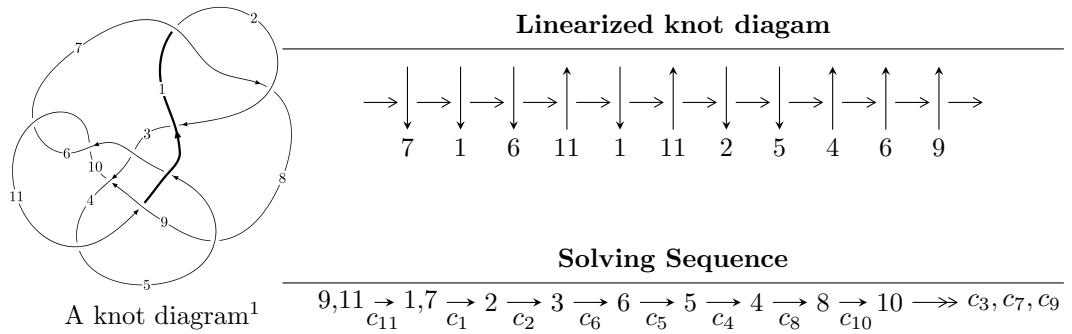


11n<sub>145</sub> ( $K11n_{145}$ )



## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle u^{11} + u^{10} + 2u^9 + u^8 + 4u^7 + 2u^6 + 3u^5 - u^4 + u^3 + 2u^2 + b + 2u + 1, \\ 3u^{11} + 5u^{10} + 6u^9 + 3u^8 + 12u^7 + 11u^6 + 6u^5 - 6u^4 + 5u^3 + 8u^2 + a + 8u + 2, \\ u^{12} + 2u^{11} + 3u^{10} + 2u^9 + 5u^8 + 5u^7 + 5u^6 - u^5 + 2u^4 + 2u^3 + 5u^2 + 2u + 1 \rangle$$

$$I_2^u = \langle u^6 - 2u^5 + 2u^4 + b - u + 1, -2u^7 + 6u^6 - 9u^5 + 5u^4 - 2u^3 + 4u^2 + a - 7u + 2, \\ u^8 - 3u^7 + 5u^6 - 4u^5 + 3u^4 - 3u^3 + 4u^2 - 2u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 20 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILS/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{11} + u^{10} + \dots + b + 1, \ 3u^{11} + 5u^{10} + \dots + a + 2, \ u^{12} + 2u^{11} + \dots + 2u + 1 \rangle^{\text{I.}}$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -3u^{11} - 5u^{10} + \dots - 8u - 2 \\ -u^{11} - u^{10} - 2u^9 - u^8 - 4u^7 - 2u^6 - 3u^5 + u^4 - u^3 - 2u^2 - 2u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^{11} - 3u^{10} + \dots - 2u - 1 \\ -u^{11} - u^9 - 3u^7 + u^6 - u^5 + u^4 - u^3 - 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2u^{11} - 2u^{10} - 3u^9 - 8u^7 - 3u^6 - 3u^5 + 6u^4 - 7u^3 - 3u^2 - 2u \\ u^{11} + u^{10} + 2u^9 + u^8 + 4u^7 + 2u^6 + 3u^5 - u^4 + u^3 + 2u^2 + 2u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2u^{11} - 4u^{10} + \dots - 6u - 1 \\ -u^{11} - u^{10} - 2u^9 - u^8 - 4u^7 - 2u^6 - 3u^5 + u^4 - u^3 - 2u^2 - 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{11} - 3u^{10} - 4u^9 - 2u^8 - 5u^7 - 8u^6 - 6u^5 + 4u^4 - u^3 - 5u^2 - 6u - 2 \\ -2u^{10} - 2u^9 - 2u^8 - u^7 - 7u^6 - 3u^5 + 2u^3 - 4u^2 - 3u - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{11} - u^{10} - 2u^9 - 4u^7 - u^6 - 3u^5 + 4u^4 - 3u^3 - u^2 - 3u \\ -2u^{10} - 2u^9 - 2u^8 - u^7 - 7u^6 - 3u^5 + 2u^3 - 4u^2 - 3u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{11} + 2u^{10} + 2u^9 + 2u^8 + 3u^7 + 6u^6 + u^5 - u^3 + 6u^2 + u + 2 \\ u^{11} + u^{10} + 2u^9 + u^8 + 3u^7 + 3u^6 + 2u^5 - u^4 + 4u^2 + 2u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{11} - u^{10} - u^9 - u^8 - 3u^7 - 2u^6 - u^3 - 2u^2 - u \\ u^{11} + 2u^{10} + u^9 + 2u^8 + 3u^7 + 5u^6 - u^5 + u^4 + 4u^2 + 2u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{11} - u^{10} - u^9 - u^8 - 3u^7 - 2u^6 - u^3 - 2u^2 - u \\ u^{11} + 2u^{10} + u^9 + 2u^8 + 3u^7 + 5u^6 - u^5 + u^4 + 4u^2 + 2u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -3u^{11} - 7u^{10} - 8u^9 - 7u^8 - 14u^7 - 21u^6 - 8u^5 - u^3 - 16u^2 - 4u - 9$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^{12} - 11u^{11} + \cdots - 48u + 16$
