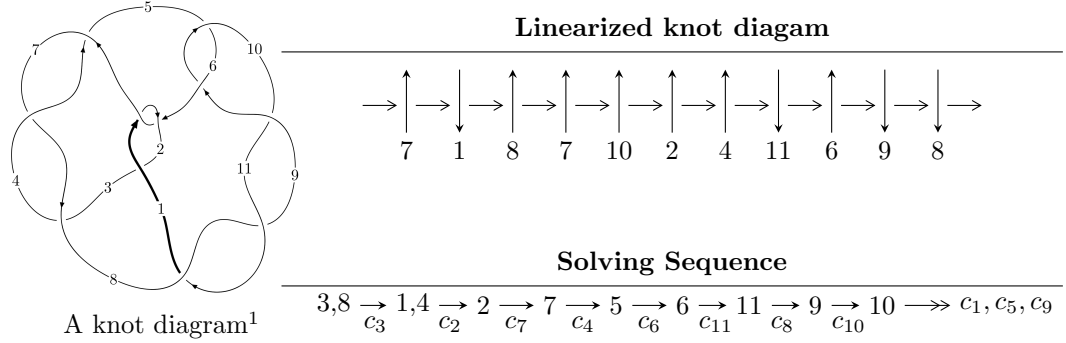


11n<sub>101</sub> (K11n<sub>101</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^2 + b, -u^{12} + u^{11} + u^9 - 8u^8 + 6u^7 + 5u^6 + 2u^5 - 18u^4 + 5u^3 + 15u^2 + 8a + u - 9, \\ u^{13} + u^{11} - u^{10} + 7u^9 + 3u^7 - 5u^6 + 8u^5 + u^4 + 4u^3 - 2u^2 - 1 \rangle$$

$$I_2^u = \langle -201u^{11} - 132u^{10} + \dots + 281b + 62, 247u^{11} + 28u^{10} + \dots + 281a + 72, \\ u^{12} + u^{11} + 2u^{10} + 2u^9 + 5u^8 + 5u^7 + 13u^6 + 11u^5 + 15u^4 + 11u^3 + 8u^2 + 4u + 1 \rangle$$

$$I_3^u = \langle b + 1, a^3 - a^2u - 2a + u, u^2 + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 31 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^2 + b, -u^{12} + u^{11} + \dots + 8a - 9, u^{13} + u^{11} + \dots - 2u^2 - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} \frac{1}{8}u^{12} - \frac{1}{8}u^{11} + \dots - \frac{1}{8}u + \frac{9}{8} \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{1}{8}u^{12} - \frac{1}{8}u^{11} + \dots - \frac{1}{8}u + \frac{9}{8} \\ -u^4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} \frac{1}{8}u^{12} + \frac{1}{8}u^{11} + \dots - \frac{17}{8}u - \frac{1}{8} \\ u^5 + u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{1}{8}u^{12} - \frac{1}{8}u^{11} + \dots - \frac{1}{8}u + \frac{9}{8} \\ \frac{1}{8}u^{12} - \frac{1}{8}u^{11} + \dots - \frac{1}{8}u + \frac{1}{8} \end{pmatrix} \\ a_9 &= \begin{pmatrix} \frac{7}{8}u^{12} + \frac{3}{8}u^{11} + \dots - \frac{17}{8}u - \frac{5}{8} \\ \frac{1}{2}u^{12} + \frac{1}{4}u^{10} + \dots + \frac{1}{4}u - \frac{1}{4} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{1}{8}u^{12} + \frac{9}{8}u^{11} + \dots + \frac{7}{8}u - \frac{13}{8} \\ \frac{7}{8}u^{12} - \frac{13}{8}u^{11} + \dots - \frac{13}{8}u - \frac{13}{8} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{1}{8}u^{12} + \frac{9}{8}u^{11} + \dots + \frac{7}{8}u - \frac{13}{8} \\ \frac{7}{8}u^{12} - \frac{13}{8}u^{11} + \dots - \frac{13}{8}u - \frac{13}{8} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 4u^{12} + \frac{7}{2}u^{10} - \frac{7}{2}u^9 + \frac{55}{2}u^8 + u^7 + \frac{15}{2}u^6 - 16u^5 + 30u^4 + 9u^3 + 5u^2 - \frac{1}{2}u + \frac{5}{2}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$u^{13} + u^{11} - u^{10} + 7u^9 + 3u^7 - 5u^6 + 8u^5 + u^4 + 4u^3 - 2u^2 - 1$
$c_2$	$u^{13} + 2u^{12} + \dots - 4u - 1$
$c_5, c_9$	$u^{13} - 3u^{12} + \dots + 5u - 2$
$c_8, c_{10}, c_{11}$	$u^{13} + 3u^{12} + \dots + 5u - 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$y^{13} + 2y^{12} + \dots - 4y - 1$
$c_2$	$y^{13} + 26y^{12} + \dots + 12y - 1$
$c_5, c_9$	$y^{13} + 3y^{12} + \dots + 5y - 4$
