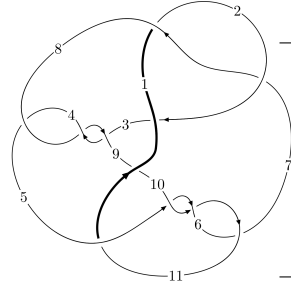
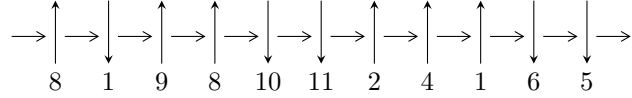


11n₁₃₈ (K11n₁₃₈)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$1, 8 \xrightarrow{c_1} 2, 4 \xrightarrow{c_4} 5 \xrightarrow{c_8} 9 \xrightarrow{c_9} 10 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \xrightarrow{c_6} 6 \longrightarrow c_2, c_5, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -u^8 - u^7 - 8u^6 - 5u^5 - 12u^4 - 3u^3 + 20u^2 + 8b + u + 1, a - 1, \\ u^9 + 9u^7 - 3u^6 + 23u^5 - 15u^4 + 7u^3 - 5u^2 - 1 \rangle$$

$$I_2^u = \langle b^3 + b^2u - 3b^2 - 2bu + 3b + 2u - 1, a + 1, u^2 + 1 \rangle$$

$$I_3^u = \langle b - 1, u^3 + 6u^2 + 15a + 4u + 20, u^4 + u^3 + 4u^2 + 5 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 19 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew (<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose (<https://github.com/CATSTAILS/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -u^8 - u^7 + \dots + 8b + 1, a - 1, u^9 + 9u^7 - 3u^6 + 23u^5 - 15u^4 + 7u^3 - 5u^2 - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ \frac{1}{8}u^8 + \frac{1}{8}u^7 + \dots - \frac{1}{8}u - \frac{1}{8} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ \frac{1}{8}u^8 + \frac{1}{8}u^7 + \dots - \frac{1}{8}u - \frac{1}{8} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ \frac{1}{8}u^8 - \frac{1}{8}u^7 + \dots + \frac{7}{8}u + \frac{1}{8} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{8}u^8 - \frac{1}{8}u^7 + \dots + \frac{15}{8}u + \frac{1}{8} \\ \frac{1}{8}u^8 - \frac{1}{8}u^7 + \dots + \frac{7}{8}u + \frac{1}{8} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{8}u^8 - \frac{1}{8}u^7 + \dots + \frac{1}{8}u + \frac{9}{8} \\ -\frac{1}{8}u^8 - \frac{1}{8}u^7 + \dots + \frac{1}{8}u + \frac{9}{8} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{8}u^8 + \frac{3}{8}u^7 + \dots - \frac{7}{8}u - \frac{1}{8} \\ \frac{1}{8}u^8 + \frac{3}{8}u^7 + \dots - \frac{7}{8}u - \frac{1}{8} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{8}u^8 + \frac{3}{8}u^7 + \dots - \frac{7}{8}u - \frac{1}{8} \\ \frac{1}{8}u^8 + \frac{3}{8}u^7 + \dots - \frac{7}{8}u - \frac{1}{8} \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{3}{2}u^8 + 2u^7 - \frac{27}{2}u^6 + 22u^5 - 40u^4 + 64u^3 - \frac{73}{2}u^2 + 10u - \frac{9}{2}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_4 c_7, c_8	$u^9 + 9u^7 + 3u^6 + 23u^5 + 15u^4 + 7u^3 + 5u^2 + 1$
c_2	$u^9 + 18u^8 + \dots - 10u - 1$
c_5, c_6, c_{10}	$u^9 - 3u^8 + 5u^6 + u^5 - 2u^4 - 9u^3 + 5u^2 + u + 2$
c_9	$u^9 + u^8 + 22u^7 + 19u^6 + 127u^5 + 84u^4 + 67u^3 - 41u^2 + 23u + 8$
c_{11}	$u^9 + 9u^8 + 38u^7 + 85u^6 + 87u^5 - 18u^4 - 147u^3 - 167u^2 - 85u - 26$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_4 c_7, c_8	$y^9 + 18y^8 + \dots - 10y - 1$
c_2	$y^9 - 70y^8 + \dots - 10y - 1$
c_5, c_6, c_{10}	$y^9 - 9y^8 + 32y^7 - 55y^6 + 53y^5 - 60y^4 + 83y^3 - 35y^2 - 19y - 4$
c_9	$y^9 + 43y^8 + \dots + 1185y - 64$
c_{11}	$y^9 - 5y^8 + \dots - 1459y - 676$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.721273$ $a = 1.00000$ $b = -0.684414$	-3.38429	-0.599760
$u = 0.159982 + 0.567821I$ $a = 1.00000$ $b = 0.666256 - 0.688894I$	$-4.68408 + 3.45373I$	$-2.44779 - 5.78928I$
$u = 0.159982 - 0.567821I$ $a = 1.00000$ $b = 0.666256 + 0.688894I$	$-4.68408 - 3.45373I$	$-2.44779 + 5.78928I$
$u = -0.198901 + 0.378443I$ $a = 1.00000$ $b = 0.170075 + 0.364475I$	$0.131099 - 0.964036I$	$2.44921 + 7.22651I$
$u = -0.198901 - 0.378443I$ $a = 1.00000$ $b = 0.170075 - 0.364475I$	$0.131099 + 0.964036I$	$2.44921 - 7.22651I$
$u = 0.14689 + 2.12129I$ $a = 1.00000$ $b = -2.55711 - 0.09982I$	$-17.5620 + 3.0332I$	$-3.21143 - 2.16261I$
$u = 0.14689 - 2.12129I$ $a = 1.00000$ $b = -2.55711 + 0.09982I$	$-17.5620 - 3.0332I$	$-3.21143 + 2.16261I$
$u = -0.46861 + 2.14498I$ $a = 1.00000$ $b = -2.43701 + 0.25982I$	$14.7600 - 7.7767I$	$-5.49011 + 2.86525I$
$u = -0.46861 - 2.14498I$ $a = 1.00000$ $b = -2.43701 - 0.25982I$	$14.7600 + 7.7767I$	$-5.49011 - 2.86525I$

