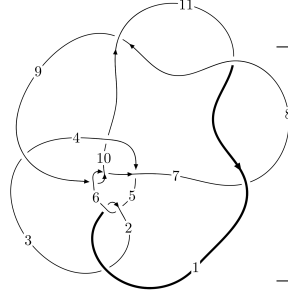
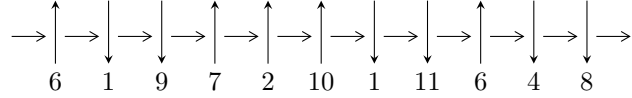


11n₈₃ (K11n₈₃)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$1,6 \xrightarrow{c_1} 2 \xrightarrow{c_2} 3,10 \xrightarrow{c_6} 7 \xrightarrow{c_7} 8 \xrightarrow{c_5} 5 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_{11}} 11 \rightsquigarrow c_3, c_8, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -1.65693 \times 10^{21}u^{29} - 1.25426 \times 10^{22}u^{28} + \dots + 7.78277 \times 10^{21}b - 2.65124 \times 10^{22}, \\ -1.16811 \times 10^{22}u^{29} - 8.79857 \times 10^{22}u^{28} + \dots + 2.33483 \times 10^{22}a - 1.51866 \times 10^{23}, \\ u^{30} + 8u^{29} + \dots + 59u + 9 \rangle$$

$$I_2^u = \langle b^2 - 2bu - u + 1, a - u - 1, u^2 + u + 1 \rangle$$

$$I_3^u = \langle b + u, a + u + 1, u^2 + u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 36 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.66 \times 10^{21}u^{29} - 1.25 \times 10^{22}u^{28} + \dots + 7.78 \times 10^{21}b - 2.65 \times 10^{22}, -1.17 \times 10^{22}u^{29} - 8.80 \times 10^{22}u^{28} + \dots + 2.33 \times 10^{22}a - 1.52 \times 10^{23}, u^{30} + 8u^{29} + \dots + 59u + 9 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.500296u^{29} + 3.76840u^{28} + \dots + 34.8145u + 6.50436 \\ 0.212897u^{29} + 1.61159u^{28} + \dots + 17.2043u + 3.40655 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.195327u^{29} - 1.50953u^{28} + \dots - 27.9406u - 7.82719 \\ -0.200124u^{29} - 1.50933u^{28} + \dots - 14.4262u - 3.01543 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.00479750u^{29} - 0.000201005u^{28} + \dots - 13.5144u - 4.81176 \\ -0.200124u^{29} - 1.50933u^{28} + \dots - 14.4262u - 3.01543 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.582123u^{29} + 4.29047u^{28} + \dots + 43.1171u + 10.9976 \\ 0.243597u^{29} + 1.73550u^{28} + \dots + 12.1493u + 1.59905 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.500296u^{29} + 3.76840u^{28} + \dots + 34.8145u + 6.50436 \\ 0.275979u^{29} + 2.11887u^{28} + \dots + 26.5057u + 5.51226 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.378505u^{29} - 2.81515u^{28} + \dots - 27.1883u - 5.12752 \\ 0.163272u^{29} + 1.28132u^{28} + \dots + 17.0522u + 4.24326 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.378505u^{29} - 2.81515u^{28} + \dots - 27.1883u - 5.12752 \\ 0.163272u^{29} + 1.28132u^{28} + \dots + 17.0522u + 4.24326 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{1349639825927485091569}{7782769931873059073724}u^{29} + \frac{9179424603349810678583}{7782769931873059073724}u^{28} + \dots + \frac{153279025524269859187337}{7782769931873059073724}u + \frac{5608854558132017698152}{648564160989421589477}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$u^{30} - 8u^{29} + \dots - 59u + 9$
