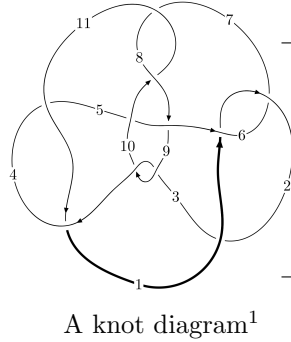
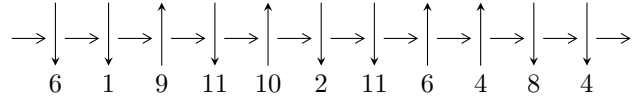


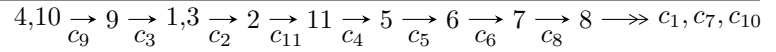
$11n_{143}$  ( $K11n_{143}$ )



**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 27169327131u^{12} - 4728521972u^{11} + \dots + 163375109309b + 102043710068, \\ 46748483168u^{12} - 1185808565u^{11} + \dots + 163375109309a - 246903703505, \\ u^{13} - u^{12} - 16u^{11} + 13u^{10} + 93u^9 - 90u^8 + 85u^7 - 4u^6 + 11u^5 - 20u^4 + 2u^2 + u - 1 \rangle$$

$$I_2^u = \langle 3u^8 - 5u^6 - u^5 - 7u^4 - 6u^3 + b - 3u + 2, -2u^8 + u^7 + 3u^6 - u^5 + 4u^4 + 3u^3 - u^2 + a + 2u - 1, \\ u^9 - u^7 - 3u^5 - 3u^4 - 2u^3 - 3u^2 - u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 22 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 2.72 \times 10^{10} u^{12} - 4.73 \times 10^9 u^{11} + \dots + 1.63 \times 10^{11} b + 1.02 \times 10^{11}, 4.67 \times 10^{10} u^{12} - 1.19 \times 10^9 u^{11} + \dots + 1.63 \times 10^{11} a - 2.47 \times 10^{11}, u^{13} - u^{12} + \dots + u - 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.286142u^{12} + 0.00725820u^{11} + \dots + 0.326465u + 1.51127 \\ -0.166300u^{12} + 0.0289427u^{11} + \dots - 0.0380012u - 0.624598 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.45178u^{12} + 1.36239u^{11} + \dots - 1.27398u - 1.38184 \\ -0.0325056u^{12} + 0.182051u^{11} + \dots - 1.79766u - 0.0596779 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.286142u^{12} + 0.00725820u^{11} + \dots + 0.326465u + 1.51127 \\ -0.0919107u^{12} + 0.0169286u^{11} + \dots - 0.0307430u - 0.345714 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1.39226u^{12} - 1.21256u^{11} + \dots - 1.08841u + 1.29245 \\ 0.0595160u^{12} - 0.149831u^{11} + \dots + 2.36239u + 0.0893943 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.45178u^{12} - 1.36239u^{11} + \dots + 1.27398u + 1.38184 \\ 0.0595160u^{12} - 0.149831u^{11} + \dots + 2.36239u + 0.0893943 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.286142u^{12} - 0.00725820u^{11} + \dots - 0.326465u - 1.51127 \\ 0.0289310u^{12} + 0.00713908u^{11} + \dots + 0.000702000u + 0.287036 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0893943u^{12} - 0.0298782u^{11} + \dots - 0.0699394u + 2.45178 \\ -0.0903148u^{12} + 0.0234848u^{11} + \dots + 0.0298782u + 0.0595160 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0893943u^{12} - 0.0298782u^{11} + \dots - 0.0699394u + 2.45178 \\ -0.0903148u^{12} + 0.0234848u^{11} + \dots + 0.0298782u + 0.0595160 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{425649841644}{163375109309} u^{12} + \frac{257561868150}{163375109309} u^{11} + \dots + \frac{821280596494}{163375109309} u - \frac{283918679660}{163375109309}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{13} - 11u^{12} + \dots - 48u + 16$
