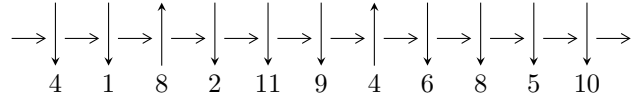


$11n_{72}$  ( $K11n_{72}$ )



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 6 \xrightarrow{c_{11}} 1,2 \xrightarrow{c_4} 4,8 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_9} 9 \longrightarrow c_1, c_2, c_6, c_8$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\begin{aligned}
I_1^u &= \langle u^2 + d, -u^6 - u^5 + u^3 - 2u^2 + 2c - 2u - 1, -u^6 - u^5 + u^3 - 2u^2 + 2b - 2u + 1, a - 1, \\
&\quad u^8 + u^7 - u^6 - 2u^5 + 2u^4 + 3u^3 + u^2 - 2u + 1 \rangle \\
I_2^u &= \langle u^2 + d, -u^{10} - 2u^9 - u^8 + 2u^7 + u^6 - 2u^5 - 4u^4 + u^2 + c + u - 1, b - 1, \\
&\quad u^{10} + 2u^9 - u^8 - 5u^7 - u^6 + 6u^5 + 4u^4 - 4u^3 - 5u^2 + a + u + 4, \\
&\quad u^{11} + 2u^{10} - 4u^8 - 2u^7 + 4u^6 + 5u^5 - 2u^4 - 5u^3 - u^2 + 3u + 1 \rangle \\
I_3^u &= \langle -u^{10} - u^9 + u^8 + 2u^7 - u^6 - 2u^5 + 2u^3 + d - u + 1, \\
&\quad u^{10} + 2u^9 - u^8 - 5u^7 - u^6 + 6u^5 + 4u^4 - 4u^3 - 5u^2 + c + u + 3, \\
&\quad -u^{10} - 2u^9 - u^8 + 2u^7 + u^6 - 2u^5 - 4u^4 + u^2 + b + u, a - 1, \\
&\quad u^{11} + 2u^{10} - 4u^8 - 2u^7 + 4u^6 + 5u^5 - 2u^4 - 5u^3 - u^2 + 3u + 1 \rangle \\
I_4^u &= \langle -17u^{10} + 8u^9 + 27u^8 - 4u^7 - 39u^6 + 6u^5 + 68u^4 + 2u^3 - 75u^2 + 86d - 41u + 80, \\
&\quad -41u^{10} - 6u^9 + 55u^8 + 132u^7 - 3u^6 - 198u^5 - 180u^4 + 106u^3 + 325u^2 + 344c - 109u - 318, b - 1, \\
&\quad -41u^{10} - 6u^9 + 55u^8 + 132u^7 - 3u^6 - 198u^5 - 180u^4 + 106u^3 + 325u^2 + 344a - 109u + 26, \\
&\quad u^{11} - 3u^9 - 2u^8 + 3u^7 + 4u^6 - 2u^4 - u^3 + 3u^2 - 4 \rangle \\
I_5^u &= \langle d, c - 1, b - 1, a + 1, u + 1 \rangle \\
I_6^u &= \langle d + 1, c, b - 1, a, u - 1 \rangle \\
I_7^u &= \langle u^2a + d + 1, c + a, b - 1, a^2 + u^2 + a - u, u^3 - u - 1 \rangle \\
I_8^u &= \langle d + 1, cb - c - 1, a + 1, u + 1 \rangle \\
I_1^v &= \langle a, d + 1, c + a - 1, b - 1, v + 1 \rangle
\end{aligned}$$

\* 8 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 50 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

