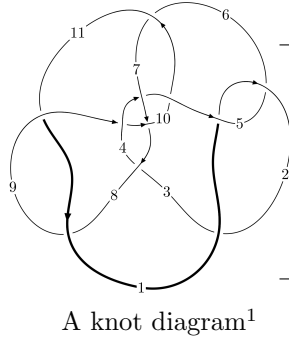
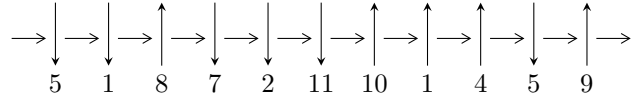


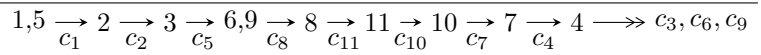
11n<sub>96</sub> (K11n<sub>96</sub>)



**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$\begin{aligned}
 I_1^u &= \langle -49163590906u^{11} + 107218013353u^{10} + \dots + 21229569666128b + 7549955391253, \\
 &\quad - 3432579931219u^{11} + 9265624647069u^{10} + \dots + 891641925977376a + 779226085539559, \\
 &\quad u^{12} - 18u^{10} - 3u^9 + 95u^8 + 104u^7 + 172u^6 - 39u^5 - 97u^4 - 126u^3 + 90u^2 + 56u + 21 \rangle \\
 I_2^u &= \langle u^4 + 2u^3 + b, 2u^4 + 4u^3 + u^2 + a + 3u, u^5 + 3u^4 + 3u^3 + 3u^2 + 2u + 1 \rangle \\
 I_3^u &= \langle -2a^3 - a^2 + b - 5a + 3, a^4 + 2a^2 - 3a + 1, u - 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 21 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -4.92 \times 10^{10}u^{11} + 1.07 \times 10^{11}u^{10} + \dots + 2.12 \times 10^{13}b + 7.55 \times 10^{12}, -3.43 \times 10^{12}u^{11} + 9.27 \times 10^{12}u^{10} + \dots + 8.92 \times 10^{14}a + 7.79 \times 10^{14}, u^{12} - 18u^{10} + \dots + 56u + 21 \rangle$$

**(i) Arc colorings**

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.00384973u^{11} - 0.0103916u^{10} + \dots + 0.0171393u - 0.873923 \\ 0.00231581u^{11} - 0.00505041u^{10} + \dots + 0.944426u - 0.355634 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.00153392u^{11} - 0.00534123u^{10} + \dots - 0.927287u - 0.518289 \\ 0.00231581u^{11} - 0.00505041u^{10} + \dots + 0.944426u - 0.355634 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.00463890u^{11} + 0.00727890u^{10} + \dots - 0.777940u + 1.33085 \\ -0.00697735u^{11} + 0.00595506u^{10} + \dots - 0.776534u + 0.0957645 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.00463890u^{11} + 0.00727890u^{10} + \dots - 0.777940u + 1.33085 \\ -0.00382620u^{11} + 0.00729647u^{10} + \dots - 0.466333u + 0.248621 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0229677u^{11} + 0.00971661u^{10} + \dots - 4.00235u - 0.352817 \\ -0.00186562u^{11} - 0.00155113u^{10} + \dots + 0.277243u - 0.308445 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.00384973u^{11} + 0.0103916u^{10} + \dots - 0.0171393u + 0.873923 \\ 0.00382620u^{11} - 0.00729647u^{10} + \dots + 0.466333u - 0.248621 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.00384973u^{11} + 0.0103916u^{10} + \dots - 0.0171393u + 0.873923 \\ 0.00382620u^{11} - 0.00729647u^{10} + \dots + 0.466333u - 0.248621 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes**

