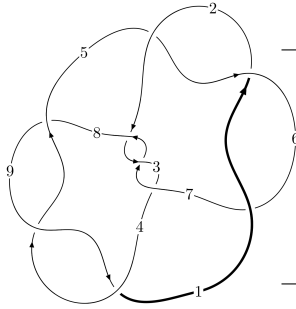
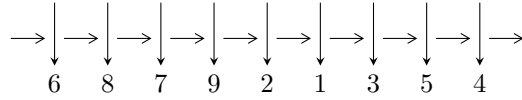


9₃₅ (K9a₄₀)

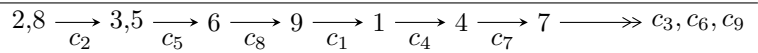


A knot diagram¹

Linearized knot diagram



Solving Sequence



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle b - u, a - 1, u^3 - u^2 + 3u - 1 \rangle$$

$$I_2^u = \langle b - u, -u^3 + a - 2u + 1, u^4 + u^3 + 3u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle u^3 - u^2 + b + 2u - 1, u^3 + 2a + u + 1, u^4 - 2u^3 + 3u^2 - 3u + 2 \rangle$$

$$I_4^u = \langle u^3 + u^2 + b + 3u + 1, a - 1, u^4 + u^3 + 3u^2 + 2u + 1 \rangle$$

$$I_5^u = \langle b + u, a + 1, u^2 + 1 \rangle$$

* 5 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 17 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b - u, a - 1, u^3 - u^2 + 3u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u + 1 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^2 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - u + 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ -2u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^2 - 2u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^2 - 2u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-6u^2 + 6u - 18$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------|--------------------------------|
| c_1, c_2, c_3 | $u^3 + u^2 + 3u + 1$ |
| c_4, c_5, c_6 | |
| c_7, c_8, c_9 | |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------|------------------------------------|
| c_1, c_2, c_3 | $y^3 + 5y^2 + 7y - 1$ |
| c_4, c_5, c_6 | |
| c_7, c_8, c_9 | |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.361103$ $a = 1.00000$ $b = 0.361103$ | -0.595615 | -16.6160 |
| $u = 0.31945 + 1.63317I$ $a = 1.00000$ $b = 0.31945 + 1.63317I$ | $17.5696 - 7.9406I$ | $-0.69212 + 3.53846I$ |
| $u = 0.31945 - 1.63317I$ $a = 1.00000$ $b = 0.31945 - 1.63317I$ | $17.5696 + 7.9406I$ | $-0.69212 - 3.53846I$ |

$$\text{II. } I_2^u = \langle b - u, -u^3 + a - 2u + 1, u^4 + u^3 + 3u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 + 2u - 1 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3 + u - 1 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^3 - 2u^2 - 5u - 3 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 + 2u^2 + 3u + 2 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ -u^3 - u^2 - 2u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^3 - 4u^2 - 12u - 10$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------------------------|--------------------------------|
| c_1, c_2, c_3 c_5, c_6, c_7 | $u^4 - u^3 + 3u^2 - 2u + 1$ |
| c_4, c_8, c_9 | $u^4 + 2u^3 + 3u^2 + 3u + 2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|------------------------------------|------------------------------------|
| c_1, c_2, c_3 c_5, c_6, c_7 | $y^4 + 5y^3 + 7y^2 + 2y + 1$ |
| c_4, c_8, c_9 | $y^4 + 2y^3 + y^2 + 3y + 4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.395123 + 0.506844I$ $a = -1.54742 + 1.12087I$ $b = -0.395123 + 0.506844I$ | $3.07886 + 1.41510I$ | $-5.82674 - 4.90874I$ |
| $u = -0.395123 - 0.506844I$ $a = -1.54742 - 1.12087I$ $b = -0.395123 - 0.506844I$ | $3.07886 - 1.41510I$ | $-5.82674 + 4.90874I$ |
| $u = -0.10488 + 1.55249I$ $a = -0.452576 - 0.585652I$ $b = -0.10488 + 1.55249I$ | $10.08060 + 3.16396I$ | $-2.17326 - 2.56480I$ |
| $u = -0.10488 - 1.55249I$ $a = -0.452576 + 0.585652I$ $b = -0.10488 - 1.55249I$ | $10.08060 - 3.16396I$ | $-2.17326 + 2.56480I$ |

