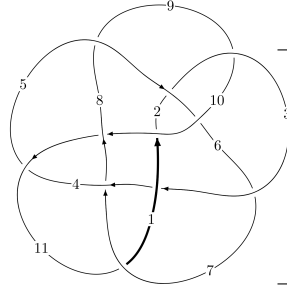
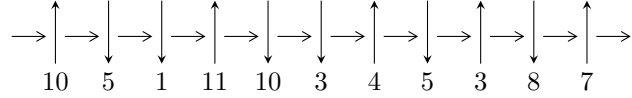


$11n_{156}$ ($K11n_{156}$)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$4, 11 \xrightarrow{c_4} 5, 7 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 1 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_6} 6 \xrightarrow{c_{10}} 10 \xrightarrow{c_9} 9 \longrightarrow c_1, c_5, c_8$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 286u^{13} + 1025u^{12} + \dots + 189b + 494, a - 1, 2u^{14} + 3u^{13} + 6u^{12} + u^{11} + 11u^{10} + 5u^9 + 20u^8 - 2u^7 + 15u^6 - 5u^5 + 11u^4 - 7u^3 + 7u^2 - 3u + 1 \rangle$$

$$I_2^u = \langle 2u^7 - 14u^6 - 8u^5 - 21u^4 + 25u^3 - 19u^2 + 9b + 30u - 14, a + 1, 2u^8 + 2u^6 - 5u^5 + 4u^4 - 6u^3 + 5u^2 - 2u + 1 \rangle$$

$$I_3^u = \langle -1.76422 \times 10^{54}u^{35} - 3.41094 \times 10^{54}u^{34} + \dots + 1.61573 \times 10^{53}b + 2.47914 \times 10^{53}, 3.12290 \times 10^{54}u^{35} + 4.43281 \times 10^{54}u^{34} + \dots + 2.30819 \times 10^{52}a - 3.74791 \times 10^{54}, 2u^{36} + 2u^{35} + \dots - 14u + 1 \rangle$$