$c_2$	$u^{13} + 7u^{12} + \dots - 640u + 256$
$c_3, c_8, c_9$	$u^{13} + u^{12} + \dots + u + 1$
$c_4, c_{11}$	$u^{13} - 3u^{12} + \dots - 2u + 1$
$c_5$	$u^{13} - 14u^{11} + \dots + 13u + 6$
$c_7, c_{10}$	$u^{13} - 3u^{12} + \dots + 3u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{13} - 7y^{12} + \dots - 640y - 256$
$c_2$	$y^{13} + 69y^{12} + \dots - 106496y - 65536$
$c_3, c_8, c_9$	$y^{13} - 33y^{12} + \dots + 5y - 1$
$c_4, c_{11}$	$y^{13} + 27y^{12} + \dots - 34y - 1$
$c_5$	$y^{13} - 28y^{12} + \dots - 83y - 36$
$c_7, c_{10}$	$y^{13} + y^{12} + \dots - y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.444507 + 0.873153I$ $a = 0.145964 + 0.210434I$ $b = -0.10255 - 2.20008I$	$-5.13656 + 3.94627I$	$0.021726 + 1.151779I$
$u = 0.444507 - 0.873153I$ $a = 0.145964 - 0.210434I$ $b = -0.10255 + 2.20008I$	$-5.13656 - 3.94627I$	$0.021726 - 1.151779I$
$u = -0.278059 + 0.532845I$ $a = 0.482522 - 0.330538I$ $b = -0.243913 + 0.386628I$	$-0.112278 - 1.172770I$	$-1.56848 + 5.39486I$
$u = -0.278059 - 0.532845I$ $a = 0.482522 + 0.330538I$ $b = -0.243913 - 0.386628I$	$-0.112278 + 1.172770I$	$-1.56848 - 5.39486I$
$u = 0.581027$ $a = 1.33008$ $b = 0.743719$	$-1.77301$	$-4.59260$
$u = -0.395821 + 0.255747I$ $a = 1.63033 - 1.89256I$ $b = -0.681021 - 0.928853I$	$3.39477 - 1.45394I$	$0.239284 + 0.384387I$
$u = -0.395821 - 0.255747I$ $a = 1.63033 + 1.89256I$ $b = -0.681021 + 0.928853I$	$3.39477 + 1.45394I$	$0.239284 - 0.384387I$
$u = 0.364118 + 0.280685I$ $a = 2.64015 + 1.42143I$ $b = -0.470210 + 1.143350I$	$3.10631 - 4.18292I$	$3.50367 + 6.73830I$
$u = 0.364118 - 0.280685I$ $a = 2.64015 - 1.42143I$ $b = -0.470210 - 1.143350I$	$3.10631 + 4.18292I$	$3.50367 - 6.73830I$
$u = -3.02519 + 1.05130I$ $a = 0.060075 + 0.847736I$ $b = 6.04324 + 4.26131I$	$16.1187 - 1.6452I$	$-0.771905 + 0.029863I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -3.02519 - 1.05130I$		
$a = 0.060075 - 0.847736I$	$16.1187 + 1.6452I$	$-0.771905 - 0.029863I$
$b = 6.04324 - 4.26131I$		
$u = 3.09993 + 0.83578I$		
$a = -0.124080 + 0.900887I$	$16.4142 + 9.3138I$	$-0.62797 - 3.85299I$
$b = -5.91741 + 5.22009I$		
$u = 3.09993 - 0.83578I$		
$a = -0.124080 - 0.900887I$	$16.4142 - 9.3138I$	$-0.62797 + 3.85299I$
$b = -5.91741 - 5.22009I$		

