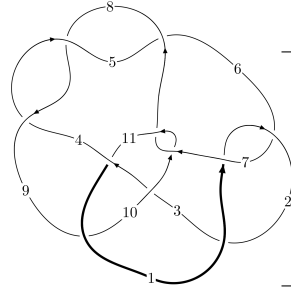
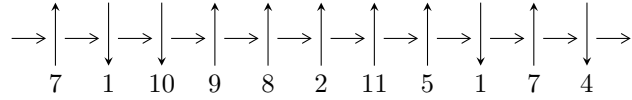


11n<sub>132</sub> (K11n<sub>132</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$1,7 \xrightarrow{c_1} 2 \xrightarrow{c_6} 4,6 \xrightarrow{c_{11}} 11 \xrightarrow{c_7} 8 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \xrightarrow{c_3} 3 \xrightarrow{c_9} 9 \longrightarrow c_2, c_4, c_8$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -7.33308 \times 10^{15}u^{20} - 1.72888 \times 10^{17}u^{19} + \dots + 1.09599 \times 10^{19}b - 8.78124 \times 10^{18}, \\ - 2.80505 \times 10^{18}u^{20} + 4.20368 \times 10^{18}u^{19} + \dots + 7.67190 \times 10^{19}a - 6.10889 \times 10^{19}, \\ u^{21} - u^{20} + \dots - 18u + 28 \rangle$$

$$I_2^u = \langle u^8 + 3u^6 + u^5 + 2u^4 + u^3 + u^2 + b + u - 1, -u^2 + a - 2, u^9 + 4u^7 + u^6 + 5u^5 + 2u^4 + 3u^3 + 2u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 30 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -7.33 \times 10^{15} u^{20} - 1.73 \times 10^{17} u^{19} + \cdots + 1.10 \times 10^{19} b - 8.78 \times 10^{18}, -2.81 \times 10^{18} u^{20} + 4.20 \times 10^{18} u^{19} + \cdots + 7.67 \times 10^{19} a - 6.11 \times 10^{19}, u^{21} - u^{20} + \cdots - 18u + 28 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0365627u^{20} - 0.0547932u^{19} + \cdots + 1.60738u + 0.796268 \\ 0.000669086u^{20} + 0.0157746u^{19} + \cdots - 0.933535u + 0.801219 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0196295u^{20} - 0.0100507u^{19} + \cdots + 1.18048u + 0.217188 \\ 0.00797850u^{20} - 0.0158077u^{19} + \cdots + 0.180611u - 0.795772 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0142692u^{20} + 0.0411108u^{19} + \cdots - 0.773349u + 1.95583 \\ -0.00351504u^{20} + 0.0137854u^{19} + \cdots - 0.476341u + 0.0864955 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0138798u^{20} - 0.0293691u^{19} + \cdots + 1.58093u + 0.793197 \\ 0.00952514u^{20} - 0.0122960u^{19} + \cdots + 0.486832u + 0.362072 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0196295u^{20} - 0.0100507u^{19} + \cdots + 1.18048u + 0.217188 \\ 0.0175759u^{20} - 0.0166603u^{19} + \cdots + 0.195992u + 0.0352752 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.00205357u^{20} - 0.0267111u^{19} + \cdots + 1.37648u + 0.252463 \\ 0.0175759u^{20} - 0.0166603u^{19} + \cdots + 0.195992u + 0.0352752 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.00205357u^{20} - 