---

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle u^2+d, -u^6-u^5+\dots+2c-1, -u^6-u^5+\dots+2b+1, a-1, u^8+u^7+\dots-2u+1 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3+u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2+1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ \frac{1}{2}u^6 + \frac{1}{2}u^5 + \dots + u - \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ \frac{1}{2}u^7 + \frac{1}{2}u^6 + \dots + u^2 + \frac{1}{2}u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{2}u^6 + \frac{1}{2}u^5 + \dots + u + \frac{1}{2} \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^4 - u^2 + 1 \\ \frac{1}{2}u^6 + \frac{1}{2}u^5 + \dots + u - \frac{1}{2} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{2}u^7 + \frac{1}{2}u^6 - \frac{1}{2}u^4 + u^2 + \frac{3}{2}u \\ -u^5 + u^3 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u^6 + \frac{1}{2}u^5 - \frac{1}{2}u^3 + u + \frac{1}{2} \\ -u^4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u^6 + \frac{1}{2}u^5 - \frac{1}{2}u^3 + u + \frac{1}{2} \\ -u^4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $3u^7 + 6u^6 - u^5 - 7u^4 + 3u^3 + 16u^2 + 7u - 9$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_{10}$	$u^8 - u^7 - u^6 + 2u^5 + 2u^4 - 3u^3 + u^2 + 2u + 1$
$c_2, c_9, c_{11}$	$u^8 + 3u^7 + 9u^6 + 12u^5 + 20u^4 + 15u^3 + 17u^2 + 2u + 1$
$c_3, c_7$	$u^8 - u^7 - u^6 + 5u^5 - 4u^4 + 8u^2 - 4u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_{10}$	$y^8 - 3y^7 + 9y^6 - 12y^5 + 20y^4 - 15y^3 + 17y^2 - 2y + 1$
$c_2, c_9, c_{11}$	$y^8 + 9y^7 + 49y^6 + 160y^5 + 336y^4 + 425y^3 + 269y^2 + 30y + 1$
$c_3, c_7$	$y^8 - 3y^7 + 3y^6 - y^5 - 32y^3 + 32y^2 + 48y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.725725 + 0.895340I$ $a = 1.00000$ $b = -1.23064 - 0.78420I$ $c = -0.230638 - 0.784197I$ $d = 0.274957 + 1.299540I$	$6.13361 + 3.53925I$	$-3.48597 - 4.52491I$
$u = -0.725725 - 0.895340I$ $a = 1.00000$ $b = -1.23064 + 0.78420I$ $c = -0.230638 + 0.784197I$ $d = 0.274957 - 1.299540I$	$6.13361 - 3.53925I$	$-3.48597 + 4.52491I$
$u = 1.052770 + 0.635427I$ $a = 1.00000$ $b = -1.68524 + 1.42536I$ $c = -0.68524 + 1.42536I$ $d = -0.70455 - 1.33791I$	$-1.61416 - 7.63502I$	$-9.74769 + 6.83193I$
$u = 1.052770 - 0.635427I$ $a = 1.00000$ $b = -1.68524 - 1.42536I$ $c = -0.68524 - 1.42536I$ $d = -0.70455 + 1.33791I$	$-1.61416 + 7.63502I$	$-9.74769 - 6.83193I$
$u = -1.213440 + 0.663590I$ $a = 1.00000$ $b = -2.02473 - 1.24139I$ $c = -1.02473 - 1.24139I$ $d = -1.03209 + 1.61046I$	$0.8567 + 14.6934I$	$-9.31845 - 9.04054I$
$u = -1.213440 - 0.663590I$ $a = 1.00000$ $b = -2.02473 + 1.24139I$ $c = -1.02473 + 1.24139I$ $d = -1.03209 - 1.61046I$	$0.8567 - 14.6934I$	$-9.31845 + 9.04054I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.386400 + 0.333144I$ $a = 1.00000$ $b = -0.059390 + 0.519525I$ $c = 0.940610 + 0.519525I$ $d = -0.038320 - 0.257454I$	$-0.441338 - 1.103720I$	$-5.44788 + 6.54224I$
$u = 0.386400 - 0.333144I$ $a = 1.00000$ $b = -0.059390 - 0.519525I$ $c = 0.940610 - 0.519525I$ $d = -0.038320 + 0.257454I$	$-0.441338 + 1.103720I$	$-5.44788 - 6.54224I$