$$\text{II. } I_2^u = \langle 3u^8 - 5u^6 - u^5 - 7u^4 - 6u^3 + b - 3u + 2, -2u^8 + u^7 + \dots + a - 1, u^9 - u^7 - 3u^5 - 3u^4 - 2u^3 - 3u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 2u^8 - u^7 - 3u^6 + u^5 - 4u^4 - 3u^3 + u^2 - 2u + 1 \\ -3u^8 + 5u^6 + u^5 + 7u^4 + 6u^3 + 3u - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^7 + 2u^5 + u^3 + 3u^2 + 1 \\ -3u^8 + 5u^6 + u^5 + 7u^4 + 6u^3 + 2u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2u^8 - u^7 - 3u^6 + u^5 - 4u^4 - 3u^3 + u^2 - 2u + 1 \\ -2u^8 + 3u^6 + u^5 + 5u^4 + 4u^3 + 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2u^7 - 4u^5 - 3u^3 - 5u^2 - 2 \\ -u^7 + 2u^5 + 2u^3 + 2u^2 + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^7 - 2u^5 - u^3 - 3u^2 - 1 \\ -u^7 + 2u^5 + 2u^3 + 2u^2 + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2u^8 + u^7 + 3u^6 - u^5 + 4u^4 + 3u^3 - u^2 + 2u - 1 \\ 3u^8 + u^7 - 4u^6 - 3u^5 - 9u^4 - 8u^3 - 3u^2 - 4u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^8 + 2u^6 + u^4 + 3u^3 + u + 1 \\ u^8 - 2u^6 - 2u^4 - 2u^3 + u^2 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^8 + 2u^6 + u^4 + 3u^3 + u + 1 \\ u^8 - 2u^6 - 2u^4 - 2u^3 + u^2 - u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -11u^8 - 6u^7 + 11u^6 + 15u^5 + 36u^4 + 40u^3 + 29u^2 + 19u + 4$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^9 + u^8 - 3u^7 - 5u^6 + 2u^5 + 8u^4 + u^3 - 4u^2 - u + 1$
$c_2$	$u^9 + 7u^8 + 23u^7 + 51u^6 + 84u^5 + 96u^4 + 71u^3 + 34u^2 + 9u + 1$
$c_3, c_8$	$u^9 - u^7 - 3u^5 + 3u^4 - 2u^3 + 3u^2 - u + 1$
$c_4$	$u^9 + 2u^8 + 3u^7 + 3u^6 + u^5 + u^4 + u^3 - 2u^2 + 1$
$c_5$	$u^9 + u^8 + 2u^5 + 5u^4 + 4u^3 + 3u^2 + 2u + 1$
$c_6$	$u^9 - u^8 - 3u^7 + 5u^6 + 2u^5 - 8u^4 + u^3 + 4u^2 - u - 1$
$c_7$	$u^9 - 4u^8 + 8u^7 - 8u^6 + 4u^5 + u^4 - 3u^3 + 4u^2 - 3u + 1$
$c_9$	$u^9 - u^7 - 3u^5 - 3u^4 - 2u^3 - 3u^2 - u - 1$
$c_{10}$	$u^9 + 4u^8 + 8u^7 + 8u^6 + 4u^5 - u^4 - 3u^3 - 4u^2 - 3u - 1$
$c_{11}$	$u^9 - 2u^8 + 3u^7 - 3u^6 + u^5 - u^4 + u^3 + 2u^2 - 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^9 - 7y^8 + 23y^7 - 51y^6 + 84y^5 - 96y^4 + 71y^3 - 34y^2 + 9y - 1$
$c_2$	$y^9 - 3y^8 - 17y^7 + 61y^6 + 72y^5 - 356y^4 - 77y^3 - 70y^2 + 13y - 1$
$c_3, c_8, c_9$	$y^9 - 2y^8 - 5y^7 + 2y^6 + 11y^5 + 5y^4 - 8y^3 - 11y^2 - 5y - 1$
$c_4, c_{11}$	$y^9 + 2y^8 - y^7 - 5y^6 + 9y^5 + 9y^4 - y^3 - 6y^2 + 4y - 1$
$c_5$	$y^9 - y^8 + 4y^7 - 2y^6 + 2y^5 - 11y^4 - 6y^3 - 3y^2 - 2y - 1$
$c_7, c_{10}$	$y^9 + 8y^7 + 2y^6 + 10y^5 - y^4 - 7y^3 + y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.187026 + 0.975482I$ $a = 1.49016 - 0.14200I$ $b = -1.04647 + 1.04626I$	$2.30462 - 3.49273I$	$-2.36810 + 1.84153I$
$u = 0.187026 - 0.975482I$ $a = 1.49016 + 0.14200I$ $b = -1.04647 - 1.04626I$	$2.30462 + 3.49273I$	$-2.36810 - 1.84153I$