$c_2$	$u^{12} + 9u^{11} + \cdots + 896u + 256$
$c_3$	$u^{12} - 4u^{11} + \cdots - 4u + 1$
$c_4$	$u^{12} - u^{11} + \cdots + 4u + 10$
$c_5, c_8$	$u^{12} + 2u^{11} + \cdots - 16u^2 + 1$
$c_6, c_9, c_{10}$	$u^{12} - 10u^{10} + \cdots - u + 1$
$c_{11}$	$u^{12} + 2u^{11} + \cdots + 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y^{12} - 9y^{11} + \cdots - 896y + 256$
$c_2$	$y^{12} + 59y^{11} + \cdots + 253952y + 65536$
$c_3$	$y^{12} - 30y^{11} + \cdots - 16y + 1$
$c_4$	$y^{12} - 25y^{11} + \cdots - 896y + 100$
$c_5, c_8$	$y^{12} + 26y^{11} + \cdots - 32y + 1$
$c_6, c_9, c_{10}$	$y^{12} - 20y^{11} + \cdots + 3y + 1$
$c_{11}$	$y^{12} + 2y^{11} + \cdots + 6y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.800801 + 0.482482I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.183380 + 0.498565I$	$1.43652 + 0.62326I$	$4.44877 + 0.65496I$
$b = 0.698671 + 0.235425I$		
$u = 0.800801 - 0.482482I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.183380 - 0.498565I$	$1.43652 - 0.62326I$	$4.44877 - 0.65496I$
$b = 0.698671 - 0.235425I$		
$u = -0.372107 + 0.751953I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.81363 + 1.82447I$	$-9.07675 - 1.52290I$	$-4.89097 + 7.64925I$
$b = 0.243009 + 0.355918I$		
$u = -0.372107 - 0.751953I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.81363 - 1.82447I$	$-9.07675 + 1.52290I$	$-4.89097 - 7.64925I$
$b = 0.243009 - 0.355918I$		
$u = 0.690074 + 1.109750I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.458254 - 0.957045I$	$-0.63619 + 5.03255I$	$-5.39872 - 6.82429I$
$b = -0.715998 - 0.535824I$		
$u = 0.690074 - 1.109750I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.458254 + 0.957045I$	$-0.63619 - 5.03255I$	$-5.39872 + 6.82429I$
$b = -0.715998 + 0.535824I$		
$u = -0.981759 + 0.915783I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.31213 - 0.66172I$	$11.48080 + 2.02735I$	$-0.446845 + 0.080322I$
$b = 2.49508 + 1.02200I$		
$u = -0.981759 - 0.915783I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.31213 + 0.66172I$	$11.48080 - 2.02735I$	$-0.446845 - 0.080322I$
$b = 2.49508 - 1.02200I$		
$u = -0.924436 + 1.006840I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.21708 + 2.14841I$	$11.1731 - 9.0121I$	$-0.90831 + 4.12550I$
$b = -2.45017 + 1.30392I$		
$u = -0.924436 - 1.006840I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.21708 - 2.14841I$	$11.1731 + 9.0121I$	$-0.90831 - 4.12550I$
$b = -2.45017 - 1.30392I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.212573 + 0.487267I$		
$a = 0.49344 - 1.36791I$	$-1.218070 - 0.691278I$	$-5.30392 + 1.72582I$
$b = -0.270602 - 0.384607I$		
$u = -0.212573 - 0.487267I$		
$a = 0.49344 + 1.36791I$	$-1.218070 + 0.691278I$	$-5.30392 - 1.72582I$
$b = -0.270602 + 0.384607I$		

II.