$$\text{II. } I_2^u = \langle u^2 + d, -u^{10} - 2u^9 + \dots + c - 1, b - 1, u^{10} + 2u^9 + \dots + a + 4, u^{11} + 2u^{10} + \dots + 3u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{10} - 2u^9 + u^8 + 5u^7 + u^6 - 6u^5 - 4u^4 + 4u^3 + 5u^2 - u - 4 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{10} - 3u^9 - u^8 + 5u^7 + 4u^6 - 5u^5 - 7u^4 + 2u^3 + 7u^2 + u - 4 \\ u^9 + u^8 - u^7 - 2u^6 + u^5 + 2u^4 - 2u^2 + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{10} + 2u^9 + u^8 - 2u^7 - u^6 + 2u^5 + 4u^4 - u^2 - u + 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{10} - 3u^9 + u^8 + 7u^7 + 3u^6 - 9u^5 - 7u^4 + 5u^3 + 10u^2 - 2u - 6 \\ u^{10} + 2u^9 - u^8 - 4u^7 - u^6 + 5u^5 + 3u^4 - 3u^3 - 5u^2 + 2u + 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^9 + 2u^8 + u^7 - 2u^6 - u^5 + 2u^4 + 3u^3 - u - 1 \\ -u^5 + u^3 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{10} + 2u^9 + u^8 - 2u^7 - u^6 + 2u^5 + 4u^4 - 2u^2 - u + 1 \\ -u^4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{10} + 2u^9 + u^8 - 2u^7 - u^6 + 2u^5 + 4u^4 - 2u^2 - u + 1 \\ -u^4 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 4u^{10} + 6u^9 - 10u^7 - 4u^6 + 6u^5 + 12u^4 - 4u^3 - 8u^2 - 6u - 4$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{11} - 3u^9 + 2u^8 + 3u^7 - 4u^6 + 2u^4 - u^3 - 3u^2 + 4$
$c_2$	$u^{11} + 6u^{10} + \dots + 24u + 16$
$c_3, c_7$	$u^{11} - 2u^{10} - u^9 + 3u^8 + u^7 - 2u^6 + 4u^5 - 11u^4 + 9u^3 - u^2 - 2u + 2$
$c_5, c_6, c_8$ $c_{10}$	$u^{11} - 2u^{10} + 4u^8 - 2u^7 - 4u^6 + 5u^5 + 2u^4 - 5u^3 + u^2 + 3u - 1$
$c_9, c_{11}$	$u^{11} + 4u^{10} + \dots + 11u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{11} - 6y^{10} + \dots + 24y - 16$
$c_2$	$y^{11} - 6y^{10} + \dots - 224y - 256$
$c_3, c_7$	$y^{11} - 6y^{10} + \dots + 8y - 4$
$c_5, c_6, c_8$ $c_{10}$	$y^{11} - 4y^{10} + \dots + 11y - 1$
$c_9, c_{11}$	$y^{11} + 8y^{10} + \dots + 67y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.952018 + 0.226513I$ $a = -1.085970 + 0.401284I$ $b = 1.00000$ $c = 0.40050 + 4.16652I$ $d = -0.855030 - 0.431288I$	$-5.02081 - 0.74196I$	$-15.5393 + 1.1191I$
$u = 0.952018 - 0.226513I$ $a = -1.085970 - 0.401284I$ $b = 1.00000$ $c = 0.40050 - 4.16652I$ $d = -0.855030 + 0.431288I$	$-5.02081 + 0.74196I$	$-15.5393 - 1.1191I$
$u = 0.850023 + 0.614930I$ $a = 0.007368 - 0.850380I$ $b = 1.00000$ $c = -0.138893 + 1.373110I$ $d = -0.344399 - 1.045410I$	$-0.08426 - 2.41892I$	$-7.07184 + 2.88947I$
$u = 0.850023 - 0.614930I$ $a = 0.007368 + 0.850380I$ $b = 1.00000$ $c = -0.138893 - 1.373110I$ $d = -0.344399 + 1.045410I$	$-0.08426 + 2.41892I$	$-7.07184 - 2.88947I$
$u = -0.523691 + 0.948055I$ $a = -0.184008 + 1.141810I$ $b = 1.00000$ $c = -0.103739 - 0.547821I$ $d = 0.624556 + 0.992977I$	$5.32590 - 2.58451I$	$-3.80806 + 1.01660I$
$u = -0.523691 - 0.948055I$ $a = -0.184008 - 1.141810I$ $b = 1.00000$ $c = -0.103739 + 0.547821I$ $d = 0.624556 - 0.992977I$	$5.32590 + 2.58451I$	$-3.80806 - 1.01660I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.978643 + 0.595733I$ $a = -0.939343 - 0.770160I$ $b = 1.00000$ $c = -0.47651 - 1.53693I$ $d = -0.602844 + 1.166020I$	$-2.61864 + 4.69742I$	$-9.08124 - 5.88322I$
$u = -0.978643 - 0.595733I$ $a = -0.939343 + 0.770160I$ $b = 1.00000$ $c = -0.47651 + 1.53693I$ $d = -0.602844 - 1.166020I$	$-2.61864 - 4.69742I$	$-9.08124 + 5.88322I$
$u = -1.126060 + 0.711355I$ $a = -0.175044 + 0.783251I$ $b = 1.00000$ $c = -0.81852 - 1.22144I$ $d = -0.76197 + 1.60205I$	$3.47965 + 8.65115I$	$-6.21430 - 5.57892I$
$u = -1.126060 - 0.711355I$ $a = -0.175044 - 0.783251I$ $b = 1.00000$ $c = -0.81852 + 1.22144I$ $d = -0.76197 - 1.60205I$	$3.47965 - 8.65115I$	$-6.21430 + 5.57892I$
$u = -0.347303$ $a = -3.24600$ $b = 1.00000$ $c = 1.27433$ $d = -0.120619$	$-2.16369$	$-2.57060$