$$\text{II. } I_2^u = \langle b^3 + b^2u - 3b^2 - 2bu + 3b + 2u - 1, a + 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ b \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ b - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -bu + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -bu + 2u \\ -bu + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} b \\ -b^2 + 2b - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -b^2u - b^2 + 2bu + 2b - 2u - 2 \\ -b^2u + 2bu + b - 2u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -b^2u - b^2 + 2bu + 2b - 2u - 2 \\ -b^2u + 2bu + b - 2u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4bu + 4u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_4 c_7, c_8	$(u^2 + 1)^3$
c_2	$(u + 1)^6$
c_5, c_6, c_{10}	$u^6 - 3u^4 + 2u^2 + 1$
c_9	$(u^3 - u^2 + 1)^2$
c_{11}	$u^6 + u^4 + 2u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_4 c_7, c_8	$(y + 1)^6$
c_2	$(y - 1)^6$
c_5, c_6, c_{10}	$(y^3 - 3y^2 + 2y + 1)^2$
c_9	$(y^3 - y^2 + 2y - 1)^2$
c_{11}	$(y^3 + y^2 + 2y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = -1.00000$ $b = 0.255138 - 0.877439I$	$-6.31400 - 2.82812I$	$-7.50976 + 2.97945I$
$u = 1.000000I$ $a = -1.00000$ $b = 1.000000 + 0.754878I$	-2.17641	$-6 - 0.980489 + 0.10I$
$u = 1.000000I$ $a = -1.00000$ $b = 1.74486 - 0.87744I$	$-6.31400 + 2.82812I$	$-7.50976 - 2.97945I$
$u = -1.000000I$ $a = -1.00000$ $b = 0.255138 + 0.877439I$	$-6.31400 + 2.82812I$	$-7.50976 - 2.97945I$
$u = -1.000000I$ $a = -1.00000$ $b = 1.000000 - 0.754878I$	-2.17641	$-6 - 0.980489 + 0.10I$
$u = -1.000000I$ $a = -1.00000$ $b = 1.74486 + 0.87744I$	$-6.31400 - 2.82812I$	$-7.50976 + 2.97945I$