$c_8, c_{10}, c_{11}$	$y^{13} + 15y^{12} + \dots + 177y - 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.871545 + 0.665952I$ $a = -0.145280 - 0.753872I$ $b = 0.316099 + 1.160810I$	$2.81429 + 2.20167I$	$6.81300 - 2.37182I$
$u = 0.871545 - 0.665952I$ $a = -0.145280 + 0.753872I$ $b = 0.316099 - 1.160810I$	$2.81429 - 2.20167I$	$6.81300 + 2.37182I$
$u = -0.745925 + 0.860258I$ $a = -0.294264 + 1.109470I$ $b = -0.183640 - 1.283380I$	$1.03858 - 7.07395I$	$2.58380 + 8.11816I$
$u = -0.745925 - 0.860258I$ $a = -0.294264 - 1.109470I$ $b = -0.183640 + 1.283380I$	$1.03858 + 7.07395I$	$2.58380 - 8.11816I$
$u = -0.438163 + 0.579645I$ $a = 0.727972 + 1.025400I$ $b = -0.144001 - 0.507958I$	$-2.29540 - 1.46021I$	$-0.76105 + 4.77537I$
$u = -0.438163 - 0.579645I$ $a = 0.727972 - 1.025400I$ $b = -0.144001 + 0.507958I$	$-2.29540 + 1.46021I$	$-0.76105 - 4.77537I$
$u = 0.622206$ $a = 0.441815$ $b = 0.387141$	$0.957360$	$10.3810$
$u = -0.052177 + 0.598239I$ $a = 2.07278 + 0.29749I$ $b = -0.355168 - 0.062429I$	$1.24085 + 2.67797I$	$5.53095 - 2.23117I$
$u = -0.052177 - 0.598239I$ $a = 2.07278 - 0.29749I$ $b = -0.355168 + 0.062429I$	$1.24085 - 2.67797I$	$5.53095 + 2.23117I$
$u = -0.95082 + 1.19131I$ $a = -0.819335 + 0.844166I$ $b = -0.51516 - 2.26544I$	$10.8970 - 11.1670I$	$4.44754 + 6.34112I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.95082 - 1.19131I$		
$a = -0.819335 - 0.844166I$	$10.8970 + 11.1670I$	$4.44754 - 6.34112I$
$b = -0.51516 + 2.26544I$		
$u = 1.00444 + 1.14917I$		
$a = -0.762781 - 0.795622I$	$11.32250 + 4.40088I$	$5.19535 - 1.84237I$
$b = -0.31170 + 2.30854I$		
$u = 1.00444 - 1.14917I$		
$a = -0.762781 + 0.795622I$	$11.32250 - 4.40088I$	$5.19535 + 1.84237I$
$b = -0.31170 - 2.30854I$		

$$\text{II. } I_2^u = \langle -201u^{11} - 132u^{10} + \dots + 281b + 62, 247u^{11} + 28u^{10} + \dots + 281a + 72, u^{12} + u^{11} + \dots + 4u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.879004u^{11} - 0.0996441u^{10} + \dots - 4.62633u - 0.256228 \\ 0.715302u^{11} + 0.469751u^{10} + \dots + 2.23843u - 0.220641 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.59431u^{11} - 0.569395u^{10} + \dots - 6.86477u - 1.03559 \\ 1.23132u^{11} + 0.868327u^{10} + \dots + 4.74377u + 0.804270 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.754448u^{11} - 0.555160u^{10} + \dots - 4.91815u - 3.28470 \\ 0.661922u^{11} - 0.192171u^{10} + \dots + 0.220641u + 0.362989 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.879004u^{11} - 0.0996441u^{10} + \dots - 4.62633u - 0.256228 \\ 1.43060u^{11} + 0.939502u^{10} + \dots + 4.47687u + 0.558719 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1.77936u^{11} - 