$$\text{III. } I_3^u = \langle -u^{10} - u^9 + \cdots + d + 1, u^{10} + 2u^9 + \cdots + c + 3, -u^{10} - 2u^9 + \cdots + b + u, a - 1, u^{11} + 2u^{10} + \cdots + 3u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^{10} + 2u^9 + u^8 - 2u^7 - u^6 + 2u^5 + 4u^4 - u^2 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^9 + 2u^8 + u^7 - 2u^6 - u^5 + 2u^4 + 4u^3 - 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{10} - 2u^9 + u^8 + 5u^7 + u^6 - 6u^5 - 4u^4 + 4u^3 + 5u^2 - u - 3 \\ u^{10} + u^9 - u^8 - 2u^7 + u^6 + 2u^5 - 2u^3 + u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^4 - u^2 + 1 \\ u^{10} + 2u^9 + u^8 - 2u^7 - u^6 + 2u^5 + 3u^4 - u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2u^{10} - 3u^9 + 2u^8 + 7u^7 - 9u^5 - 5u^4 + 7u^3 + 7u^2 - 3u - 4 \\ u^{10} - u^9 - 3u^8 - u^7 + 5u^6 + 2u^5 - 3u^4 - 5u^3 + 3u^2 + 3u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^{10} - 3u^9 + 2u^8 + 7u^7 - 8u^5 - 4u^4 + 6u^3 + 6u^2 - 2u - 3 \\ u^{10} - u^8 + 3u^6 - u^5 - 2u^4 - u^3 + 3u^2 - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^{10} - 3u^9 + 2u^8 + 7u^7 - 8u^5 - 4u^4 + 6u^3 + 6u^2 - 2u - 3 \\ u^{10} - u^8 + 3u^6 - u^5 - 2u^4 - u^3 + 3u^2 - 2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 4u^{10} + 6u^9 - 10u^7 - 4u^6 + 6u^5 + 12u^4 - 4u^3 - 8u^2 - 6u - 4$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}$	$u^{11} - 2u^{10} + 4u^8 - 2u^7 - 4u^6 + 5u^5 + 2u^4 - 5u^3 + u^2 + 3u - 1$
$c_2, c_{11}$	$u^{11} + 4u^{10} + \dots + 11u + 1$
$c_3, c_7$	$u^{11} - 2u^{10} - u^9 + 3u^8 + u^7 - 2u^6 + 4u^5 - 11u^4 + 9u^3 - u^2 - 2u + 2$
$c_6, c_8$	$u^{11} - 3u^9 + 2u^8 + 3u^7 - 4u^6 + 2u^4 - u^3 - 3u^2 + 4$
$c_9$	$u^{11} + 6u^{10} + \dots + 24u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_{10}$	$y^{11} - 4y^{10} + \dots + 11y - 1$
$c_2, c_{11}$	$y^{11} + 8y^{10} + \dots + 67y - 1$
$c_3, c_7$	$y^{11} - 6y^{10} + \dots + 8y - 4$
$c_6, c_8$	$y^{11} - 6y^{10} + \dots + 24y - 16$
$c_9$	$y^{11} - 6y^{10} + \dots - 224y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.952018 + 0.226513I$ $a = 1.00000$ $b = -0.59950 + 4.16652I$ $c = -0.085971 + 0.401284I$ $d = -1.246580 + 0.306031I$	$-5.02081 - 0.74196I$	$-15.5393 + 1.1191I$
$u = 0.952018 - 0.226513I$ $a = 1.00000$ $b = -0.59950 - 4.16652I$ $c = -0.085971 - 0.401284I$ $d = -1.246580 - 0.306031I$	$-5.02081 + 0.74196I$	$-15.5393 - 1.1191I$
$u = 0.850023 + 0.614930I$ $a = 1.00000$ $b = -1.13889 + 1.37311I$ $c = 1.007370 - 0.850380I$ $d = 0.235931 + 0.760242I$	$-0.08426 - 2.41892I$	$-7.07184 + 2.88947I$
$u = 0.850023 - 0.614930I$ $a = 1.00000$ $b = -1.13889 - 1.37311I$ $c = 1.007370 + 0.850380I$ $d = 0.235931 - 0.760242I$	$-0.08426 + 2.41892I$	$-7.07184 - 2.88947I$
$u = -0.523691 + 0.948055I$ $a = 1.00000$ $b = -1.103740 - 0.547821I$ $c = 0.815992 + 1.141810I$ $d = -0.37585 - 1.52338I$	$5.32590 - 2.58451I$	$-3.80806 + 1.01660I$
$u = -0.523691 - 0.948055I$ $a = 1.00000$ $b = -1.103740 + 0.547821I$ $c = 0.815992 - 1.141810I$ $d = -0.37585 + 1.52338I$	$5.32590 + 2.58451I$	$-3.80806 - 1.01660I$



Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.978643 + 0.595733I$ $a = 1.00000$ $b = -1.47651 - 1.53693I$ $c = 0.060657 - 0.770160I$ $d = -1.86145 - 0.53501I$	$-2.61864 + 4.69742I$	$-9.08124 - 5.88322I$
$u = -0.978643 - 0.595733I$ $a = 1.00000$ $b = -1.47651 + 1.53693I$ $c = 0.060657 + 0.770160I$ $d = -1.86145 + 0.53501I$	$-2.61864 - 4.69742I$	$-9.08124 + 5.88322I$
$u = -1.126060 + 0.711355I$ $a = 1.00000$ $b = -1.81852 - 1.22144I$ $c = 0.824956 + 0.783251I$ $d = 0.883402 - 0.724805I$	$3.47965 + 8.65115I$	$-6.21430 - 5.57892I$
$u = -1.126060 - 0.711355I$ $a = 1.00000$ $b = -1.81852 + 1.22144I$ $c = 0.824956 - 0.783251I$ $d = 0.883402 + 0.724805I$	$3.47965 - 8.65115I$	$-6.21430 + 5.57892I$
$u = -0.347303$ $a = 1.00000$ $b = 0.274328$ $c = -2.24600$ $d = -1.27091$	$-2.16369$	$-2.57060$