0.0267111u^{19} + \cdots + 1.37648u + 0.252463 \\ 0.0175759u^{20} - 0.0166603u^{19} + \cdots + 0.195992u + 0.0352752 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) Cusp Shapes} = \frac{445709904941671169}{2739962993558394514} u^{20} - \frac{891361635722125989}{5479925987116789028} u^{19} + \cdots + \frac{14080564157258258655}{2739962993558394514} u + \frac{2949485749258559055}{1369981496779197257}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{21} + u^{20} + \dots - 18u - 28$
$c_2$	$u^{21} + 33u^{20} + \dots - 1972u - 784$
$c_3$	$u^{21} - 24u^{19} + \dots + 1851u - 281$
$c_4, c_5, c_8$	$u^{21} + 2u^{20} + \dots - 12u - 11$
$c_7, c_{10}$	$u^{21} - 3u^{20} + \dots - 10u - 47$
$c_9$	$u^{21} - 17u^{19} + \dots + 73u - 13$
$c_{11}$	$u^{21} - 4u^{20} + \dots + 19u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{21} + 33y^{20} + \dots - 1972y - 784$
$c_2$	$y^{21} - 87y^{20} + \dots + 22145008y - 614656$
$c_3$	$y^{21} - 48y^{20} + \dots + 982063y - 78961$
$c_4, c_5, c_8$	$y^{21} + 26y^{20} + \dots - 846y - 121$
$c_7, c_{10}$	$y^{21} + 7y^{20} + \dots - 7232y - 2209$
$c_9$	$y^{21} - 34y^{20} + \dots + 2495y - 169$
$c_{11}$	$y^{21} - 4y^{20} + \dots + 319y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.667126 + 0.763695I$		
$a = 0.82594 - 1.23941I$	$1.34010 - 2.53227I$	$0.85890 + 6.43019I$
$b = 0.258218 + 1.151380I$		
$u = -0.667126 - 0.763695I$		
$a = 0.82594 + 1.23941I$	$1.34010 + 2.53227I$	$0.85890 - 6.43019I$
$b = 0.258218 - 1.151380I$		
$u = -0.354561 + 1.008430I$		
$a = -0.227436 + 0.200357I$	$-7.02572 + 3.49738I$	$-2.24629 - 2.87148I$
$b = 0.917813 - 0.821950I$		
$u = -0.354561 - 1.008430I$		
$a = -0.227436 - 0.200357I$	$-7.02572 - 3.49738I$	$-2.24629 + 2.87148I$
$b = 0.917813 + 0.821950I$		
$u = -0.135425 + 0.749831I$		
$a = 2.26639 + 0.24841I$	$1.72913 + 0.18094I$	$3.57258 - 0.16926I$
$b = 0.299503 - 0.694156I$		
$u = -0.135425 - 0.749831I$		
$a = 2.26639 - 0.24841I$	$1.72913 - 0.18094I$	$3.57258 + 0.16926I$
$b = 0.299503 + 0.694156I$		
$u = 0.137433 + 0.625721I$		
$a = 0.041014 - 0.214438I$	$-1.28019 - 1.09527I$	$-2.70112 + 3.21254I$
$b = 0.721689 + 0.405487I$		
$u = 0.137433 - 0.625721I$		
$a = 0.041014 + 0.214438I$	$-1.28019 + 1.09527I$	$-2.70112 - 3.21254I$
$b = 0.721689 - 0.405487I$		
$u = 0.576539 + 0.104726I$		
$a = 0.14734 - 1.76070I$	$-4.46536 - 3.00711I$	$1.90224 + 0.80232I$
