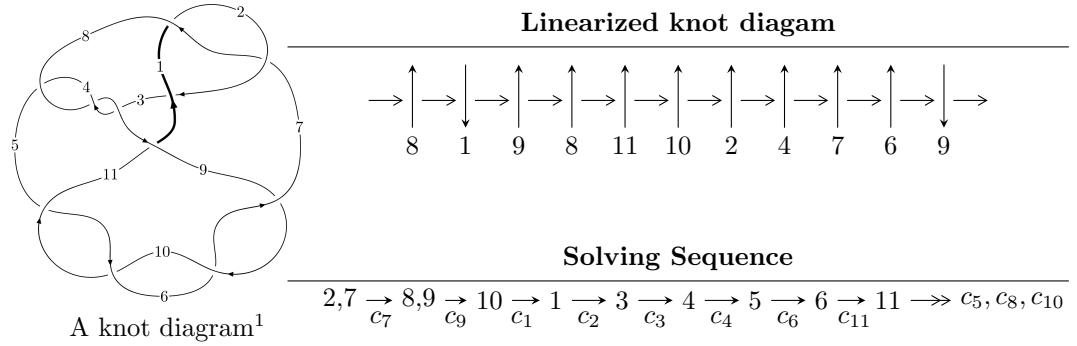


## $11n_{140}$ ( $K11n_{140}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -u^{12} + u^{11} - u^{10} + 2u^9 - 6u^8 + 5u^7 - u^6 + 4u^5 - 6u^4 + 4u^3 + 6u^2 + 4b + 1, \\
 &\quad -u^{12} + u^{11} - u^{10} + 2u^9 - 6u^8 + 5u^7 - u^6 + 4u^5 - 10u^4 + 4u^3 + 2u^2 + 4a - 3, \\
 &\quad u^{13} + 2u^{11} - u^{10} + 6u^9 - u^8 + 6u^7 - 3u^6 + 8u^5 + 4u^3 + u + 1 \rangle \\
 I_2^u &= \langle 2336u^{15} - 694u^{14} + \dots + 13139b - 13544, -7442u^{15} + 7948u^{14} + \dots + 65695a + 191727, \\
 &\quad u^{16} + u^{15} + \dots + 4u + 5 \rangle \\
 I_3^u &= \langle b - a - 1, a^2 - au + 2a - u + 2, u^2 + 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 33 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{12} + u^{11} + \dots + 4b + 1, -u^{12} + u^{11} + \dots + 4a - 3, u^{13} + 2u^{11} + \dots + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots - \frac{1}{2}u^2 + \frac{3}{4} \\ \frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots - \frac{3}{2}u^2 - \frac{1}{4} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}u^{12} - \frac{1}{2}u^{11} + \dots - 2u^2 + \frac{1}{2} \\ \frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots - \frac{3}{2}u^2 - \frac{1}{4} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots + \frac{1}{2}u - \frac{1}{4} \\ -\frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots + \frac{1}{2}u - \frac{1}{4} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots + \frac{3}{2}u - \frac{1}{4} \\ -\frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots + \frac{1}{2}u - \frac{1}{4} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{4}u^{12} - \frac{5}{4}u^{11} + \dots - u - \frac{5}{4} \\ -\frac{1}{2}u^{11} + \frac{1}{2}u^{10} + \dots - \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{5}{4}u^{12} - \frac{1}{4}u^{11} + \dots - \frac{5}{2}u - \frac{3}{4} \\ -u^{12} - \frac{3}{2}u^{10} + \dots - u - \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{5}{4}u^{12} - \frac{1}{4}u^{11} + \dots - \frac{5}{2}u - \frac{3}{4} \\ -u^{12} - \frac{3}{2}u^{10} + \dots - u - \frac{1}{2} \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 3u^{12} - 3u^{11} + 6u^{10} - 9u^9 + 20u^8 - 20u^7 + 19u^6 - 24u^5 + 29u^4 - 20u^3 + 7u^2 - 8u + 6$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_7, c_8$	$u^{13} + 2u^{11} + u^{10} + 6u^9 + u^8 + 6u^7 + 3u^6 + 8u^5 + 4u^3 + u - 1$
$c_2$	$u^{13} + 4u^{12} + \cdots + u - 1$
$c_5, c_6, c_9$ $c_{10}$	$u^{13} + 3u^{12} + \cdots - 3u - 2$
$c_{11}$	$u^{13} - 3u^{12} + \cdots + 41u - 24$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_7, c_8$	$y^{13} + 4y^{12} + \cdots + y - 1$
$c_2$	$y^{13} + 16y^{12} + \cdots + 17y - 1$
$c_5, c_6, c_9$ $c_{10}$	$y^{13} + 15y^{12} + \cdots + 17y - 4$