$$\text{III. } I_3^u = \langle b - 1, u^3 + 6u^2 + 15a + 4u + 20, u^4 + u^3 + 4u^2 + 5 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{15}u^3 - \frac{2}{5}u^2 - \frac{4}{15}u - \frac{4}{3} \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{15}u^3 - \frac{2}{5}u^2 - \frac{4}{15}u - \frac{4}{3} \\ -\frac{1}{3}u^3 - \frac{1}{3}u - \frac{2}{3} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{8}{15}u^3 + \frac{1}{5}u^2 + \frac{17}{15}u - \frac{1}{3} \\ -\frac{1}{3}u^3 - \frac{1}{3}u + \frac{1}{3} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{5}u^3 + \frac{1}{5}u^2 + \frac{4}{5}u \\ -\frac{1}{3}u^3 - \frac{1}{3}u + \frac{1}{3} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{4}{15}u^3 - \frac{3}{5}u^2 - \frac{1}{15}u - \frac{1}{3} \\ -u^3 - u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{2}{15}u^3 - \frac{4}{5}u^2 - \frac{8}{15}u - \frac{5}{3} \\ -\frac{2}{3}u^3 - \frac{2}{3}u - \frac{4}{3} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{2}{15}u^3 - \frac{4}{5}u^2 - \frac{8}{15}u - \frac{5}{3} \\ -\frac{2}{3}u^3 - \frac{2}{3}u - \frac{4}{3} \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_4 c_7, c_8	$u^4 - u^3 + 4u^2 + 5$
c_2	$u^4 + 7u^3 + 26u^2 + 40u + 25$
c_5, c_6, c_{10}	$(u^2 + u - 1)^2$
c_9	$(u^2 - u - 1)^2$
c_{11}	$(u^2 - 3u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_4 c_7, c_8	$y^4 + 7y^3 + 26y^2 + 40y + 25$
c_2	$y^4 + 3y^3 + 166y^2 - 300y + 625$
c_5, c_6, c_9 c_{10}	$(y^2 - 3y + 1)^2$
c_{11}	$(y^2 - 7y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.309017 + 1.134230I$ $a = -0.861803 - 0.507242I$ $b = 1.00000$	-4.27683	-6.00000
$u = 0.309017 - 1.134230I$ $a = -0.861803 + 0.507242I$ $b = 1.00000$	-4.27683	-6.00000
$u = -0.80902 + 1.72149I$ $a = -0.638197 + 0.769873I$ $b = 1.00000$	-12.1725	-6.00000
$u = -0.80902 - 1.72149I$ $a = -0.638197 - 0.769873I$ $b = 1.00000$	-12.1725	-6.00000

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_3, c_4 c_7, c_8	$(u^2 + 1)^3(u^4 - u^3 + 4u^2 + 5)$ $\cdot (u^9 + 9u^7 + 3u^6 + 23u^5 + 15u^4 + 7u^3 + 5u^2 + 1)$
c_2	$((u + 1)^6)(u^4 + 7u^3 + \dots + 40u + 25)(u^9 + 18u^8 + \dots - 10u - 1)$
c_5, c_6, c_{10}	$(u^2 + u - 1)^2(u^6 - 3u^4 + 2u^2 + 1)$ $\cdot (u^9 - 3u^8 + 5u^6 + u^5 - 2u^4 - 9u^3 + 5u^2 + u + 2)$
c_9	$(u^2 - u - 1)^2(u^3 - u^2 + 1)^2$ $\cdot (u^9 + u^8 + 22u^7 + 19u^6 + 127u^5 + 84u^4 + 67u^3 - 41u^2 + 23u + 8)$
c_{11}	$(u^2 - 3u + 1)^2(u^6 + u^4 + 2u^2 + 1)$ $\cdot (u^9 + 9u^8 + 38u^7 + 85u^6 + 87u^5 - 18u^4 - 147u^3 - 167u^2 - 85u - 26)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_4 c_7, c_8	$((y + 1)^6)(y^4 + 7y^3 + \dots + 40y + 25)(y^9 + 18y^8 + \dots - 10y - 1)$
c_2	$((y - 1)^6)(y^4 + 3y^3 + \dots - 300y + 625)(y^9 - 70y^8 + \dots - 10y - 1)$
c_5, c_6, c_{10}	$(y^2 - 3y + 1)^2(y^3 - 3y^2 + 2y + 1)^2$ $\cdot (y^9 - 9y^8 + 32y^7 - 55y^6 + 53y^5 - 60y^4 + 83y^3 - 35y^2 - 19y - 4)$
c_9	$((y^2 - 3y + 1)^2)(y^3 - y^2 + 2y - 1)^2(y^9 + 43y^8 + \dots + 1185y - 64)$
c_{11}	$((y^2 - 7y + 1)^2)(y^3 + y^2 + 2y + 1)^2(y^9 - 5y^8 + \dots - 1459y - 676)$