1.06406u^{10} + \dots - 10.2598u - 4.87900 \\ 1.27046u^{11} + 0.953737u^{10} + \dots + 6.42349u + 2.30961 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 - 1 \\ 1.43060u^{11} + 0.939502u^{10} + \dots + 4.47687u + 1.55872 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 - 1 \\ 1.43060u^{11} + 0.939502u^{10} + \dots + 4.47687u + 1.55872 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{212}{281}u^{11} + \frac{1280}{281}u^{10} + \frac{404}{281}u^9 + \frac{1208}{281}u^8 + \frac{1568}{281}u^7 + \frac{4548}{281}u^6 + \frac{3124}{281}u^5 + \frac{10520}{281}u^4 + \frac{2840}{281}u^3 + \frac{6608}{281}u^2 + \frac{1944}{281}u + \frac{1766}{281}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$u^{12} + u^{11} + \dots + 4u + 1$
$c_2$	$u^{12} + 3u^{11} + \dots + 6u^2 + 1$
$c_5, c_9$	$(u^6 + u^5 + u^4 + 2u^2 + u + 1)^2$
$c_8, c_{10}, c_{11}$	$(u^6 + u^5 + 5u^4 + 4u^3 + 6u^2 + 3u + 1)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$y^{12} + 3y^{11} + \dots + 6y^2 + 1$
$c_2$	$y^{12} + 11y^{11} + \dots + 12y + 1$
$c_5, c_9$	$(y^6 + y^5 + 5y^4 + 4y^3 + 6y^2 + 3y + 1)^2$
$c_8, c_{10}, c_{11}$	$(y^6 + 9y^5 + 29y^4 + 40y^3 + 22y^2 + 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.276186 + 0.937280I$ $a = 1.096930 + 0.475717I$ $b = 0.126264 - 0.186282I$	$1.35295 + 2.65597I$	$5.58115 - 3.39809I$
$u = 0.276186 - 0.937280I$ $a = 1.096930 - 0.475717I$ $b = 0.126264 + 0.186282I$	$1.35295 - 2.65597I$	$5.58115 + 3.39809I$
$u = -0.247920 + 0.814674I$ $a = -0.293452 + 0.484072I$ $b = -1.372270 + 0.172983I$	$-3.54796 - 1.10871I$	$0.46385 + 6.18117I$
$u = -0.247920 - 0.814674I$ $a = -0.293452 - 0.484072I$ $b = -1.372270 - 0.172983I$	$-3.54796 + 1.10871I$	$0.46385 - 6.18117I$
$u = -0.073688 + 1.173750I$ $a = 0.321857 + 0.253794I$ $b = -0.602229 + 0.403948I$	$-3.54796 + 1.10871I$	$0.46385 - 6.18117I$
$u = -0.073688 - 1.173750I$ $a = 0.321857 - 0.253794I$ $b = -0.602229 - 0.403948I$	$-3.54796 - 1.10871I$	$0.46385 + 6.18117I$
$u = -1.18584 + 0.84722I$ $a = 0.727937 - 0.977012I$ $b = 0.46202 + 2.13527I$	$12.06460 + 3.42721I$	$5.95500 - 2.25224I$
$u = -1.18584 - 0.84722I$ $a = 0.727937 + 0.977012I$ $b = 0.46202 - 2.13527I$	$12.06460 - 3.42721I$	$5.95500 + 2.25224I$
$u = 1.15037 + 0.92808I$ $a = 0.735494 + 0.949873I$ $b = 0.68843 - 2.00934I$	$12.06460 + 3.42721I$	$5.95500 - 2.25224I$
$u = 1.15037 - 0.92808I$ $a = 0.735494 - 0.949873I$ $b = 0.68843 + 2.00934I$	$12.06460 - 3.42721I$	$5.95500 + 2.25224I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.419110 + 0.222236I$	$1.35295 + 2.65597I$	$5.58115 - 3.39809I$
$a = 1.41124 - 2.01830I$		
$b = -0.802215 + 0.517727I$		
$u = -0.419110 - 0.222236I$	$1.35295 - 2.65597I$	$5.58115 + 3.39809I$