$u = 0.371524 + 0.883251I$ $a = 0.023313 + 0.680902I$ $b = -0.23136 - 2.96704I$	$-5.46047 + 4.24647I$	$-14.3219 - 11.0959I$
$u = 0.371524 - 0.883251I$ $a = 0.023313 - 0.680902I$ $b = -0.23136 + 2.96704I$	$-5.46047 - 4.24647I$	$-14.3219 + 11.0959I$
$u = -1.182340 + 0.166435I$ $a = 0.381598 - 0.765916I$ $b = -0.406219 - 0.959782I$	$4.76964 - 2.24591I$	$6.27523 + 4.01918I$
$u = -1.182340 - 0.166435I$ $a = 0.381598 + 0.765916I$ $b = -0.406219 + 0.959782I$	$4.76964 + 2.24591I$	$6.27523 - 4.01918I$
$u = -0.245900 + 0.620274I$ $a = -0.08889 - 1.83830I$ $b = -0.76587 + 2.09421I$	$-2.24646 - 2.97681I$	$0.11269 + 3.28969I$
$u = -0.245900 - 0.620274I$ $a = -0.08889 + 1.83830I$ $b = -0.76587 - 2.09421I$	$-2.24646 + 2.97681I$	$0.11269 - 3.28969I$
$u = 1.73938$ $a = 0.387642$ $b = 1.89983$	$1.26533$	$-2.39580$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^9 + u^8 - 3u^7 - 5u^6 + 2u^5 + 8u^4 + u^3 - 4u^2 - u + 1)$ $\cdot (u^{13} - 11u^{12} + \dots - 48u + 16)$
$c_2$	$(u^9 + 7u^8 + 23u^7 + 51u^6 + 84u^5 + 96u^4 + 71u^3 + 34u^2 + 9u + 1)$ $\cdot (u^{13} + 7u^{12} + \dots - 640u + 256)$
$c_3, c_8$	$(u^9 - u^7 + \dots - u + 1)(u^{13} + u^{12} + \dots + u + 1)$
$c_4$	$(u^9 + 2u^8 + \dots - 2u^2 + 1)(u^{13} - 3u^{12} + \dots - 2u + 1)$
$c_5$	$(u^9 + u^8 + \dots + 2u + 1)(u^{13} - 14u^{11} + \dots + 13u + 6)$
$c_6$	$(u^9 - u^8 - 3u^7 + 5u^6 + 2u^5 - 8u^4 + u^3 + 4u^2 - u - 1)$ $\cdot (u^{13} - 11u^{12} + \dots - 48u + 16)$
$c_7$	$(u^9 - 4u^8 + 8u^7 - 8u^6 + 4u^5 + u^4 - 3u^3 + 4u^2 - 3u + 1)$ $\cdot (u^{13} - 3u^{12} + \dots + 3u - 1)$
$c_9$	$(u^9 - u^7 + \dots - u - 1)(u^{13} + u^{12} + \dots + u + 1)$
$c_{10}$	$(u^9 + 4u^8 + 8u^7 + 8u^6 + 4u^5 - u^4 - 3u^3 - 4u^2 - 3u - 1)$ $\cdot (u^{13} - 3u^{12} + \dots + 3u - 1)$
$c_{11}$	$(u^9 - 2u^8 + \dots + 2u^2 - 1)(u^{13} - 3u^{12} + \dots - 2u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$(y^9 - 7y^8 + 23y^7 - 51y^6 + 84y^5 - 96y^4 + 71y^3 - 34y^2 + 9y - 1)$ $\cdot (y^{13} - 7y^{12} + \dots - 640y - 256)$
$c_2$	$(y^9 - 3y^8 - 17y^7 + 61y^6 + 72y^5 - 356y^4 - 77y^3 - 70y^2 + 13y - 1)$ $\cdot (y^{13} + 69y^{12} + \dots - 106496y - 65536)$
$c_3, c_8, c_9$	$(y^9 - 2y^8 - 5y^7 + 2y^6 + 11y^5 + 5y^4 - 8y^3 - 11y^2 - 5y - 1)$ $\cdot (y^{13} - 33y^{12} + \dots + 5y - 1)$
$c_4, c_{11}$	$(y^9 + 2y^8 - y^7 - 5y^6 + 9y^5 + 9y^4 - y^3 - 6y^2 + 4y - 1)$ $\cdot (y^{13} + 27y^{12} + \dots - 34y - 1)$
$c_5$	$(y^9 - y^8 + 4y^7 - 2y^6 + 2y^5 - 11y^4 - 6y^3 - 3y^2 - 2y - 1)$ $\cdot (y^{13} - 28y^{12} + \dots - 83y - 36)$
$c_7, c_{10}$	$(y^9 + 8y^7 + \dots + y - 1)(y^{13} + y^{12} + \dots - y - 1)$