IV.  $I_4^u = \langle -17u^{10} + 8u^9 + \dots + 86d + 80, -41u^{10} - 6u^9 + \dots + 344c - 318, b - 1, -41u^{10} - 6u^9 + \dots + 344a + 26, u^{11} - 3u^9 + \dots + 3u^2 - 4 \rangle$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.119186u^{10} + 0.0174419u^9 + \dots + 0.316860u - 0.0755814 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.232558u^{10} - 0.197674u^9 + \dots - 0.174419u - 0.476744 \\ 0.0174419u^{10} + 0.197674u^9 + \dots + 0.924419u + 0.476744 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.119186u^{10} + 0.0174419u^9 + \dots + 0.316860u + 0.924419 \\ 0.197674u^{10} - 0.0930233u^9 + \dots + 0.476744u - 0.930233 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0377907u^{10} - 0.238372u^9 + \dots + 0.00290698u - 0.633721 \\ 0.279070u^{10} + 0.162791u^9 + \dots + 0.790698u + 0.627907 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.156977u^{10} + 0.279070u^9 + \dots - 0.180233u + 0.790698 \\ 0.238372u^{10} + 0.0348837u^9 + \dots + 0.633721u - 0.151163 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0784884u^{10} + 0.110465u^9 + \dots - 0.159884u + 0.854651 \\ 0.116279u^{10} - 0.348837u^9 + \dots + 0.162791u - 0.488372 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0784884u^{10} + 0.110465u^9 + \dots - 0.159884u + 0.854651 \\ 0.116279u^{10} - 0.348837u^9 + \dots + 0.162791u - 0.488372 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{54}{43}u^{10} + \frac{10}{43}u^9 - \frac{106}{43}u^8 - \frac{134}{43}u^7 - \frac{38}{43}u^6 + \frac{158}{43}u^5 + \frac{128}{43}u^4 + \frac{24}{43}u^3 - \frac{126}{43}u^2 + \frac{196}{43}u - \frac{244}{43}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_6$ $c_8$	$u^{11} - 2u^{10} + 4u^8 - 2u^7 - 4u^6 + 5u^5 + 2u^4 - 5u^3 + u^2 + 3u - 1$
$c_2, c_9$	$u^{11} + 4u^{10} + \dots + 11u + 1$
$c_3, c_7$	$u^{11} - 2u^{10} - u^9 + 3u^8 + u^7 - 2u^6 + 4u^5 - 11u^4 + 9u^3 - u^2 - 2u + 2$
$c_5, c_{10}$	$u^{11} - 3u^9 + 2u^8 + 3u^7 - 4u^6 + 2u^4 - u^3 - 3u^2 + 4$
$c_{11}$	$u^{11} + 6u^{10} + \dots + 24u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_6$ $c_8$	$y^{11} - 4y^{10} + \dots + 11y - 1$
$c_2, c_9$	$y^{11} + 8y^{10} + \dots + 67y - 1$
$c_3, c_7$	$y^{11} - 6y^{10} + \dots + 8y - 4$
$c_5, c_{10}$	$y^{11} - 6y^{10} + \dots + 24y - 16$
$c_{11}$	$y^{11} - 6y^{10} + \dots - 224y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.360061 + 1.006500I$ $a = -0.271755 + 1.216000I$ $b = 1.00000$ $c = 0.72825 + 1.21600I$ $d = -0.76197 - 1.60205I$	$3.47965 - 8.65115I$	$-6.21430 + 5.57892I$
$u = -0.360061 - 1.006500I$ $a = -0.271755 - 1.216000I$ $b = 1.00000$ $c = 0.72825 - 1.21600I$ $d = -0.76197 + 1.60205I$	$3.47965 + 8.65115I$	$-6.21430 - 5.57892I$
$u = 0.529187 + 0.718311I$ $a = 0.010188 - 1.175860I$ $b = 1.00000$ $c = 1.01019 - 1.17586I$ $d = -0.344399 + 1.045410I$	$-0.08426 + 2.41892I$	$-7.07184 - 2.88947I$
$u = 0.529187 - 0.718311I$ $a = 0.010188 + 1.175860I$ $b = 1.00000$ $c = 1.01019 + 1.17586I$ $d = -0.344399 - 1.045410I$	$-0.08426 - 2.41892I$	$-7.07184 + 2.88947I$
$u = 1.12735$ $a = -0.308071$ $b = 1.00000$ $c = 0.691929$ $d = -0.120619$	$-2.16369$	$-2.57060$
$u = -1.124760 + 0.136043I$ $a = -0.810207 - 0.299385I$ $b = 1.00000$ $c = 0.189793 - 0.299385I$ $d = -0.855030 - 0.431288I$	$-5.02081 - 0.74196I$	$-15.5393 + 1.1191I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.124760 - 0.136043I$ $a = -0.810207 + 0.299385I$ $b = 1.00000$ $c = 0.189793 + 0.299385I$ $d = -0.855030 + 0.431288I$	$-5.02081 + 0.74196I$	$-15.5393 - 1.1191I$
$u = -0.986131 + 0.772404I$ $a = -0.137568 + 0.853636I$ $b = 1.00000$ $c = 0.862432 + 0.853636I$ $d = 0.624556 - 0.992977I$	$5.32590 + 2.58451I$	$-3.80806 - 1.01660I$
$u = -0.986131 - 0.772404I$ $a = -0.137568 - 0.853636I$ $b = 1.00000$ $c = 0.862432 - 0.853636I$ $d = 0.624556 + 0.992977I$	$5.32590 - 2.58451I$	$-3.80806 + 1.01660I$
$u = 1.378090 + 0.194114I$ $a = -0.636622 + 0.521961I$ $b = 1.00000$ $c = 0.363378 + 0.521961I$ $d = -0.602844 + 1.166020I$	$-2.61864 + 4.69742I$	$-9.08124 - 5.88322I$
$u = 1.378090 - 0.194114I$ $a = -0.636622 - 0.521961I$ $b = 1.00000$ $c = 0.363378 - 0.521961I$ $d = -0.602844 - 1.166020I$	$-2.61864 - 4.69742I$	$-9.08124 + 5.88322I$