$b = -0.906943 - 0.072981I$		
$u = 0.576539 - 0.104726I$		
$a = 0.14734 + 1.76070I$	$-4.46536 + 3.00711I$	$1.90224 - 0.80232I$
$b = -0.906943 + 0.072981I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.534365$ $a = 2.09662$ $b = -0.0562424$	1.11788	11.2410
$u = 0.07520 + 1.61647I$ $a = -0.453620 - 0.070826I$ $b = -0.793621 - 0.491574I$	$-8.87305 + 0.26805I$	$-1.47803 + 0.75243I$
$u = 0.07520 - 1.61647I$ $a = -0.453620 + 0.070826I$ $b = -0.793621 + 0.491574I$	$-8.87305 - 0.26805I$	$-1.47803 - 0.75243I$
$u = 1.10769 + 1.23434I$ $a = 0.723626 + 0.961597I$ $b = 1.194160 - 0.750185I$	$-7.93629 + 2.97451I$	$-2.24011 - 2.11283I$
$u = 1.10769 - 1.23434I$ $a = 0.723626 - 0.961597I$ $b = 1.194160 + 0.750185I$	$-7.93629 - 2.97451I$	$-2.24011 + 2.11283I$
$u = -0.31257 + 1.99292I$ $a = -0.345671 + 0.172538I$ $b = -1.21980 + 1.39213I$	$-17.7841 - 0.7836I$	$-1.50922 + 0.14627I$
$u = -0.31257 - 1.99292I$ $a = -0.345671 - 0.172538I$ $b = -1.21980 - 1.39213I$	$-17.7841 + 0.7836I$	$-1.50922 - 0.14627I$
$u = 0.42977 + 2.01390I$ $a = -0.984072 - 0.475371I$ $b = -1.34381 + 1.14589I$	$-18.4994 + 10.2668I$	$-1.32790 - 4.15834I$
$u = 0.42977 - 2.01390I$ $a = -0.984072 + 0.475371I$ $b = -1.34381 - 1.14589I$	$-18.4994 - 10.2668I$	$-1.32790 + 4.15834I$
$u = -0.08976 + 2.09219I$ $a = -1.363250 + 0.356504I$ $b = -1.099090 - 0.439233I$	$-10.14110 - 4.18838I$	$-1.95156 + 4.03302I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.08976 - 2.09219I$		
$a = -1.363250 - 0.356504I$	$-10.14110 + 4.18838I$	$-1.95156 - 4.03302I$
$b = -1.099090 + 0.439233I$		

$$\text{II. } I_2^u = \langle u^8 + 3u^6 + u^5 + 2u^4 + u^3 + u^2 + b + u - 1, -u^2 + a - 2, u^9 + 4u^7 + u^6 + 5u^5 + 2u^4 + 3u^3 + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 2 \\ -u^8 - 3u^6 - u^5 - 2u^4 - u^3 - u^2 - u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^8 + 3u^6 + u^5 + 2u^4 + u^3 + u^2 + u - 1 \\ 2u^8 + u^7 + 7u^6 + 5u^5 + 7u^4 + 5u^3 + 3u^2 + 3u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^8 + u^7 - 3u^6 + 3u^5 - u^4 + 3u^3 + u^2 + 2 \\ -2u^8 - u^7 - 7u^6 - 4u^5 - 7u^4 - 2u^3 - 2u^2 - u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^8 + 3u^6 + u^4 - 2u^3 - 2u^2 - 2u - 1 \\ -u^8 - 3u^6 - u^5 - 2u^4 - u^3 - 2u^2 - 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^8 + 3u^6 + u^5 + 2u^4 + u^3 + u^2 + u - 1 \\ u^8 + u^7 + 4u^6 + 4u^5 + 5u^4 + 4u^3 + 2u^2 + 2u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^8 + u^7 + 7u^6 + 5u^5 + 7u^4 + 5u^3 + 3u^2 + 3u - 1 \\ u^8 + u^7 + 4u^6 + 4u^5 + 5u^4 + 4u^3 + 2u^2 + 2u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^8 + u^7 + 7u^6 + 5u^5 + 7u^4 + 5u^3 + 3u^2 + 3u - 1 \\ u^8 + u^7 + 4u^6 + 4u^5 + 5u^4 + 4u^3 + 2u^2 + 2u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -2u^8 - 3u^7 - 8u^6 - 12u^5 - 15u^4 - 12u^3 - 14u^2 - 7u - 4$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^9 + 4u^7 + u^6 + 5u^5 + 2u^4 + 3u^3 + 2u^2 + 1$
$c_2$	$u^9 + 8u^8 + 26u^7 + 45u^6 + 45u^5 + 22u^4 - u^3 - 8u^2 - 4u - 1$
$c_3$	$u^9 + u^8 - 2u^7 - 3u^6 - u^5 + 4u^4 + 7u^3 + 6u^2 + 3u + 1$
$c_4, c_5$	$u^9 + u^8 + 5u^7 + 5u^6 + 9u^5 + 10u^4 + 7u^3 + 8u^2 + 2u + 1$
$c_6$	$u^9 + 4u^7 - u^6 + 5u^5 - 2u^4 + 3u^3 - 2u^2 - 1$
$c_7$	$u^9 - 2u^8 - u^7 + 4u^6 - 3u^5 + 4u^3 - 3u^2 + 1$
$c_8$	$u^9 - u^8 + 5u^7 - 5u^6 + 9u^5 - 10u^4 + 7u^3 - 8u^2 + 2u - 1$
$c_9$	$u^9 - 3u^8 - u^7 + 9u^6 - 2u^5 - 10u^4 + 7u^3 + 2u^2 - u - 1$
$c_{10}$	$u^9 + 2u^8 - u^7 - 4u^6 - 3u^5 + 4u^3 + 3u^2 - 1$
$c_{11}$	$u^9 - 3u^8 + 6u^7 - 7u^6 + 4u^5 + u^4 - 3u^3 + 2u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^9 + 8y^8 + 26y^7 + 45y^6 + 45y^5 + 22y^4 - y^3 - 8y^2 - 4y - 1$
$c_2$	$y^9 - 12y^8 + 46y^7 - 39y^6 + 113y^5 - 46y^4 + 83y^3 - 12y^2 - 1$
$c_3$	$y^9 - 5y^8 + 8y^7 + y^6 - 9y^5 - 8y^4 + y^3 - 2y^2 - 3y - 1$
$c_4, c_5, c_8$	$y^9 + 9y^8 + 33y^7 + 59y^6 + 39y^5 - 36y^4 - 85y^3 - 56y^2 - 12y - 1$
$c_7, c_{10}$	$y^9 - 6y^8 + 11y^7 - 2y^6 - 11y^5 + 4y^4 + 8y^3 - 9y^2 + 6y - 1$
$c_9$	$y^9 - 11y^8 + 51y^7 - 123y^6 + 180y^5 - 168y^4 + 111y^3 - 38y^2 + 5y - 1$
$c_{11}$	$y^9 + 3y^8 + 2y^7 - y^6 + 8y^5 + 9y^4 - y^3 - 8y^2 + 5y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.338665 + 0.974837I$ $a = 1.164390 + 0.660286I$ $b = 0.35504 - 1.42610I$	$-1.24626 + 1.32727I$	$-0.553077 - 1.214568I$
$u = 0.338665 - 0.974837I$ $a = 1.164390 - 0.660286I$ $b = 0.35504 + 1.42610I$	$-1.24626 - 1.32727I$	$-0.553077 + 1.214568I$
$u = -0.447524 + 0.951550I$ $a = 1.29483 - 0.85168I$ $b = 0.362962 + 1.048500I$	$1.95197 - 1.71727I$	$4.44186 + 1.84082I$
$u = -0.447524 - 0.951550I$ $a = 1.29483 + 0.85168I$ $b = 0.362962 - 1.048500I$	$1.95197 + 1.71727I$	$4.44186 - 1.84082I$
$u = -0.738179$ $a = 2.54491$ $b = 0.647287$	$0.518289$	$-4.57070$
$u = 0.318685 + 0.594099I$ $a = 1.74861 + 0.37866I$ $b = 1.063670 - 0.538027I$	$-4.97869 + 4.28681I$	$0.36640 - 5.34247I$
