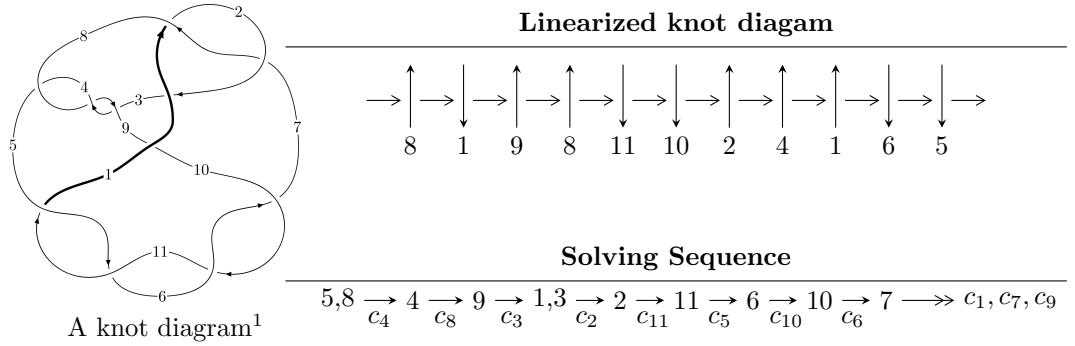


$11n_{141}$ ($K11n_{141}$)



Ideals for irreducible components² of X_{par}

$$\begin{aligned} I_1^u &= \langle -u^7 - u^6 - 6u^5 - 7u^4 - 9u^3 - 15u^2 + 4b - 1, a - 1, u^8 + 7u^6 + u^5 + 14u^4 + 4u^3 + 5u^2 - u + 1 \rangle \\ I_2^u &= \langle -u^5 + 2u^4 - u^3 + 5u^2 + 5b - u, u^5 + 2u^3 + 2u^2 + 5a + u + 7, u^6 - u^5 + 4u^4 - 4u^3 + 6u^2 - 4u + 5 \rangle \\ I_3^u &= \langle b^2 + bu + 1, a + 1, u^2 + 1 \rangle \end{aligned}$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 18 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^7 - u^6 - 6u^5 - 7u^4 - 9u^3 - 15u^2 + 4b - 1, \ a - 1, \ u^8 + 7u^6 + u^5 + 14u^4 + 4u^3 + 5u^2 - u + 1 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ \frac{1}{4}u^7 + \frac{1}{4}u^6 + \cdots + \frac{15}{4}u^2 + \frac{1}{4} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ \frac{1}{4}u^7 + \frac{1}{4}u^6 + \cdots + \frac{11}{4}u^2 + \frac{1}{4} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^7 + \frac{1}{4}u^6 + \cdots + \frac{15}{4}u^2 + \frac{5}{4} \\ \frac{1}{4}u^7 + \frac{1}{4}u^6 + \cdots + \frac{15}{4}u^2 + \frac{1}{4} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{4}u^7 + \frac{1}{4}u^6 + \cdots - \frac{1}{2}u + \frac{3}{4} \\ -\frac{1}{2}u^7 - \frac{1}{2}u^5 + \cdots - \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{4}u^7 + \frac{1}{4}u^6 + \cdots + \frac{3}{2}u + \frac{1}{4} \\ \frac{1}{2}u^5 - \frac{1}{2}u^4 + \cdots + 2u - \frac{1}{2} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ \frac{1}{4}u^7 - \frac{1}{4}u^6 + \cdots - \frac{1}{2}u - \frac{1}{4} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ \frac{1}{4}u^7 - \frac{1}{4}u^6 + \cdots - \frac{1}{2}u - \frac{1}{4} \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = $-2u^7 - 2u^6 - 13u^5 - 15u^4 - 25u^3 - 30u^2 - 12u + 1$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|---|
| c_1, c_3, c_4 c_7, c_8 | $u^8 + 7u^6 + u^5 + 14u^4 + 4u^3 + 5u^2 - u + 1$ |
| c_2 | $u^8 + 14u^7 + 77u^6 + 205u^5 + 260u^4 + 140u^3 + 61u^2 + 9u + 1$ |
| c_5, c_6, c_{10} c_{11} | $u^8 + 3u^7 + 9u^6 + 16u^5 + 23u^4 + 24u^3 + 18u^2 + 7u + 2$ |
| c_9 | $u^8 + u^7 + 21u^6 + 24u^5 + 109u^4 + 142u^3 - 10u^2 - 23u + 24$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1, c_3, c_4 c_7, c_8 | $y^8 + 14y^7 + 77y^6 + 205y^5 + 260y^4 + 140y^3 + 61y^2 + 9y + 1$ |
| c_2 | $y^8 - 42y^7 + \dots + 41y + 1$ |
| c_5, c_6, c_{10} c_{11} | $y^8 + 9y^7 + 31y^6 + 50y^5 + 47y^4 + 64y^3 + 80y^2 + 23y + 4$ |
| c_9 | $y^8 + 41y^7 + \dots - 1009y + 576$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.405950 + 0.590547I$ | | |
| $a = 1.00000$ | $6.99421 - 1.46497I$ | $5.63406 + 4.72165I$ |
| $b = -0.00585 - 1.54991I$ | | |
| $u = -0.405950 - 0.590547I$ | | |
| $a = 1.00000$ | $6.99421 + 1.46497I$ | $5.63406 - 4.72165I$ |
| $b = -0.00585 + 1.54991I$ | | |
| $u = 0.195934 + 0.349055I$ | | |
| $a = 1.00000$ | $0.133570 + 0.902562I$ | $2.84755 - 7.78366I$ |
| $b = -0.218002 + 0.455338I$ | | |
| $u = 0.195934 - 0.349055I$ | | |
| $a = 1.00000$ | $0.133570 - 0.902562I$ | $2.84755 + 7.78366I$ |
| $b = -0.218002 - 0.455338I$ | | |
| $u = 0.33222 + 1.78481I$ | | |
| $a = 1.00000$ | $-9.04281 + 7.80349I$ | $0.02756 - 3.21559I$ |
| $b = -0.34865 + 1.60107I$ | | |
| $u = 0.33222 - 1.78481I$ | | |
| $a = 1.00000$ | $-9.04281 - 7.80349I$ | $0.02756 + 3.21559I$ |
| $b = -0.34865 - 1.60107I$ | | |
| $u = -0.12220 + 1.91634I$ | | |
| $a = 1.00000$ | $-16.1792 - 3.0379I$ | $-2.50917 + 2.22003I$ |
| $b = -0.927504 - 0.597003I$ | | |
| $u = -0.12220 - 1.91634I$ | | |
| $a = 1.00000$ | $-16.1792 + 3.0379I$ | $-2.50917 - 2.22003I$ |
| $b = -0.927504 + 0.597003I$ | | |