$$= \frac{6189983418965}{84918278664512}u^{11} + \frac{1650234375373}{84918278664512}u^{10} + \dots + \frac{95722121856831}{84918278664512}u + \frac{414947504713599}{84918278664512}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{12} - 18u^{10} + \dots - 56u + 21$
$c_2$	$u^{12} + 36u^{11} + \dots - 644u + 441$
$c_3$	$u^{12} + 43u^{10} + \dots - 242u + 713$
$c_4$	$u^{12} - 3u^{11} + 4u^{10} - u^9 + u^8 - 6u^7 + 8u^6 + u^5 - 5u^4 - u^3 + 4u^2 - 3u + 1$
$c_6$	$u^{12} + 2u^{11} + \dots + 211u + 199$
$c_7$	$u^{12} + 4u^{11} + \dots - 56u + 48$
$c_8, c_{11}$	$u^{12} + 2u^{11} + \dots - 2u + 1$
$c_9$	$u^{12} + 9u^{11} + \dots + 32u + 8$
$c_{10}$	$u^{12} - u^{11} + \dots - u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{12} - 36y^{11} + \dots + 644y + 441$
$c_2$	$y^{12} - 268y^{11} + \dots + 15582980y + 194481$
$c_3$	$y^{12} + 86y^{11} + \dots - 2050686y + 508369$
$c_4$	$y^{12} - y^{11} + \dots - y + 1$
$c_6$	$y^{12} - 50y^{11} + \dots - 181433y + 39601$
$c_7$	$y^{12} + 14y^{11} + \dots + 19136y + 2304$
$c_8, c_{11}$	$y^{12} + 30y^{11} + \dots - 34y + 1$
$c_9$	$y^{12} - 5y^{11} + \dots - 160y + 64$
$c_{10}$	$y^{12} - 31y^{11} + \dots + 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.695715 + 0.738682I$		
$a = 0.84389 - 1.18718I$	$0.40587 + 4.64089I$	$1.41872 - 4.81790I$
$b = -0.353721 - 0.071932I$		
$u = -0.695715 - 0.738682I$		
$a = 0.84389 + 1.18718I$	$0.40587 - 4.64089I$	$1.41872 + 4.81790I$
$b = -0.353721 + 0.071932I$		
$u = 0.778147 + 0.299444I$		
$a = -0.811194 - 0.475700I$	$-1.39285 - 0.48352I$	$-6.04456 + 0.14475I$
$b = 0.333912 - 0.014682I$		
$u = 0.778147 - 0.299444I$		
$a = -0.811194 + 0.475700I$	$-1.39285 + 0.48352I$	$-6.04456 - 0.14475I$
$b = 0.333912 + 0.014682I$		
$u = -0.182826 + 1.285270I$		
$a = 0.012072 + 0.419952I$	$-4.09909 - 2.92553I$	$-6.51732 + 0.13616I$
$b = -0.18796 + 1.60199I$		
$u = -0.182826 - 1.285270I$		
$a = 0.012072 - 0.419952I$	$-4.09909 + 2.92553I$	$-6.51732 - 0.13616I$
$b = -0.18796 - 1.60199I$		
$u = -0.246048 + 0.302553I$		
$a = -0.835828 - 0.015119I$	$1.34063 - 0.78648I$	$4.38906 + 1.25430I$
$b = -0.578983 + 0.267705I$		
$u = -0.246048 - 0.302553I$		
$a = -0.835828 + 0.015119I$	$1.34063 + 0.78648I$	$4.38906 - 1.25430I$
$b = -0.578983 - 0.267705I$		
$u = -3.01586 + 0.46060I$		
$a = -0.161563 + 0.704724I$	$18.0497 + 1.3274I$	$-3.03771 + 0.06650I$
$b = 0.81768 + 2.58567I$		
$u = -3.01586 - 0.46060I$		
$a = -0.161563 - 0.704724I$	$18.0497 - 1.3274I$	$-3.03771 - 0.06650I$
$b = 0.81768 - 2.58567I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 3.36230 + 0.99651I$	$17.7719 - 9.0470I$	$-3.20819 + 3.73893I$
$a = -0.214046 - 0.589764I$		
$b = 0.96907 - 2.80816I$		
$u = 3.36230 - 0.99651I$	$17.7719 + 9.0470I$	$-3.20819 - 3.73893I$
$a = -0.214046 + 0.589764I$		
$b = 0.96907 + 2.80816I$		

## II.

$$I_2^u = \langle u^4 + 2u^3 + b, 2u^4 + 4u^3 + u^2 + a + 3u, u^5 + 3u^4 + 3u^3 + 3u^2 + 2u + 1 \rangle$$

### (i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^4 - 4u^3 - u^2 - 3u \\ -u^4 - 2u^3 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^4 - 2u^3 - u^2 - 3u \\ -u^4 - 2u^3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^4 - 3u^3 - 2u^2 - u - 1 \\ u^4 + 3u^3 + 3u^2 + 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^4 - 3u^3 - 2u^2 - u - 1 \\ u^3 + 2u^2 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 + 2u^2 + u + 2 \\ u^4 + 3u^3 + 4u^2 + 2u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2u^4 + 4u^3 + u^2 + 3u \\ -u^3 - 2u^2 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2u^4 + 4u^3 + u^2 + 3u \\ -u^3 - 2u^2 - u \end{pmatrix}$$