c_2	$u^{30} + 32u^{29} + \dots + 47u + 81$
c_3	$u^{30} - 8u^{28} + \dots - 3557u + 451$
c_4	$u^{30} + 4u^{29} + \dots - 295u + 1601$
c_6, c_9	$u^{30} - 3u^{29} + \dots + 4u + 3$
c_7, c_8, c_{11}	$u^{30} - u^{29} + \dots - 16u + 4$
c_{10}	$u^{30} + 2u^{29} + \dots - u + 3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5	$y^{30} + 32y^{29} + \dots + 47y + 81$
c_2	$y^{30} - 64y^{29} + \dots - 221233y + 6561$
c_3	$y^{30} - 16y^{29} + \dots - 5277497y + 203401$
c_4	$y^{30} + 24y^{29} + \dots + 28807823y + 2563201$
c_6, c_9	$y^{30} - 9y^{29} + \dots - 58y + 9$
c_7, c_8, c_{11}	$y^{30} + 25y^{29} + \dots - 32y + 16$
c_{10}	$y^{30} + 8y^{29} + \dots + 59y + 9$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.289006 + 0.960575I$		
$a = 0.341844 + 0.310737I$	$4.98680 - 2.32242I$	$-0.98983 + 4.15024I$
$b = 0.004028 - 1.301360I$		
$u = -0.289006 - 0.960575I$		
$a = 0.341844 - 0.310737I$	$4.98680 + 2.32242I$	$-0.98983 - 4.15024I$
$b = 0.004028 + 1.301360I$		
$u = -0.827863 + 0.788133I$		
$a = 0.610296 + 0.163041I$	$0.80409 - 2.85458I$	$-2.92837 + 5.79821I$
$b = -0.907811 + 0.765680I$		
$u = -0.827863 - 0.788133I$		
$a = 0.610296 - 0.163041I$	$0.80409 + 2.85458I$	$-2.92837 - 5.79821I$
$b = -0.907811 - 0.765680I$		
$u = -0.215656 + 1.206980I$		
$a = 0.182869 + 1.070300I$	$3.45780 - 2.70205I$	$2.31582 + 3.42763I$
$b = -0.07834 + 1.70158I$		
$u = -0.215656 - 1.206980I$		
$a = 0.182869 - 1.070300I$	$3.45780 + 2.70205I$	$2.31582 - 3.42763I$
$b = -0.07834 - 1.70158I$		
$u = -0.956886 + 0.832908I$		
$a = -0.124030 - 0.650953I$	$4.02348 - 1.34734I$	$3.26214 + 0.58804I$
$b = 1.108780 - 0.402600I$		
$u = -0.956886 - 0.832908I$		
$a = -0.124030 + 0.650953I$	$4.02348 + 1.34734I$	$3.26214 - 0.58804I$
$b = 1.108780 + 0.402600I$		
$u = -1.194550 + 0.646359I$		
$a = -0.806434 + 0.092426I$	$4.62105 - 5.90679I$	$4.52831 + 6.63187I$
$b = 1.66643 - 0.93121I$		
$u = -1.194550 - 0.646359I$		
$a = -0.806434 - 0.092426I$	$4.62105 + 5.90679I$	$4.52831 - 6.63187I$
$b = 1.66643 + 0.93121I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.29191 + 1.42887I$ $a = 0.744398 - 0.614810I$ $b = -1.13746 - 1.62619I$	$-3.80529 + 5.57168I$	$-1.0000 - 2.74433I$
$u = 0.29191 - 1.42887I$ $a = 0.744398 + 0.614810I$ $b = -1.13746 + 1.62619I$	$-3.80529 - 5.57168I$	$-1.0000 + 2.74433I$
$u = 0.534931 + 0.013556I$ $a = 1.31577 + 1.24844I$ $b = -0.939218 - 0.571832I$	$0.93475 + 2.30280I$	$-1.24616 - 3.74570I$
$u = 0.534931 - 0.013556I$ $a = 1.31577 - 1.24844I$ $b = -0.939218 + 0.571832I$	$0.93475 - 2.30280I$	$-1.24616 + 3.74570I$
$u = 0.131917 + 0.513534I$ $a = -1.123520 - 0.076835I$ $b = 0.192615 + 0.679919I$	$-1.028650 - 0.891272I$	$-5.65753 + 3.58094I$