$$I_2^u = \langle u^6 - 2u^5 + 2u^4 + b - u + 1, -2u^7 + 6u^6 + \dots + a + 2, u^8 - 3u^7 + \dots - 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2u^7 - 6u^6 + 9u^5 - 5u^4 + 2u^3 - 4u^2 + 7u - 2 \\ -u^6 + 2u^5 - 2u^4 + u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -4u^7 + 11u^6 - 16u^5 + 9u^4 - 5u^3 + 8u^2 - 12u + 4 \\ -u^7 + 3u^6 - 5u^5 + 4u^4 - 2u^3 + u^2 - 3u + 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -4u^7 + 10u^6 - 14u^5 + 6u^4 - 4u^3 + 7u^2 - 11u + 1 \\ u^6 - 2u^5 + 2u^4 - u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2u^7 - 5u^6 + 7u^5 - 3u^4 + 2u^3 - 4u^2 + 6u - 1 \\ -u^6 + 2u^5 - 2u^4 + u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2u^7 - 6u^6 + 9u^5 - 6u^4 + 3u^3 - 5u^2 + 7u - 3 \\ u^7 - 3u^6 + 5u^5 - 4u^4 + 2u^3 - 2u^2 + 3u - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^7 - 3u^6 + 4u^5 - 2u^4 + u^3 - 3u^2 + 4u - 1 \\ u^7 - 3u^6 + 5u^5 - 4u^4 + 2u^3 - 2u^2 + 3u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -3u^7 + 9u^6 - 14u^5 + 9u^4 - 5u^3 + 7u^2 - 11u + 3 \\ -u^7 + 4u^6 - 7u^5 + 6u^4 - 3u^3 + 4u^2 - 5u + 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^7 + 2u^6 - 2u^5 - u^4 + u^3 - u - 1 \\ -u^7 + 3u^6 - 5u^5 + 4u^4 - 3u^3 + 3u^2 - 3u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^7 + 2u^6 - 2u^5 - u^4 + u^3 - u - 1 \\ -u^7 + 3u^6 - 5u^5 + 4u^4 - 3u^3 + 3u^2 - 3u + 1 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-2u^7 + 5u^5 - 11u^4 + 2u^3 - 4u^2 + 7u - 9$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^8 + u^7 - 4u^6 - 2u^5 + 7u^4 + u^3 - 5u^2 + 2$
$c_2$	$u^8 + 9u^7 + 34u^6 + 72u^5 + 97u^4 + 87u^3 + 53u^2 + 20u + 4$
$c_3$	$u^8 - 9u^7 + 31u^6 - 51u^5 + 42u^4 - 20u^3 + 9u^2 - 2u + 1$
$c_4$	$u^8 + u^6 + 2u^5 + 3u^4 + 3u^3 - u^2 + 2$
$c_5, c_8$	$u^8 - u^7 - u^6 - u^5 + 2u^4 + 2u^3 + 3u^2 + 2u + 1$
$c_6, c_9$	$u^8 - u^7 + 2u^6 - u^5 - u^4 + 3u^3 - u^2 - u + 1$
$c_7$	$u^8 - u^7 - 4u^6 + 2u^5 + 7u^4 - u^3 - 5u^2 + 2$
$c_{10}$	$u^8 + u^7 + 2u^6 + u^5 - u^4 - 3u^3 - u^2 + u + 1$
$c_{11}$	$u^8 - 3u^7 + 5u^6 - 4u^5 + 3u^4 - 3u^3 + 4u^2 - 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y^8 - 9y^7 + 34y^6 - 72y^5 + 97y^4 - 87y^3 + 53y^2 - 20y + 4$
$c_2$	$y^8 - 13y^7 + 54y^6 - 48y^5 + 133y^4 + 105y^3 + 105y^2 + 24y + 16$
$c_3$	$y^8 - 19y^7 + 127y^6 - 339y^5 + 248y^4 + 214y^3 + 85y^2 + 14y + 1$
$c_4$	$y^8 + 2y^7 + 7y^6 - y^4 - 11y^3 + 13y^2 - 4y + 4$
$c_5, c_8$	$y^8 - 3y^7 + 3y^6 + 5y^5 + 8y^4 + 10y^3 + 5y^2 + 2y + 1$
$c_6, c_9, c_{10}$	$y^8 + 3y^7 - y^5 + 3y^4 - 5y^3 + 5y^2 - 3y + 1$
$c_{11}$	$y^8 + y^7 + 7y^6 + 4y^5 + 15y^4 + 9y^3 + 10y^2 + 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.601219 + 0.700245I$		