$c_{11}$	$y^{13} + 3y^{12} + \cdots + 6385y - 576$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.849803 + 0.688633I$		
$a = 0.100600 + 0.370738I$	$-2.33364 + 0.79324I$	$4.73185 - 2.01069I$
$b = 0.161020 - 1.380070I$		
$u = 0.849803 - 0.688633I$		
$a = 0.100600 - 0.370738I$	$-2.33364 - 0.79324I$	$4.73185 + 2.01069I$
$b = 0.161020 + 1.380070I$		
$u = -0.301931 + 0.795374I$		
$a = 0.53836 + 1.69819I$	$-11.18850 - 1.28224I$	$2.05046 + 5.61257I$
$b = 0.01733 + 1.65836I$		
$u = -0.301931 - 0.795374I$		
$a = 0.53836 - 1.69819I$	$-11.18850 + 1.28224I$	$2.05046 - 5.61257I$
$b = 0.01733 - 1.65836I$		
$u = -0.793875 + 0.936102I$		
$a = -0.703154 - 0.416062I$	$3.03190 - 3.86102I$	$7.31704 + 2.47395I$
$b = 0.691430 + 0.338829I$		
$u = -0.793875 - 0.936102I$		
$a = -0.703154 + 0.416062I$	$3.03190 + 3.86102I$	$7.31704 - 2.47395I$
$b = 0.691430 - 0.338829I$		
$u = 0.426416 + 0.596732I$		
$a = 0.581070 - 0.572912I$	$-2.28202 + 1.46619I$	$3.02331 - 4.77758I$
$b = -0.016047 - 0.904459I$		
$u = 0.426416 - 0.596732I$		
$a = 0.581070 + 0.572912I$	$-2.28202 - 1.46619I$	$3.02331 + 4.77758I$
$b = -0.016047 + 0.904459I$		
$u = 0.760740 + 1.064260I$		
$a = -1.237650 + 0.471225I$	$2.12458 + 8.30943I$	$4.97203 - 7.67433I$
$b = 0.631392 + 0.645827I$		
$u = 0.760740 - 1.064260I$		
$a = -1.237650 - 0.471225I$	$2.12458 - 8.30943I$	$4.97203 + 7.67433I$
$b = 0.631392 - 0.645827I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.717554 + 1.160670I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$1.59544 + 6.78413I$
$a = -1.71256 - 0.47703I$	$-5.31862 - 11.41160I$	$1.59544 + 6.78413I$
$b = 0.20153 - 1.58392I$		
$u = -0.717554 - 1.160670I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$1.59544 - 6.78413I$
$a = -1.71256 + 0.47703I$	$-5.31862 + 11.41160I$	$1.59544 - 6.78413I$
$b = 0.20153 + 1.58392I$		
$u = -0.447199$		
$a = 0.866672$	0.678852	14.6200
$b = -0.373309$		

$$\text{II. } I_2^u = \langle 2336u^{15} - 694u^{14} + \cdots + 13139b - 13544, -7442u^{15} + 7948u^{14} + \cdots + 65695a + 191727, u^{16} + u^{15} + \cdots + 4u + 5 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.113281u^{15} - 0.120983u^{14} + \cdots - 0.144562u - 2.91844 \\ -0.177791u^{15} + 0.0528198u^{14} + \cdots - 0.306035u + 1.03082 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0645102u^{15} - 0.0681635u^{14} + \cdots - 0.450597u - 1.88762 \\ -0.177791u^{15} + 0.0528198u^{14} + \cdots - 0.306035u + 1.03082 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.440429u^{15} + 0.374290u^{14} + \cdots + 5.23398u + 1.69710 \\ -0.246594u^{15} - 0.358246u^{14} + \cdots - 0.496385u - 1.22780 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{5}u^{15} + \frac{1}{5}u^{14} + \cdots + \frac{14}{5}u + \frac{4}{5} \\ -0.240429u^{15} - 0.174290u^{14} + \cdots - 1.43398u - 0.897100 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0488926u^{15} - 