$u = 0.131917 - 0.513534I$ $a = -1.123520 + 0.076835I$ $b = 0.192615 - 0.679919I$	$-1.028650 + 0.891272I$	$-5.65753 - 3.58094I$
$u = -0.288296 + 0.396727I$ $a = -1.58170 - 1.42670I$ $b = -0.0250531 - 0.0445070I$	$1.85260 - 1.11432I$	$2.87293 - 2.42323I$
$u = -0.288296 - 0.396727I$ $a = -1.58170 + 1.42670I$ $b = -0.0250531 + 0.0445070I$	$1.85260 + 1.11432I$	$2.87293 + 2.42323I$
$u = -0.473408 + 0.105538I$ $a = 2.08968 + 0.90137I$ $b = -0.08348 + 1.42196I$	$7.52373 - 0.32119I$	$8.17779 - 0.83002I$
$u = -0.473408 - 0.105538I$ $a = 2.08968 - 0.90137I$ $b = -0.08348 - 1.42196I$	$7.52373 + 0.32119I$	$8.17779 + 0.83002I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.01716 + 1.58025I$		
$a = -0.639515 - 0.509136I$	$-4.75687 - 1.39165I$	0
$b = -0.029559 - 0.549776I$		
$u = 0.01716 - 1.58025I$		
$a = -0.639515 + 0.509136I$	$-4.75687 + 1.39165I$	0
$b = -0.029559 + 0.549776I$		
$u = 0.09265 + 1.59384I$		
$a = -0.666239 + 0.534839I$	$-8.24005 + 0.28940I$	0
$b = 0.455313 + 1.306320I$		
$u = 0.09265 - 1.59384I$		
$a = -0.666239 - 0.534839I$	$-8.24005 - 0.28940I$	0
$b = 0.455313 - 1.306320I$		
$u = -0.17358 + 1.65624I$		
$a = 0.598313 - 0.464993I$	$-4.52151 - 5.10629I$	0
$b = 0.030527 - 0.633530I$		
$u = -0.17358 - 1.65624I$		
$a = 0.598313 + 0.464993I$	$-4.52151 + 5.10629I$	0
$b = 0.030527 + 0.633530I$		
$u = -0.22083 + 1.70141I$		
$a = 0.625937 + 0.523734I$	$-7.86584 - 6.86749I$	0
$b = -0.49633 + 1.34756I$		
$u = -0.22083 - 1.70141I$		
$a = 0.625937 - 0.523734I$	$-7.86584 + 6.86749I$	0
$b = -0.49633 - 1.34756I$		
$u = -0.42849 + 1.69223I$		
$a = -0.623225 - 0.533526I$	$-2.92088 - 12.01220I$	0
$b = 1.23958 - 1.77796I$		
$u = -0.42849 - 1.69223I$		
$a = -0.623225 + 0.533526I$	$-2.92088 + 12.01220I$	0
$b = 1.23958 + 1.77796I$		

$$\text{II. } I_2^u = \langle b^2 - 2bu - u + 1, a - u - 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u + 1 \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u - 1 \\ -b + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b - 2u - 1 \\ -b + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} b - 2u + 1 \\ -bu + 2u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u + 1 \\ b - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -bu - b - 2 \\ 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -bu - b - 2 \\ 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u + 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_{10}	$(u^2 + u + 1)^2$
c_3	$u^4 - 2u^3 + u^2 - 6u + 9$
c_4	$u^4 + 2u^3 + u^2 + 6u + 9$
c_5	$(u^2 - u + 1)^2$
c_6	$(u - 1)^4$
c_7, c_8, c_{11}	$(u^2 + 2)^2$
c_9	$(u + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5 c_{10}	$(y^2 + y + 1)^2$
c_3, c_4	$y^4 - 2y^3 - 5y^2 - 18y + 81$
