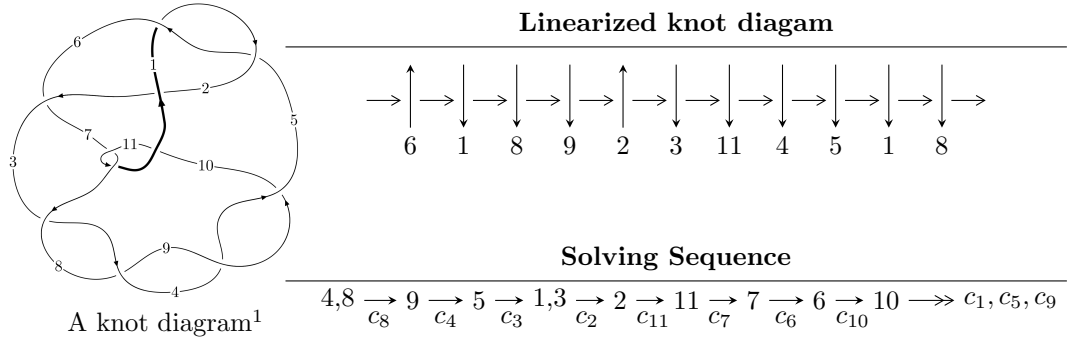


11n<sub>88</sub> (K11n<sub>88</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -68u^{10} + 123u^9 + \dots + 3382b - 1078, 1249u^{10} - 46u^9 + \dots + 6764a - 1934, \\ u^{11} - u^{10} - 10u^9 + 9u^8 + 37u^7 - 31u^6 - 54u^5 + 48u^4 + 8u^3 - 4u - 4 \rangle$$

$$I_2^u = \langle b + 1, 2a^2 - au + 4a - u + 3, u^2 - 2 \rangle$$

$$I_1^v = \langle a, b - 1, v^2 + v + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 17 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -68u^{10} + 123u^9 + \dots + 3382b - 1078, 1249u^{10} - 46u^9 + \dots + 6764a - 1934, u^{11} - u^{10} + \dots - 4u - 4 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.184654u^{10} + 0.00680071u^9 + \dots - 0.694855u + 0.285925 \\ 0.0201064u^{10} - 0.0363690u^9 + \dots + 0.324660u + 0.318746 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.102750u^{10} + 0.0604672u^9 + \dots + 2.38705u - 0.0990538 \\ -0.191455u^{10} - 0.00295683u^9 + \dots - 0.937020u - 0.689533 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.164548u^{10} - 0.0295683u^9 + \dots - 0.370195u + 0.604672 \\ 0.0201064u^{10} - 0.0363690u^9 + \dots + 0.324660u + 0.318746 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.178888u^{10} + 0.0368125u^9 + \dots - 0.609107u + 0.384684 \\ -0.175636u^{10} + 0.00887049u^9 + \dots - 1.68894u - 0.931402 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.184654u^{10} + 0.00680071u^9 + \dots - 0.694855u + 0.285925 \\ -0.181402u^{10} - 0.0211413u^9 + \dots - 1.77469u - 1.03016 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{1322}{1691}u^{10} - \frac{750}{1691}u^9 - \frac{13061}{1691}u^8 + \frac{6124}{1691}u^7 + \frac{523}{19}u^6 - \frac{20067}{1691}u^5 - \frac{60106}{1691}u^4 + \frac{35628}{1691}u^3 - \frac{7299}{1691}u^2 + \frac{756}{1691}u - \frac{12564}{1691}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{11} - 2u^{10} + 7u^9 - 10u^8 + 17u^7 - 19u^6 + 14u^5 - 18u^4 - 6u^2 - 6u - 1$
$c_2$	$u^{11} + 10u^{10} + \dots + 24u - 1$
$c_3, c_4, c_8$ $c_9$	$u^{11} - u^{10} - 10u^9 + 9u^8 + 37u^7 - 31u^6 - 54u^5 + 48u^4 + 8u^3 - 4u - 4$
$c_6$	$u^{11} + 2u^{10} + \dots - 90u - 13$
$c_7, c_{11}$	$u^{11} + 3u^{10} + \dots - u - 7$
$c_{10}$	$u^{11} + 23u^{10} + \dots + 225u + 49$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{11} + 10y^{10} + \dots + 24y - 1$
$c_2$	$y^{11} - 14y^{10} + \dots + 432y - 1$
$c_3, c_4, c_8$ $c_9$	$y^{11} - 21y^{10} + \dots + 16y - 16$
$c_6$	$y^{11} - 38y^{10} + \dots + 4460y - 169$
$c_7, c_{11}$	$y^{11} - 23y^{10} + \dots + 225y - 49$
$c_{10}$	$y^{11} - 63y^{10} + \dots - 61879y - 2401$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.927671 + 0.197201I$ $a = -0.182641 + 0.461344I$ $b = 0.723376 - 0.590700I$	$-3.55618 + 2.69456I$	$-12.98158 - 3.53797I$
$u = 0.927671 - 0.197201I$ $a = -0.182641 - 0.461344I$ $b = 0.723376 + 0.590700I$	$-3.55618 - 2.69456I$	$-12.98158 + 3.53797I$
$u = 1.36751$ $a = -1.06580$ $b = -1.10452$	$-6.50002$	$-13.6590$
$u = -0.128515 + 0.466174I$ $a = 1.31999 + 0.78489I$ $b = -0.333924 - 0.361452I$	$-0.58979 + 1.50760I$	$-5.46704 - 3.06669I$
$u = -0.128515 - 0.466174I$ $a = 1.31999 - 0.78489I$ $b = -0.333924 + 0.361452I$	$-0.58979 - 1.50760I$	$-5.46704 + 3.06669I$
$u = -0.464364$ $a = 0.318779$ $b = 0.568678$	$-0.828081$	$-11.8310$
$u = -1.75254 + 0.61261I$ $a = -0.637478 - 0.443047I$ $b = -1.97688 - 0.71300I$	$-12.58100 + 1.38651I$	$-13.48038 - 0.69811I$
$u = -1.75254 - 0.61261I$ $a = -0.637478 + 0.443047I$ $b = -1.97688 + 0.71300I$	$-12.58100 - 1.38651I$	$-13.48038 + 0.69811I$
$u = 2.03058 + 0.31596I$ $a = 1.212210 - 0.346594I$ $b = 2.21938 + 0.57715I$	$13.7044 - 7.4448I$	$-12.73851 + 2.77525I$
$u = 2.03058 - 0.31596I$ $a = 1.212210 + 0.346594I$ $b = 2.21938 - 0.57715I$	$13.7044 + 7.4448I$	$-12.73851 - 2.77525I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -2.05754$		
$a = 1.32286$	18.3080	-11.1750
$b = 2.27195$		