0.264525u^{14} + \cdots - 0.240840u - 0.483477 \\ -0.287236u^{15} - 0.200624u^{14} + \cdots - 0.500419u - 0.889413 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.206165u^{15} + 0.383956u^{14} + \cdots + 0.862410u + 1.13069 \\ -0.0159830u^{15} - 0.106553u^{14} + \cdots + 1.24560u - 0.338839 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.206165u^{15} + 0.383956u^{14} + \cdots + 0.862410u + 1.13069 \\ -0.0159830u^{15} - 0.106553u^{14} + \cdots + 1.24560u - 0.338839 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $\frac{488}{1877}u^{15} - \frac{1752}{1877}u^{14} + \cdots - \frac{16008}{1877}u - \frac{9926}{1877}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_7, c_8$	$u^{16} - u^{15} + \cdots - 4u + 5$
$c_2$	$u^{16} + 7u^{15} + \cdots + 124u + 25$
$c_5, c_6, c_9$ $c_{10}, c_{11}$	$(u^8 - u^7 + 5u^6 - 4u^5 + 7u^4 - 4u^3 + 2u^2 + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_7, c_8$	$y^{16} + 7y^{15} + \cdots + 124y + 25$
$c_2$	$y^{16} + 3y^{15} + \cdots + 824y + 625$
$c_5, c_6, c_9$ $c_{10}, c_{11}$	$(y^8 + 9y^7 + 31y^6 + 50y^5 + 39y^4 + 22y^3 + 18y^2 + 4y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.548614 + 0.832668I$		
$a = -1.83759 + 1.08227I$	$-9.89946 - 2.18536I$	$0.41681 + 3.14055I$
$b = 0.06382 - 1.51723I$		
$u = -0.548614 - 0.832668I$		
$a = -1.83759 - 1.08227I$	$-9.89946 + 2.18536I$	$0.41681 - 3.14055I$
$b = 0.06382 + 1.51723I$		
$u = -0.969644 + 0.496042I$		
$a = 0.353364 + 0.413115I$	$-3.28987 + 5.23868I$	$4.00000 - 3.04258I$
$b = -0.19980 - 1.51366I$		
$u = -0.969644 - 0.496042I$		
$a = 0.353364 - 0.413115I$	$-3.28987 - 5.23868I$	$4.00000 + 3.04258I$
$b = -0.19980 + 1.51366I$		
$u = 0.886697 + 0.673651I$		
$a = 0.835367 - 0.338086I$	$3.31972 - 2.18536I$	$7.58319 + 3.14055I$
$b = -0.647085 + 0.502738I$		
$u = 0.886697 - 0.673651I$		
$a = 0.835367 + 0.338086I$	$3.31972 + 2.18536I$	$7.58319 - 3.14055I$
$b = -0.647085 - 0.502738I$		
$u = -0.822874 + 0.843581I$		
$a = 1.216240 + 0.256877I$	$3.31972 - 2.18536I$	$7.58319 + 3.14055I$
$b = -0.647085 + 0.502738I$		
$u = -0.822874 - 0.843581I$		
$a = 1.216240 - 0.256877I$	$3.31972 + 2.18536I$	$7.58319 - 3.14055I$
$b = -0.647085 - 0.502738I$		
$u = 0.043421 + 1.182100I$		
$a = -0.104055 - 0.579236I$	$-3.28987 - 1.04600I$	$4.00000 + 6.68545I$
$b = 0.283060 - 0.443755I$		
$u = 0.043421 - 1.182100I$		
$a = -0.104055 + 0.579236I$	$-3.28987 + 1.04600I$	$4.00000 - 6.68545I$
$b = 0.283060 + 0.443755I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.239639 + 0.738346I$		
$a = -1.82664 - 0.62597I$	$-3.28987 + 1.04600I$	$4.00000 - 6.68545I$
$b = 0.283060 + 0.443755I$		
$u = 0.239639 - 0.738346I$		
$a = -1.82664 + 0.62597I$	$-3.28987 - 1.04600I$	$4.00000 + 6.68545I$
$b = 0.283060 - 0.443755I$		
$u = 0.769845 + 1.017620I$		
$a = 1.54571 - 0.12141I$	$-3.28987 + 5.23868I$	$4.00000 - 3.04258I$