c_6, c_9	$(y - 1)^4$
c_7, c_8, c_{11}	$(y + 2)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 0.500000 + 0.866025I$	$6.57974 - 2.02988I$	$6.00000 + 3.46410I$
$b = -0.500000 - 0.548188I$		
$u = -0.500000 + 0.866025I$		
$a = 0.500000 + 0.866025I$	$6.57974 - 2.02988I$	$6.00000 + 3.46410I$
$b = -0.500000 + 2.28024I$		
$u = -0.500000 - 0.866025I$		
$a = 0.500000 - 0.866025I$	$6.57974 + 2.02988I$	$6.00000 - 3.46410I$
$b = -0.500000 + 0.548188I$		
$u = -0.500000 - 0.866025I$		
$a = 0.500000 - 0.866025I$	$6.57974 + 2.02988I$	$6.00000 - 3.46410I$
$b = -0.500000 - 2.28024I$		

$$\text{III. } I_3^u = \langle b + u, a + u + 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u - 1 \\ -u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u - 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u - 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u + 1 \\ u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u - 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_3 c_4	$u^2 + u + 1$
c_5, c_{10}	$u^2 - u + 1$
c_6	$(u + 1)^2$
c_7, c_8, c_{11}	u^2
c_9	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_4, c_5, c_{10}	$y^2 + y + 1$
c_6, c_9	$(y - 1)^2$
c_7, c_8, c_{11}	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$	$1.64493 - 2.02988I$	$0. + 3.46410I$
$a = -0.500000 - 0.866025I$		
$b = 0.500000 - 0.866025I$		
$u = -0.500000 - 0.866025I$	$1.64493 + 2.02988I$	$0. - 3.46410I$
$a = -0.500000 + 0.866025I$		
$b = 0.500000 + 0.866025I$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u^2 + u + 1)^3)(u^{30} - 8u^{29} + \dots - 59u + 9)$
c_2	$((u^2 + u + 1)^3)(u^{30} + 32u^{29} + \dots + 47u + 81)$
c_3	$(u^2 + u + 1)(u^4 - 2u^3 + u^2 - 6u + 9)(u^{30} - 8u^{28} + \dots - 3557u + 451)$
c_4	$(u^2 + u + 1)(u^4 + 2u^3 + u^2 + 6u + 9)(u^{30} + 4u^{29} + \dots - 295u + 1601)$
c_5	$((u^2 - u + 1)^3)(u^{30} - 8u^{29} + \dots - 59u + 9)$
c_6	$((u - 1)^4)(u + 1)^2(u^{30} - 3u^{29} + \dots + 4u + 3)$
c_7, c_8, c_{11}	$u^2(u^2 + 2)^2(u^{30} - u^{29} + \dots - 16u + 4)$
c_9	$((u - 1)^2)(u + 1)^4(u^{30} - 3u^{29} + \dots + 4u + 3)$
c_{10}	$(u^2 - u + 1)(u^2 + u + 1)^2(u^{30} + 2u^{29} + \dots - u + 3)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_5	$((y^2 + y + 1)^3)(y^{30} + 32y^{29} + \dots + 47y + 81)$
c_2	$((y^2 + y + 1)^3)(y^{30} - 64y^{29} + \dots - 221233y + 6561)$
c_3	$(y^2 + y + 1)(y^4 - 2y^3 - 5y^2 - 18y + 81)$ $\cdot (y^{30} - 16y^{29} + \dots - 5277497y + 203401)$
c_4	$(y^2 + y + 1)(y^4 - 2y^3 - 5y^2 - 18y + 81)$ $\cdot (y^{30} + 24y^{29} + \dots + 28807823y + 2563201)$
c_6, c_9	$((y - 1)^6)(y^{30} - 9y^{29} + \dots - 58y + 9)$
c_7, c_8, c_{11}	$y^2(y + 2)^4(y^{30} + 25y^{29} + \dots - 32y + 16)$
c_{10}	$((y^2 + y + 1)^3)(y^{30} + 8y^{29} + \dots + 59y + 9)$