$$\mathbf{V. } I_5^u = \langle d, c - 1, b - 1, a + 1, u + 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -12**

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_5$	$u - 1$
$c_2, c_4, c_{10}$ $c_{11}$	$u + 1$
$c_3, c_6, c_7$ $c_8, c_9$	$u$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_{10}, c_{11}$	$y - 1$
$c_3, c_6, c_7$ $c_8, c_9$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = -1.00000$		
$b = 1.00000$	-3.28987	-12.0000
$c = 1.00000$		
$d = 0$		

$$\text{VI. } I_6^u = \langle d + 1, c, b - 1, a, u - 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -12**

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_7$	$u$
$c_5, c_8, c_9$ $c_{11}$	$u + 1$
$c_6, c_{10}$	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_7$	$y$
$c_5, c_6, c_8$ $c_9, c_{10}, c_{11}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$		
$b = 1.00000$	-3.28987	-12.0000
$c = 0$		
$d = -1.00000$		

$$\text{VII. } I_7^u = \langle u^2a + d + 1, c + a, b - 1, a^2 + u^2 + a - u, u^3 - u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -au + u^2 - u - 1 \\ au + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a \\ -u^2a - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -au + u^2 + a - u - 1 \\ u^2a + au + u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -au + u^2 - a - u - 1 \\ -u^2a + au + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2a + u^2 - a \\ -u^2a + au + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2a + u^2 - a \\ -u^2a + au + u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_{10}$	$(u^3 - u + 1)^2$
$c_2, c_9, c_{11}$	$(u^3 + 2u^2 + u + 1)^2$
$c_3, c_7$	$(u + 1)^6$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_{10}$	$(y^3 - 2y^2 + y - 1)^2$
$c_2, c_9, c_{11}$	$(y^3 - 2y^2 - 3y - 1)^2$
$c_3, c_7$	$(y - 1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_7^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.662359 + 0.562280I$ $a = 0.162359 + 0.986732I$ $b = 1.00000$ $c = -0.162359 - 0.986732I$ $d = -1.75488$	-1.64493	-6.00000
$u = -0.662359 + 0.562280I$ $a = -1.16236 - 0.98673I$ $b = 1.00000$ $c = 1.16236 + 0.98673I$ $d = -0.122561 - 0.744862I$	-1.64493	-6.00000
$u = -0.662359 - 0.562280I$ $a = 0.162359 - 0.986732I$ $b = 1.00000$ $c = -0.162359 + 0.986732I$ $d = -1.75488$	-1.64493	-6.00000
$u = -0.662359 - 0.562280I$ $a = -1.16236 + 0.98673I$ $b = 1.00000$ $c = 1.16236 - 0.98673I$ $d = -0.122561 + 0.744862I$	-1.64493	-6.00000
$u = 1.32472$ $a = -0.500000 + 0.424452I$ $b = 1.00000$ $c = 0.500000 - 0.424452I$ $d = -0.122561 - 0.744862I$	-1.64493	-6.00000
$u = 1.32472$ $a = -0.500000 - 0.424452I$ $b = 1.00000$ $c = 0.500000 + 0.424452I$ $d = -0.122561 + 0.744862I$	-1.64493	-6.00000

$$\text{VIII. } I_{\mathfrak{g}}^u = \langle d + 1, cb - c - 1, a + 1, u + 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ b - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} c \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ b - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} c \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} c + 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} c + 1 \\ -1 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =  $-c^2 - b^2 + 2b - 17$**