$$\text{II. } I_2^u = \langle b + 1, 2a^2 - au + 4a - u + 3, u^2 - 2 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -au + a - \frac{1}{2}u + 1 \\ -au \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a - 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a - 2 \\ -2a - 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4au + 4u - 16$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$(u^2 - u + 1)^2$
$c_2, c_5$	$(u^2 + u + 1)^2$
$c_3, c_4, c_8$ $c_9$	$(u^2 - 2)^2$
$c_7$	$(u + 1)^4$
$c_{10}, c_{11}$	$(u - 1)^4$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$(y^2 + y + 1)^2$
$c_3, c_4, c_8$ $c_9$	$(y - 2)^4$
$c_7, c_{10}, c_{11}$	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$ $a = -0.646447 + 0.612372I$ $b = -1.00000$	$-6.57974 - 2.02988I$	$-14.0000 + 3.4641I$
$u = 1.41421$ $a = -0.646447 - 0.612372I$ $b = -1.00000$	$-6.57974 + 2.02988I$	$-14.0000 - 3.4641I$
$u = -1.41421$ $a = -1.35355 + 0.61237I$ $b = -1.00000$	$-6.57974 + 2.02988I$	$-14.0000 - 3.4641I$
$u = -1.41421$ $a = -1.35355 - 0.61237I$ $b = -1.00000$	$-6.57974 - 2.02988I$	$-14.0000 + 3.4641I$

$$\text{III. } I_1^v = \langle a, b - 1, v^2 + v + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v \\ -v \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v + 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4v - 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_6$	$u^2 + u + 1$
$c_3, c_4, c_8$ $c_9$	$u^2$
$c_5$	$u^2 - u + 1$
$c_7, c_{10}$	$(u - 1)^2$
$c_{11}$	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$y^2 + y + 1$
$c_3, c_4, c_8$ $c_9$	$y^2$
$c_7, c_{10}, c_{11}$	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.500000 + 0.866025I$ $a = 0$ $b = 1.00000$	$-1.64493 + 2.02988I$	$-12.00000 - 3.46410I$
$v = -0.500000 - 0.866025I$ $a = 0$ $b = 1.00000$	$-1.64493 - 2.02988I$	$-12.00000 + 3.46410I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)^2(u^2 + u + 1)$ $\cdot (u^{11} - 2u^{10} + 7u^9 - 10u^8 + 17u^7 - 19u^6 + 14u^5 - 18u^4 - 6u^2 - 6u - 1)$
$c_2$	$((u^2 + u + 1)^3)(u^{11} + 10u^{10} + \dots + 24u - 1)$
$c_3, c_4, c_8$ $c_9$	$u^2(u^2 - 2)^2$ $\cdot (u^{11} - u^{10} - 10u^9 + 9u^8 + 37u^7 - 31u^6 - 54u^5 + 48u^4 + 8u^3 - 4u - 4)$
$c_5$	$(u^2 - u + 1)(u^2 + u + 1)^2$ $\cdot (u^{11} - 2u^{10} + 7u^9 - 10u^8 + 17u^7 - 19u^6 + 14u^5 - 18u^4 - 6u^2 - 6u - 1)$
$c_6$	$((u^2 - u + 1)^2)(u^2 + u + 1)(u^{11} + 2u^{10} + \dots - 90u - 13)$
$c_7$	$((u - 1)^2)(u + 1)^4(u^{11} + 3u^{10} + \dots - u - 7)$
$c_{10}$	$((u - 1)^6)(u^{11} + 23u^{10} + \dots + 225u + 49)$
$c_{11}$	$((u - 1)^4)(u + 1)^2(u^{11} + 3u^{10} + \dots - u - 7)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$((y^2 + y + 1)^3)(y^{11} + 10y^{10} + \dots + 24y - 1)$
$c_2$	$((y^2 + y + 1)^3)(y^{11} - 14y^{10} + \dots + 432y - 1)$
$c_3, c_4, c_8$ $c_9$	$y^2(y - 2)^4(y^{11} - 21y^{10} + \dots + 16y - 16)$
$c_6$	$((y^2 + y + 1)^3)(y^{11} - 38y^{10} + \dots + 4460y - 169)$
$c_7, c_{11}$	$((y - 1)^6)(y^{11} - 23y^{10} + \dots + 225y - 49)$
$c_{10}$	$((y - 1)^6)(y^{11} - 63y^{10} + \dots - 61879y - 2401)$