$u = 0.318685 - 0.594099I$ $a = 1.74861 - 0.37866I$ $b = 1.063670 + 0.538027I$	$-4.97869 - 4.28681I$	$0.36640 + 5.34247I$
$u = 0.15926 + 1.58292I$ $a = -0.480277 + 0.504206I$ $b = -0.605320 - 0.206182I$	$-9.14564 - 1.83774I$	$-3.46986 + 2.95801I$
$u = 0.15926 - 1.58292I$ $a = -0.480277 - 0.504206I$ $b = -0.605320 + 0.206182I$	$-9.14564 + 1.83774I$	$-3.46986 - 2.95801I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^9 + 4u^7 + \dots + 2u^2 + 1)(u^{21} + u^{20} + \dots - 18u - 28)$
$c_2$	$(u^9 + 8u^8 + 26u^7 + 45u^6 + 45u^5 + 22u^4 - u^3 - 8u^2 - 4u - 1)$ $\cdot (u^{21} + 33u^{20} + \dots - 1972u - 784)$
$c_3$	$(u^9 + u^8 - 2u^7 - 3u^6 - u^5 + 4u^4 + 7u^3 + 6u^2 + 3u + 1)$ $\cdot (u^{21} - 24u^{19} + \dots + 1851u - 281)$
$c_4, c_5$	$(u^9 + u^8 + 5u^7 + 5u^6 + 9u^5 + 10u^4 + 7u^3 + 8u^2 + 2u + 1)$ $\cdot (u^{21} + 2u^{20} + \dots - 12u - 11)$
$c_6$	$(u^9 + 4u^7 + \dots - 2u^2 - 1)(u^{21} + u^{20} + \dots - 18u - 28)$
$c_7$	$(u^9 - 2u^8 + \dots - 3u^2 + 1)(u^{21} - 3u^{20} + \dots - 10u - 47)$
$c_8$	$(u^9 - u^8 + 5u^7 - 5u^6 + 9u^5 - 10u^4 + 7u^3 - 8u^2 + 2u - 1)$ $\cdot (u^{21} + 2u^{20} + \dots - 12u - 11)$
$c_9$	$(u^9 - 3u^8 - u^7 + 9u^6 - 2u^5 - 10u^4 + 7u^3 + 2u^2 - u - 1)$ $\cdot (u^{21} - 17u^{19} + \dots + 73u - 13)$
$c_{10}$	$(u^9 + 2u^8 + \dots + 3u^2 - 1)(u^{21} - 3u^{20} + \dots - 10u - 47)$
$c_{11}$	$(u^9 - 3u^8 + 6u^7 - 7u^6 + 4u^5 + u^4 - 3u^3 + 2u^2 + u - 1)$ $\cdot (u^{21} - 4u^{20} + \dots + 19u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$(y^9 + 8y^8 + 26y^7 + 45y^6 + 45y^5 + 22y^4 - y^3 - 8y^2 - 4y - 1)$ $\cdot (y^{21} + 33y^{20} + \dots - 1972y - 784)$
$c_2$	$(y^9 - 12y^8 + 46y^7 - 39y^6 + 113y^5 - 46y^4 + 83y^3 - 12y^2 - 1)$ $\cdot (y^{21} - 87y^{20} + \dots + 22145008y - 614656)$
$c_3$	$(y^9 - 5y^8 + 8y^7 + y^6 - 9y^5 - 8y^4 + y^3 - 2y^2 - 3y - 1)$ $\cdot (y^{21} - 48y^{20} + \dots + 982063y - 78961)$
$c_4, c_5, c_8$	$(y^9 + 9y^8 + 33y^7 + 59y^6 + 39y^5 - 36y^4 - 85y^3 - 56y^2 - 12y - 1)$ $\cdot (y^{21} + 26y^{20} + \dots - 846y - 121)$
$c_7, c_{10}$	$(y^9 - 6y^8 + 11y^7 - 2y^6 - 11y^5 + 4y^4 + 8y^3 - 9y^2 + 6y - 1)$ $\cdot (y^{21} + 7y^{20} + \dots - 7232y - 2209)$
$c_9$	$(y^9 - 11y^8 + 51y^7 - 123y^6 + 180y^5 - 168y^4 + 111y^3 - 38y^2 + 5y - 1)$ $\cdot (y^{21} - 34y^{20} + \dots + 2495y - 169)$
$c_{11}$	$(y^9 + 3y^8 + 2y^7 - y^6 + 8y^5 + 9y^4 - y^3 - 8y^2 + 5y - 1)$ $\cdot (y^{21} - 4y^{20} + \dots + 319y - 1)$