$$\text{III. } I_3^u = \langle u^3 - u^2 + b + 2u - 1, u^3 + 2a + u + 1, u^4 - 2u^3 + 3u^2 - 3u + 2 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{2}u^3 - \frac{1}{2}u - \frac{1}{2} \\ -u^3 + u^2 - 2u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^3 - u^2 + \frac{3}{2}u - \frac{3}{2} \\ -u^3 + u^2 - 2u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{3}{2}u^3 + 2u^2 - \frac{5}{2}u + \frac{5}{2} \\ -u^3 + 2u^2 - u + 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{2}u^3 - \frac{1}{2}u + \frac{1}{2} \\ -u^3 + 2u^2 - 2u + 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ 2u^3 - u^2 + 3u - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $4u - 6$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------------------------|--------------------------------|
| c_1, c_4, c_5 c_6, c_8, c_9 | $u^4 - u^3 + 3u^2 - 2u + 1$ |
| c_2, c_3, c_7 | $u^4 + 2u^3 + 3u^2 + 3u + 2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|------------------------------------|------------------------------------|
| c_1, c_4, c_5 c_6, c_8, c_9 | $y^4 + 5y^3 + 7y^2 + 2y + 1$ |
| c_2, c_3, c_7 | $y^4 + 2y^3 + y^2 + 3y + 4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.956685 + 0.641200I$ $a = -0.826150 - 1.069070I$ $b = -0.10488 - 1.55249I$ | $10.08060 - 3.16396I$ | $-2.17326 + 2.56480I$ |
| $u = 0.956685 - 0.641200I$ $a = -0.826150 + 1.069070I$ $b = -0.10488 + 1.55249I$ | $10.08060 + 3.16396I$ | $-2.17326 - 2.56480I$ |
| $u = 0.043315 + 1.227190I$ $a = -0.423850 + 0.307015I$ $b = -0.395123 - 0.506844I$ | $3.07886 - 1.41510I$ | $-5.82674 + 4.90874I$ |
| $u = 0.043315 - 1.227190I$ $a = -0.423850 - 0.307015I$ $b = -0.395123 + 0.506844I$ | $3.07886 + 1.41510I$ | $-5.82674 - 4.90874I$ |

$$\text{IV. } I_4^u = \langle u^3 + u^2 + b + 3u + 1, a - 1, u^4 + u^3 + 3u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^3 - u^2 - 3u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3 + u^2 + 3u + 2 \\ -u^3 - u^2 - 3u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 + 2u \\ u^2 + u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ -u^3 - u^2 - 2u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^3 - 4u^2 - 12u - 10$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------------------------|--------------------------------|
| c_1, c_5, c_6 | $u^4 + 2u^3 + 3u^2 + 3u + 2$ |
| c_2, c_3, c_4 c_7, c_8, c_9 | $u^4 - u^3 + 3u^2 - 2u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|------------------------------------|------------------------------------|
| c_1, c_5, c_6 | $y^4 + 2y^3 + y^2 + 3y + 4$ |
| c_2, c_3, c_4 c_7, c_8, c_9 | $y^4 + 5y^3 + 7y^2 + 2y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.395123 + 0.506844I$ $a = 1.00000$ $b = 0.043315 - 1.227190I$ | $3.07886 + 1.41510I$ | $-5.82674 - 4.90874I$ |
| $u = -0.395123 - 0.506844I$ $a = 1.00000$ $b = 0.043315 + 1.227190I$ | $3.07886 - 1.41510I$ | $-5.82674 + 4.90874I$ |
| $u = -0.10488 + 1.55249I$ $a = 1.00000$ $b = 0.956685 - 0.641200I$ | $10.08060 + 3.16396I$ | $-2.17326 - 2.56480I$ |
| $u = -0.10488 - 1.55249I$ $a = 1.00000$ $b = 0.956685 + 0.641200I$ | $10.08060 - 3.16396I$ | $-2.17326 + 2.56480I$ |

$$\mathbf{V. } I_5^u = \langle b + u, a + 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u - 1 \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------|--------------------------------|
| c_1, c_2, c_3 | $u^2 + 1$ |
| c_4, c_5, c_6 | |
| c_7, c_8, c_9 | |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------|------------------------------------|
| c_1, c_2, c_3 | |
| c_4, c_5, c_6 | $(y + 1)^2$ |
| c_7, c_8, c_9 | |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_5^u | | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|--------------|---------------------------------------|------------|
| $u =$ | $1.000000I$ | 4.93480 | 0 |
| $a =$ | -1.00000 | | |
| $b =$ | $-1.000000I$ | | |
| $u =$ | $-1.000000I$ | 4.93480 | 0 |
| $a =$ | -1.00000 | | |
| $b =$ | $1.000000I$ | | |

VI. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---|--|
| c_1, c_2, c_3 c_4, c_5, c_6 c_7, c_8, c_9 | $(u^2 + 1)(u^3 + u^2 + 3u + 1)(u^4 - u^3 + 3u^2 - 2u + 1)^2$ $\cdot (u^4 + 2u^3 + 3u^2 + 3u + 2)$ |

VII. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|---|---|
| c_1, c_2, c_3 c_4, c_5, c_6 c_7, c_8, c_9 | $(y + 1)^2(y^3 + 5y^2 + 7y - 1)(y^4 + 2y^3 + y^2 + 3y + 4)$ $\cdot (y^4 + 5y^3 + 7y^2 + 2y + 1)^2$ |