**(iv) u-Polynomials at the component :** It cannot be defined for a positive dimension component.

**(v) Riley Polynomials at the component :** It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

Solution to $I_8^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = \dots$		
$a = \dots$		
$b = \dots$	-4.93480	-18.1451 - 0.9948I
$c = \dots$		
$d = \dots$		

$$\text{IX. } I_1^v = \langle a, d + 1, c + a - 1, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_6$	$u - 1$
$c_2, c_4, c_8$ $c_9$	$u + 1$
$c_3, c_5, c_7$ $c_{10}, c_{11}$	$u$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_6, c_8, c_9$	$y - 1$
$c_3, c_5, c_7$ $c_{10}, c_{11}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$		
$b = 1.00000$	-3.28987	-12.0000
$c = 1.00000$		
$d = -1.00000$		



## X. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u(u-1)^2(u^3-u+1)^2(u^8-u^7+\dots+2u+1)$ $\cdot (u^{11}-3u^9+2u^8+3u^7-4u^6+2u^4-u^3-3u^2+4)$ $\cdot (u^{11}-2u^{10}+4u^8-2u^7-4u^6+5u^5+2u^4-5u^3+u^2+3u-1)^2$
$c_2, c_9, c_{11}$	$u(u+1)^2(u^3+2u^2+u+1)^2$ $\cdot (u^8+3u^7+9u^6+12u^5+20u^4+15u^3+17u^2+2u+1)$ $\cdot ((u^{11}+4u^{10}+\dots+11u+1)^2)(u^{11}+6u^{10}+\dots+24u+16)$
$c_3, c_7$	$u^3(u+1)^6(u^8-u^7-u^6+5u^5-4u^4+8u^2-4u+4)$ $\cdot (u^{11}-2u^{10}-u^9+3u^8+u^7-2u^6+4u^5-11u^4+9u^3-u^2-2u+2)^3$
$c_4, c_8$	$u(u+1)^2(u^3-u+1)^2(u^8-u^7+\dots+2u+1)$ $\cdot (u^{11}-3u^9+2u^8+3u^7-4u^6+2u^4-u^3-3u^2+4)$ $\cdot (u^{11}-2u^{10}+4u^8-2u^7-4u^6+5u^5+2u^4-5u^3+u^2+3u-1)^2$
$c_5, c_{10}$	$u(u-1)(u+1)(u^3-u+1)^2(u^8-u^7+\dots+2u+1)$ $\cdot (u^{11}-3u^9+2u^8+3u^7-4u^6+2u^4-u^3-3u^2+4)$ $\cdot (u^{11}-2u^{10}+4u^8-2u^7-4u^6+5u^5+2u^4-5u^3+u^2+3u-1)^2$

### XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_8, c_{10}$	$y(y-1)^2(y^3-2y^2+y-1)^2$ $\cdot (y^8-3y^7+9y^6-12y^5+20y^4-15y^3+17y^2-2y+1)$ $\cdot (y^{11}-6y^{10}+\dots+24y-16)(y^{11}-4y^{10}+\dots+11y-1)^2$
$c_2, c_9, c_{11}$	$y(y-1)^2(y^3-2y^2-3y-1)^2$ $\cdot (y^8+9y^7+49y^6+160y^5+336y^4+425y^3+269y^2+30y+1)$ $\cdot (y^{11}-6y^{10}+\dots-224y-256)(y^{11}+8y^{10}+\dots+67y-1)^2$
$c_3, c_7$	$y^3(y-1)^6(y^8-3y^7+3y^6-y^5-32y^3+32y^2+48y+16)$ $\cdot (y^{11}-6y^{10}+\dots+8y-4)^3$