$a = 1.41124 + 2.01830I$		
$b = -0.802215 - 0.517727I$		

$$\text{III. } I_3^u = \langle b + 1, a^3 - a^2u - 2a + u, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} au \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ a - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -a^2u \\ -a^2u + au + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -a^2u - a + u \\ -a^2u + a^2 + u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -a^2u - a + u \\ -a^2u + a^2 + u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4a^2 - 4au - 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$(u^2 + 1)^3$
$c_2$	$(u + 1)^6$
$c_5, c_9$	$u^6 + u^4 + 2u^2 + 1$
$c_8$	$(u^3 - u^2 + 2u - 1)^2$
$c_{10}, c_{11}$	$(u^3 + u^2 + 2u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$(y + 1)^6$
$c_2$	$(y - 1)^6$
$c_5, c_9$	$(y^3 + y^2 + 2y + 1)^2$
$c_8, c_{10}, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = 1.307140 + 0.215080I$ $b = -1.000000$	$-0.26574 + 2.82812I$	$-0.49024 - 2.97945I$
$u = 1.000000I$ $a = -1.307140 + 0.215080I$ $b = -1.000000$	$-0.26574 - 2.82812I$	$-0.49024 + 2.97945I$
$u = 1.000000I$ $a = 0.569840I$ $b = -1.000000$	$-4.40332$	$-7.01950$
$u = -1.000000I$ $a = -1.307140 - 0.215080I$ $b = -1.000000$	$-0.26574 - 2.82812I$	$-0.49024 + 2.97945I$
$u = -1.000000I$ $a = 1.307140 - 0.215080I$ $b = -1.000000$	$-0.26574 + 2.82812I$	$-0.49024 - 2.97945I$
$u = -1.000000I$ $a = -0.569840I$ $b = -1.000000$	$-4.40332$	$-7.01950$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$((u^2 + 1)^3)(u^{12} + u^{11} + \dots + 4u + 1)$ $\cdot (u^{13} + u^{11} - u^{10} + 7u^9 + 3u^7 - 5u^6 + 8u^5 + u^4 + 4u^3 - 2u^2 - 1)$
$c_2$	$((u + 1)^6)(u^{12} + 3u^{11} + \dots + 6u^2 + 1)(u^{13} + 2u^{12} + \dots - 4u - 1)$
$c_5, c_9$	$(u^6 + u^4 + 2u^2 + 1)(u^6 + u^5 + u^4 + 2u^2 + u + 1)^2$ $\cdot (u^{13} - 3u^{12} + \dots + 5u - 2)$
$c_8$	$(u^3 - u^2 + 2u - 1)^2(u^6 + u^5 + 5u^4 + 4u^3 + 6u^2 + 3u + 1)^2$ $\cdot (u^{13} + 3u^{12} + \dots + 5u - 4)$
$c_{10}, c_{11}$	$(u^3 + u^2 + 2u + 1)^2(u^6 + u^5 + 5u^4 + 4u^3 + 6u^2 + 3u + 1)^2$ $\cdot (u^{13} + 3u^{12} + \dots + 5u - 4)$



### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$((y+1)^6)(y^{12} + 3y^{11} + \dots + 6y^2 + 1)(y^{13} + 2y^{12} + \dots - 4y - 1)$
$c_2$	$((y-1)^6)(y^{12} + 11y^{11} + \dots + 12y + 1)(y^{13} + 26y^{12} + \dots + 12y - 1)$
$c_5, c_9$	$(y^3 + y^2 + 2y + 1)^2(y^6 + y^5 + 5y^4 + 4y^3 + 6y^2 + 3y + 1)^2$ $\cdot (y^{13} + 3y^{12} + \dots + 5y - 4)$
$c_8, c_{10}, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2(y^6 + 9y^5 + 29y^4 + 40y^3 + 22y^2 + 3y + 1)^2$ $\cdot (y^{13} + 15y^{12} + \dots + 177y - 16)$