$b = -0.19980 - 1.51366I$		
$u = 0.769845 - 1.017620I$		
$a = 1.54571 + 0.12141I$	$-3.28987 - 5.23868I$	$4.00000 + 3.04258I$
$b = -0.19980 + 1.51366I$		
$u = -0.098471 + 1.335410I$		
$a = 0.017611 + 1.367960I$	$-9.89946 + 2.18536I$	$0.41681 - 3.14055I$
$b = 0.06382 + 1.51723I$		
$u = -0.098471 - 1.335410I$		
$a = 0.017611 - 1.367960I$	$-9.89946 - 2.18536I$	$0.41681 + 3.14055I$
$b = 0.06382 - 1.51723I$		

$$\text{III. } I_3^u = \langle b - a - 1, \ a^2 - au + 2a - u + 2, \ u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} a \\ a+1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 2a+1 \\ a+1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -au+u \\ -au \end{pmatrix} \\ a_5 &= \begin{pmatrix} -au \\ -au-u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 2au-a+2u-2 \\ au+u-1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -au-a-3u-1 \\ -a-u-1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -au-a-3u-1 \\ -a-u-1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -4

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_7, c_8$	$(u^2 + 1)^2$
$c_2$	$(u + 1)^4$
$c_5, c_6, c_9$ $c_{10}$	$u^4 + 3u^2 + 1$
$c_{11}$	$(u^2 - u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_7, c_8$	$(y + 1)^4$
$c_2$	$(y - 1)^4$
$c_5, c_6, c_9$ $c_{10}$	$(y^2 + 3y + 1)^2$
$c_{11}$	$(y^2 - 3y + 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$		
$a = -1.000000 - 0.618034I$	-4.27683	-4.00000
$b = -0.618034I$		
$u = 1.000000I$		
$a = -1.000000 + 1.618034I$	-12.1725	-4.00000
$b = 1.618034I$		
$u = -1.000000I$		
$a = -1.000000 + 0.618034I$	-4.27683	-4.00000
$b = 0.618034I$		
$u = -1.000000I$		
$a = -1.000000 - 1.618034I$	-12.1725	-4.00000
$b = -1.618034I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_7, c_8$	$(u^2 + 1)^2(u^{13} + 2u^{11} + u^{10} + 6u^9 + u^8 + 6u^7 + 3u^6 + 8u^5 + 4u^3 + u - 1) \cdot (u^{16} - u^{15} + \dots - 4u + 5)$
$c_2$	$((u + 1)^4)(u^{13} + 4u^{12} + \dots + u - 1)(u^{16} + 7u^{15} + \dots + 124u + 25)$
$c_5, c_6, c_9$ $c_{10}$	$(u^4 + 3u^2 + 1)(u^8 - u^7 + 5u^6 - 4u^5 + 7u^4 - 4u^3 + 2u^2 + 1)^2 \cdot (u^{13} + 3u^{12} + \dots - 3u - 2)$
$c_{11}$	$(u^2 - u - 1)^2(u^8 - u^7 + 5u^6 - 4u^5 + 7u^4 - 4u^3 + 2u^2 + 1)^2 \cdot (u^{13} - 3u^{12} + \dots + 41u - 24)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_7, c_8$	$((y+1)^4)(y^{13} + 4y^{12} + \dots + y - 1)(y^{16} + 7y^{15} + \dots + 124y + 25)$
$c_2$	$((y-1)^4)(y^{13} + 16y^{12} + \dots + 17y - 1)(y^{16} + 3y^{15} + \dots + 824y + 625)$
$c_5, c_6, c_9$ $c_{10}$	$(y^2 + 3y + 1)^2$ $\cdot (y^8 + 9y^7 + 31y^6 + 50y^5 + 39y^4 + 22y^3 + 18y^2 + 4y + 1)^2$ $\cdot (y^{13} + 15y^{12} + \dots + 17y - 4)$
$c_{11}$	$(y^2 - 3y + 1)^2$ $\cdot (y^8 + 9y^7 + 31y^6 + 50y^5 + 39y^4 + 22y^3 + 18y^2 + 4y + 1)^2$ $\cdot (y^{13} + 3y^{12} + \dots + 6385y - 576)$