### (ii) Obstruction class = 1

$$(iii) \text{ Cusp Shapes} = -10u^4 - 25u^3 - 19u^2 - 24u - 15$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^5 + 3u^4 + 3u^3 + 3u^2 + 2u + 1$
$c_2$	$u^5 + 3u^4 - 5u^3 + 3u^2 - 2u + 1$
$c_3$	$u^5 - u^4 - 2u^3 + 9u^2 - 17u + 11$
$c_4$	$u^5 - 2u^4 + 2u^3 + u^2 - 2u + 1$
$c_5$	$u^5 - 3u^4 + 3u^3 - 3u^2 + 2u - 1$
$c_6$	$u^5 + 3u^4 - 5u^3 - 8u^2 + 9u + 11$
$c_7$	$u^5 + u^4 - 2u^3 + 3u^2 + 7u + 13$
$c_8$	$u^5 - u^4 + 3u^3 - 3u^2 + 2u - 1$
$c_9$	$u^5 - u^3 + u^2 + u - 1$
$c_{10}$	$u^5 + u^4 - u^3 - u^2 + 1$
$c_{11}$	$u^5 + u^4 + 3u^3 + 3u^2 + 2u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^5 - 3y^4 - 5y^3 - 3y^2 - 2y - 1$
$c_2$	$y^5 - 19y^4 + 3y^3 + 5y^2 - 2y - 1$
$c_3$	$y^5 - 5y^4 - 12y^3 + 9y^2 + 91y - 121$
$c_4$	$y^5 + 4y^3 - 5y^2 + 2y - 1$
$c_6$	$y^5 - 19y^4 + 91y^3 - 220y^2 + 257y - 121$
$c_7$	$y^5 - 5y^4 + 12y^3 - 63y^2 - 29y - 169$
$c_8, c_{11}$	$y^5 + 5y^4 + 7y^3 + y^2 - 2y - 1$
$c_9$	$y^5 - 2y^4 + 3y^3 - 3y^2 + 3y - 1$
$c_{10}$	$y^5 - 3y^4 + 3y^3 - 3y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.128506 + 0.862169I$	$-3.58220 + 3.70382I$	$-1.95503 - 6.72693I$
$a = 0.520756 + 0.228796I$		
$b = 0.08973 + 1.51845I$		
$u = 0.128506 - 0.862169I$	$-3.58220 - 3.70382I$	$-1.95503 + 6.72693I$
$a = 0.520756 - 0.228796I$		
$b = 0.08973 - 1.51845I$		
$u = -0.586994 + 0.535944I$	$-0.27969 + 5.17259I$	$-5.66442 - 10.18801I$
$a = 1.27460 - 2.43458I$		
$b = -0.214528 - 0.727972I$		
$u = -0.586994 - 0.535944I$	$-0.27969 - 5.17259I$	$-5.66442 + 10.18801I$
$a = 1.27460 + 2.43458I$		
$b = -0.214528 + 0.727972I$		
$u = -2.08302$	$-5.43570$	$-9.76110$
$a = 0.409288$		
$b = -0.750397$		