$$\text{II. } I_2^u = \langle -u^5 + 2u^4 - u^3 + 5u^2 + 5b - u, u^5 + 2u^3 + 2u^2 + 5a + u + 7, u^6 - u^5 + 4u^4 - 4u^3 + 6u^2 - 4u + 5 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -\frac{1}{5}u^5 - \frac{2}{5}u^3 + \dots - \frac{1}{5}u - \frac{7}{5} \\ \frac{1}{5}u^5 - \frac{2}{5}u^4 + \frac{1}{5}u^3 - u^2 + \frac{1}{5}u \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{1}{5}u^5 - \frac{2}{5}u^3 + \dots - \frac{1}{5}u - \frac{7}{5} \\ -1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -\frac{2}{5}u^4 - \frac{1}{5}u^3 - \frac{7}{5}u^2 - \frac{7}{5} \\ \frac{1}{5}u^5 - \frac{2}{5}u^4 + \frac{1}{5}u^3 - u^2 + \frac{1}{5}u \end{pmatrix} \\ a_6 &= \begin{pmatrix} \frac{2}{5}u^5 - \frac{2}{5}u^4 + \dots + \frac{7}{5}u - \frac{8}{5} \\ \frac{3}{5}u^5 - \frac{4}{5}u^4 + \dots + \frac{7}{5}u - 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{1}{5}u^5 - \frac{1}{5}u^4 + \dots + \frac{6}{5}u - \frac{4}{5} \\ \frac{1}{5}u^5 - \frac{2}{5}u^4 + \dots + \frac{6}{5}u - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{2}{5}u^5 - \frac{3}{5}u^4 + \dots + \frac{12}{5}u - \frac{9}{5} \\ \frac{1}{5}u^5 - \frac{2}{5}u^4 + \dots + \frac{6}{5}u - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{2}{5}u^5 - \frac{3}{5}u^4 + \dots + \frac{12}{5}u - \frac{9}{5} \\ \frac{1}{5}u^5 - \frac{2}{5}u^4 + \dots + \frac{6}{5}u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-\frac{4}{5}u^5 + \frac{8}{5}u^4 - \frac{24}{5}u^3 + 4u^2 - \frac{24}{5}u + 2$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|---|
| c_1, c_3, c_4 c_7, c_8 | $u^6 - u^5 + 4u^4 - 4u^3 + 6u^2 - 4u + 5$ |
| c_2 | $u^6 + 7u^5 + 20u^4 + 34u^3 + 44u^2 + 44u + 25$ |
| c_5, c_6, c_{10} c_{11} | $(u^3 - u^2 + 2u - 1)^2$ |
| c_9 | $(u^3 - u^2 + 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1, c_3, c_4 c_7, c_8 | $y^6 + 7y^5 + 20y^4 + 34y^3 + 44y^2 + 44y + 25$ |
| c_2 | $y^6 - 9y^5 + 12y^4 + 38y^3 - 56y^2 + 264y + 625$ |
| c_5, c_6, c_{10} c_{11} | $(y^3 + 3y^2 + 2y - 1)^2$ |
| c_9 | $(y^3 - y^2 + 2y - 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|----------------------|
| $u = 0.862082 + 0.785389I$ | $-0.26574 + 2.82812I$ | $1.50976 - 2.97945I$ |
| $a = -0.873959 - 0.978854I$ | | |
| $b = 0.215080 - 1.307140I$ | | |
| $u = 0.862082 - 0.785389I$ | $-0.26574 - 2.82812I$ | $1.50976 + 2.97945I$ |
| $a = -0.873959 + 0.978854I$ | | |
| $b = 0.215080 + 1.307140I$ | | |
| $u = -0.377439 + 1.194730I$ | -4.40332 | $-5.01951 + 0.I$ |
| $a = -0.818504 + 0.574501I$ | | |
| $b = 0.569840$ | | |
| $u = -0.377439 - 1.194730I$ | -4.40332 | $-5.01951 + 0.I$ |
| $a = -0.818504 - 0.574501I$ | | |
| $b = 0.569840$ | | |
| $u = 0.01536 + 1.53025I$ | $-0.26574 - 2.82812I$ | $1.50976 + 2.97945I$ |
| $a = -0.507537 - 0.568454I$ | | |
| $b = 0.215080 + 1.307140I$ | | |
| $u = 0.01536 - 1.53025I$ | $-0.26574 + 2.82812I$ | $1.50976 - 2.97945I$ |
| $a = -0.507537 + 0.568454I$ | | |
| $b = 0.215080 - 1.307140I$ | | |