$a = -1.25463 - 1.13763I$	$-5.61184 - 2.16662I$	$-1.31720 + 3.92427I$
$b = 0.04009 - 1.51942I$		
$u = -0.601219 - 0.700245I$		
$a = -1.25463 + 1.13763I$	$-5.61184 + 2.16662I$	$-1.31720 - 3.92427I$
$b = 0.04009 + 1.51942I$		
$u = 0.975658 + 0.743632I$		
$a = 0.205573 + 0.088262I$	$1.42321 + 1.81732I$	$3.74465 - 3.23500I$
$b = 0.804982 + 0.154967I$		
$u = 0.975658 - 0.743632I$		
$a = 0.205573 - 0.088262I$	$1.42321 - 1.81732I$	$3.74465 + 3.23500I$
$b = 0.804982 - 0.154967I$		
$u = 0.235731 + 0.563343I$		
$a = 0.73791 + 2.94527I$	$-9.14900 + 0.88713I$	$-6.29124 + 4.01225I$
$b = -0.641984 + 0.737766I$		
$u = 0.235731 - 0.563343I$		
$a = 0.73791 - 2.94527I$	$-9.14900 - 0.88713I$	$-6.29124 - 4.01225I$
$b = -0.641984 - 0.737766I$		
$u = 0.88983 + 1.14020I$		
$a = -0.188850 - 0.848475I$	$0.17815 + 5.07460I$	$4.36379 - 8.11889I$
$b = -0.703087 - 0.423228I$		
$u = 0.88983 - 1.14020I$		
$a = -0.188850 + 0.848475I$	$0.17815 - 5.07460I$	$4.36379 + 8.11889I$
$b = -0.703087 + 0.423228I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^8 + u^7 + \dots - 5u^2 + 2)(u^{12} - 11u^{11} + \dots - 48u + 16)$
$c_2$	$(u^8 + 9u^7 + 34u^6 + 72u^5 + 97u^4 + 87u^3 + 53u^2 + 20u + 4)$ $\cdot (u^{12} + 9u^{11} + \dots + 896u + 256)$
$c_3$	$(u^8 - 9u^7 + 31u^6 - 51u^5 + 42u^4 - 20u^3 + 9u^2 - 2u + 1)$ $\cdot (u^{12} - 4u^{11} + \dots - 4u + 1)$
$c_4$	$(u^8 + u^6 + 2u^5 + 3u^4 + 3u^3 - u^2 + 2)(u^{12} - u^{11} + \dots + 4u + 10)$
$c_5, c_8$	$(u^8 - u^7 - u^6 - u^5 + 2u^4 + 2u^3 + 3u^2 + 2u + 1)$ $\cdot (u^{12} + 2u^{11} + \dots - 16u^2 + 1)$
$c_6, c_9$	$(u^8 - u^7 + \dots - u + 1)(u^{12} - 10u^{10} + \dots - u + 1)$
$c_7$	$(u^8 - u^7 + \dots - 5u^2 + 2)(u^{12} - 11u^{11} + \dots - 48u + 16)$
$c_{10}$	$(u^8 + u^7 + \dots + u + 1)(u^{12} - 10u^{10} + \dots - u + 1)$
$c_{11}$	$(u^8 - 3u^7 + 5u^6 - 4u^5 + 3u^4 - 3u^3 + 4u^2 - 2u + 1)$ $\cdot (u^{12} + 2u^{11} + \dots + 2u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$(y^8 - 9y^7 + 34y^6 - 72y^5 + 97y^4 - 87y^3 + 53y^2 - 20y + 4) \cdot (y^{12} - 9y^{11} + \dots - 896y + 256)$
$c_2$	$(y^8 - 13y^7 + 54y^6 - 48y^5 + 133y^4 + 105y^3 + 105y^2 + 24y + 16) \cdot (y^{12} + 59y^{11} + \dots + 253952y + 65536)$
$c_3$	$(y^8 - 19y^7 + 127y^6 - 339y^5 + 248y^4 + 214y^3 + 85y^2 + 14y + 1) \cdot (y^{12} - 30y^{11} + \dots - 16y + 1)$
$c_4$	$(y^8 + 2y^7 + 7y^6 - y^4 - 11y^3 + 13y^2 - 4y + 4) \cdot (y^{12} - 25y^{11} + \dots - 896y + 100)$
$c_5, c_8$	$(y^8 - 3y^7 + 3y^6 + 5y^5 + 8y^4 + 10y^3 + 5y^2 + 2y + 1) \cdot (y^{12} + 26y^{11} + \dots - 32y + 1)$
$c_6, c_9, c_{10}$	$(y^8 + 3y^7 + \dots - 3y + 1)(y^{12} - 20y^{11} + \dots + 3y + 1)$
$c_{11}$	$(y^8 + y^7 + 7y^6 + 4y^5 + 15y^4 + 9y^3 + 10y^2 + 4y + 1) \cdot (y^{12} + 2y^{11} + \dots + 6y + 1)$