$$\text{III. } I_3^u = \langle -2a^3 - a^2 + b - 5a + 3, a^4 + 2a^2 - 3a + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 2a^3 + a^2 + 5a - 3 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2a^3 - a^2 - 4a + 3 \\ 2a^3 + a^2 + 5a - 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^3 + a^2 + 3a - 1 \\ 2a^3 + a^2 + 5a - 4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^3 + a^2 + 3a - 1 \\ a^3 + 2a - 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2a^3 - a^2 - 4a + 3 \\ 2a^3 + a^2 + 5a - 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -a \\ -a^3 - 2a + 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -a \\ -a^3 - 2a + 3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5a^3 - a^2 - 11a + 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^4$
$c_2, c_5$	$(u + 1)^4$
$c_3, c_4$	$u^4 - 2u^3 + 2u^2 - u + 1$
$c_6, c_{11}$	$(u^2 - u + 1)^2$
$c_7$	$u^4$
$c_8$	$(u^2 + u + 1)^2$
$c_9, c_{10}$	$u^4 - u^3 - u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^4$
$c_3, c_4$	$y^4 + 2y^2 + 3y + 1$
$c_6, c_8, c_{11}$	$(y^2 + y + 1)^2$
$c_7$	$y^4$
$c_9, c_{10}$	$y^4 - 3y^3 + 5y^2 - 3y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0.570696 + 0.107280I$	$-1.64493 + 2.02988I$	$-1.42268 - 1.82047I$
$b = 0.500000 + 0.866025I$		
$u = 1.00000$		
$a = 0.570696 - 0.107280I$	$-1.64493 - 2.02988I$	$-1.42268 + 1.82047I$
$b = 0.500000 - 0.866025I$		
$u = 1.00000$		
$a = -0.57070 + 1.62477I$	$-1.64493 + 2.02988I$	$-7.07732 - 2.50966I$
$b = 0.500000 + 0.866025I$		
$u = 1.00000$		
$a = -0.57070 - 1.62477I$	$-1.64493 - 2.02988I$	$-7.07732 + 2.50966I$
$b = 0.500000 - 0.866025I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^4)(u^5 + 3u^4 + \dots + 2u + 1)(u^{12} - 18u^{10} + \dots - 56u + 21)$
$c_2$	$(u+1)^4(u^5 + 3u^4 - 5u^3 + 3u^2 - 2u + 1)$ $\cdot (u^{12} + 36u^{11} + \dots - 644u + 441)$
$c_3$	$(u^4 - 2u^3 + 2u^2 - u + 1)(u^5 - u^4 - 2u^3 + 9u^2 - 17u + 11)$ $\cdot (u^{12} + 43u^{10} + \dots - 242u + 713)$
$c_4$	$(u^4 - 2u^3 + 2u^2 - u + 1)(u^5 - 2u^4 + 2u^3 + u^2 - 2u + 1)$ $\cdot (u^{12} - 3u^{11} + 4u^{10} - u^9 + u^8 - 6u^7 + 8u^6 + u^5 - 5u^4 - u^3 + 4u^2 - 3u + 1)$
$c_5$	$((u+1)^4)(u^5 - 3u^4 + \dots + 2u - 1)(u^{12} - 18u^{10} + \dots - 56u + 21)$
$c_6$	$(u^2 - u + 1)^2(u^5 + 3u^4 - 5u^3 - 8u^2 + 9u + 11)$ $\cdot (u^{12} + 2u^{11} + \dots + 211u + 199)$
$c_7$	$u^4(u^5 + u^4 + \dots + 7u + 13)(u^{12} + 4u^{11} + \dots - 56u + 48)$
$c_8$	$((u^2 + u + 1)^2)(u^5 - u^4 + \dots + 2u - 1)(u^{12} + 2u^{11} + \dots - 2u + 1)$
$c_9$	$(u^4 - u^3 - u^2 + u + 1)(u^5 - u^3 + u^2 + u - 1)(u^{12} + 9u^{11} + \dots + 32u + 8)$
$c_{10}$	$(u^4 - u^3 - u^2 + u + 1)(u^5 + u^4 - u^3 - u^2 + 1)(u^{12} - u^{11} + \dots - u + 1)$
$c_{11}$	$((u^2 - u + 1)^2)(u^5 + u^4 + \dots + 2u + 1)(u^{12} + 2u^{11} + \dots - 2u + 1)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$(y-1)^4(y^5 - 3y^4 - 5y^3 - 3y^2 - 2y - 1)$ $\cdot (y^{12} - 36y^{11} + \dots + 644y + 441)$
$c_2$	$(y-1)^4(y^5 - 19y^4 + 3y^3 + 5y^2 - 2y - 1)$ $\cdot (y^{12} - 268y^{11} + \dots + 15582980y + 194481)$
$c_3$	$(y^4 + 2y^2 + 3y + 1)(y^5 - 5y^4 - 12y^3 + 9y^2 + 91y - 121)$ $\cdot (y^{12} + 86y^{11} + \dots - 2050686y + 508369)$
$c_4$	$(y^4 + 2y^2 + 3y + 1)(y^5 + 4y^3 + \dots + 2y - 1)(y^{12} - y^{11} + \dots - y + 1)$
$c_6$	$(y^2 + y + 1)^2(y^5 - 19y^4 + 91y^3 - 220y^2 + 257y - 121)$ $\cdot (y^{12} - 50y^{11} + \dots - 181433y + 39601)$
$c_7$	$y^4(y^5 - 5y^4 + 12y^3 - 63y^2 - 29y - 169)$ $\cdot (y^{12} + 14y^{11} + \dots + 19136y + 2304)$
$c_8, c_{11}$	$(y^2 + y + 1)^2(y^5 + 5y^4 + 7y^3 + y^2 - 2y - 1)$ $\cdot (y^{12} + 30y^{11} + \dots - 34y + 1)$
$c_9$	$(y^4 - 3y^3 + 5y^2 - 3y + 1)(y^5 - 2y^4 + 3y^3 - 3y^2 + 3y - 1)$ $\cdot (y^{12} - 5y^{11} + \dots - 160y + 64)$
$c_{10}$	$(y^4 - 3y^3 + 5y^2 - 3y + 1)(y^5 - 3y^4 + 3y^3 - 3y^2 + 2y - 1)$ $\cdot (y^{12} - 31y^{11} + \dots + 5y + 1)$