$$\text{III. } I_3^u = \langle b^2 + bu + 1, \ a + 1, \ u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1 \\ b \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0 \\ -1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -1 \\ b-1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} b-1 \\ b \end{pmatrix} \\ a_6 &= \begin{pmatrix} -bu-b \\ -bu-1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} bu+u \\ -b+u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ bu \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ bu \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--------------------------------|
| c_1, c_3, c_4 c_7, c_8 | $(u^2 + 1)^2$ |
| c_2 | $(u + 1)^4$ |
| c_5, c_6, c_{10} c_{11} | $u^4 + 3u^2 + 1$ |
| c_9 | $(u^2 - u - 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|------------------------------------|
| c_1, c_3, c_4 c_7, c_8 | $(y + 1)^4$ |
| c_2 | $(y - 1)^4$ |
| c_5, c_6, c_{10} c_{11} | $(y^2 + 3y + 1)^2$ |
| c_9 | $(y^2 - 3y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = 1.000000I$ | | |
| $a = -1.00000$ | -2.30291 | 0 |
| $b = 0.618034I$ | | |
| $u = 1.000000I$ | | |
| $a = -1.00000$ | 5.59278 | 0 |
| $b = -1.61803I$ | | |
| $u = -1.000000I$ | | |
| $a = -1.00000$ | -2.30291 | 0 |
| $b = -0.618034I$ | | |
| $u = -1.000000I$ | | |
| $a = -1.00000$ | 5.59278 | 0 |
| $b = 1.61803I$ | | |

IV. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_3, c_4 c_7, c_8 | $(u^2 + 1)^2(u^6 - u^5 + 4u^4 - 4u^3 + 6u^2 - 4u + 5)$ $\cdot (u^8 + 7u^6 + u^5 + 14u^4 + 4u^3 + 5u^2 - u + 1)$ |
| c_2 | $(u + 1)^4(u^6 + 7u^5 + 20u^4 + 34u^3 + 44u^2 + 44u + 25)$ $\cdot (u^8 + 14u^7 + 77u^6 + 205u^5 + 260u^4 + 140u^3 + 61u^2 + 9u + 1)$ |
| c_5, c_6, c_{10} c_{11} | $(u^3 - u^2 + 2u - 1)^2(u^4 + 3u^2 + 1)$ $\cdot (u^8 + 3u^7 + 9u^6 + 16u^5 + 23u^4 + 24u^3 + 18u^2 + 7u + 2)$ |
| c_9 | $(u^2 - u - 1)^2(u^3 - u^2 + 1)^2$ $\cdot (u^8 + u^7 + 21u^6 + 24u^5 + 109u^4 + 142u^3 - 10u^2 - 23u + 24)$ |

V. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_3, c_4 c_7, c_8 | $(y+1)^4(y^6 + 7y^5 + 20y^4 + 34y^3 + 44y^2 + 44y + 25)$ $\cdot (y^8 + 14y^7 + 77y^6 + 205y^5 + 260y^4 + 140y^3 + 61y^2 + 9y + 1)$ |
| c_2 | $(y-1)^4(y^6 - 9y^5 + 12y^4 + 38y^3 - 56y^2 + 264y + 625)$ $\cdot (y^8 - 42y^7 + \dots + 41y + 1)$ |
| c_5, c_6, c_{10} c_{11} | $(y^2 + 3y + 1)^2(y^3 + 3y^2 + 2y - 1)^2$ $\cdot (y^8 + 9y^7 + 31y^6 + 50y^5 + 47y^4 + 64y^3 + 80y^2 + 23y + 4)$ |
| c_9 | $((y^2 - 3y + 1)^2)(y^3 - y^2 + 2y - 1)^2(y^8 + 41y^7 + \dots - 1009y + 576)$ |