$$I_4^u = \langle 4u^3 + 6u^2 + 3b + 4u + 1, 4u^3 + 12u^2 + 3a + 10u + 1, 2u^4 + 4u^3 + 2u^2 + 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 62 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew (<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose (<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 286u^{13} + 1025u^{12} + \dots + 189b + 494, a - 1, 2u^{14} + 3u^{13} + \dots - 3u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1.51323u^{13} - 5.42328u^{12} + \dots - 0.164021u - 2.61376 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1.51323u^{13} - 5.42328u^{12} + \dots - 0.164021u - 1.61376 \\ -1.51323u^{13} - 5.42328u^{12} + \dots - 0.164021u - 2.61376 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -3.15344u^{13} - 6.81481u^{12} + \dots - 3.88360u + 0.756614 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2.08466u^{13} + 3.32804u^{12} + \dots + 3.97354u - 0.576720 \\ 2.06349u^{13} + 2.26984u^{12} + \dots + 5.63492u - 2.73016 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 3.56614u^{13} + 4.35450u^{12} + \dots + 8.86772u - 3.40741 \\ 3.43915u^{13} + 4.67196u^{12} + \dots + 8.16931u - 3.32804 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -4.79365u^{13} - 11.9206u^{12} + \dots - 4.74603u - 0.777778 \\ -5.22751u^{13} - 10.4550u^{12} + \dots - 8.65608u + 1.37037 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -5.46032u^{13} - 10.2540u^{12} + \dots - 9.41270u + 2.55556 \\ -2.30688u^{13} - 3.43915u^{12} + \dots - 4.52910u + 1.79894 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2.08466u^{13} + 3.32804u^{12} + \dots + 3.97354u - 0.576720 \\ -3.01587u^{13} - 7.50794u^{12} + \dots - 3.39683u - 0.936508 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2.08466u^{13} + 3.32804u^{12} + \dots + 3.97354u - 0.576720 \\ -3.01587u^{13} - 7.50794u^{12} + \dots - 3.39683u - 0.936508 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{136}{27}u^{13} - \frac{1550}{189}u^{12} - \frac{2491}{189}u^{11} + \frac{248}{189}u^{10} - \frac{1103}{63}u^9 - \frac{2428}{189}u^8 - \frac{2563}{63}u^7 + \frac{1360}{189}u^6 - \frac{1738}{189}u^5 + \frac{1937}{189}u^4 - \frac{1363}{63}u^3 - \frac{16}{27}u^2 - \frac{2242}{189}u - \frac{176}{189}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1 | $4(4u^{14} + 43u^{13} + \dots + 336u + 64)$ |
| c_2, c_5 | $2(2u^{14} - u^{13} + \dots + 9u^2 + 1)$ |
| c_3, c_{10} | $u^{14} - 2u^{13} + \dots - 3u + 2$ |
| c_4, c_{11} | $2(2u^{14} - 3u^{13} + \dots + 3u + 1)$ |
| c_6, c_8 | $u^{14} - u^{13} + \dots - 13u + 2$ |
| c_7 | $u^{14} - 9u^{13} + \dots - 24u + 8$ |
| c_9 | $u^{14} - 10u^{13} + \dots - 80u + 32$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|--|
| c_1 | $16(16y^{14} - 105y^{13} + \dots + 16128y + 4096)$ |
| c_2, c_5 | $4(4y^{14} + 83y^{13} + \dots + 18y + 1)$ |
| c_3, c_{10} | $y^{14} + 4y^{13} + \dots - 5y + 4$ |
| c_4, c_{11} | $4(4y^{14} + 15y^{13} + \dots + 5y + 1)$ |
| c_6, c_8 | $y^{14} + 7y^{13} + \dots - 33y + 4$ |
| c_7 | $y^{14} + 3y^{13} + \dots - 96y + 64$ |
| c_9 | $y^{14} - 10y^{13} + \dots + 5376y + 1024$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.747471 + 0.736656I$ $a = 1.00000$ $b = -1.190140 + 0.650810I$ | $2.08139 - 2.02696I$ | $1.83038 + 2.57438I$ |
| $u = -0.747471 - 0.736656I$ $a = 1.00000$ $b = -1.190140 - 0.650810I$ | $2.08139 + 2.02696I$ | $1.83038 - 2.57438I$ |
| $u = 0.068372 + 0.773508I$ $a = 1.00000$ $b = 0.483737 - 0.312119I$ | $0.50090 - 2.66807I$ | $3.96052 + 3.99756I$ |
| $u = 0.068372 - 0.773508I$ $a = 1.00000$ $b = 0.483737 + 0.312119I$ | $0.50090 + 2.66807I$ | $3.96052 - 3.99756I$ |
| $u = 0.863068 + 0.906873I$ $a = 1.00000$ $b = -1.23002 - 1.06519I$ | $1.01240 + 7.85357I$ | $1.37704 - 6.81636I$ |
| $u = 0.863068 - 0.906873I$ $a = 1.00000$ $b = -1.23002 + 1.06519I$ | $1.01240 - 7.85357I$ | $1.37704 + 6.81636I$ |
| $u = -0.606706 + 1.104340I$ $a = 1.00000$ $b = -0.474186 + 0.465380I$ | $2.86726 - 1.52978I$ | $-3.12219 + 1.19653I$ |
| $u = -0.606706 - 1.104340I$ $a = 1.00000$ $b = -0.474186 - 0.465380I$ | $2.86726 + 1.52978I$ | $-3.12219 - 1.19653I$ |
| $u = 0.376941 + 0.517480I$ $a = 1.00000$ $b = -0.75145 + 1.71976I$ | $6.55927 + 6.69837I$ | $-2.55381 - 9.47495I$ |
| $u = 0.376941 - 0.517480I$ $a = 1.00000$ $b = -0.75145 - 1.71976I$ | $6.55927 - 6.69837I$ | $-2.55381 + 9.47495I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.387427 + 0.358801I$ $a = 1.00000$ $b = -0.081855 - 1.118280I$ | $-1.68063 + 1.15707I$ | $-4.41586 - 6.34189I$ |
| $u = 0.387427 - 0.358801I$ $a = 1.00000$ $b = -0.081855 + 1.118280I$ | $-1.68063 - 1.15707I$ | $-4.41586 + 6.34189I$ |
| $u = -1.09163 + 1.20653I$ $a = 1.00000$ $b = -1.25608 + 0.97829I$ | $8.3986 - 15.3972I$ | $1.29891 + 7.67212I$ |
| $u = -1.09163 - 1.20653I$ $a = 1.00000$ $b = -1.25608 - 0.97829I$ | $8.3986 + 15.3972I$ | $1.29891 - 7.67212I$ |

II.

$$I_2^u = \langle 2u^7 - 14u^6 + \dots + 9b - 14, a + 1, 2u^8 + 2u^6 - 5u^5 + 4u^4 - 6u^3 + 5u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -1 \\ -\frac{2}{9}u^7 + \frac{14}{9}u^6 + \dots - \frac{10}{3}u + \frac{14}{9} \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{2}{9}u^7 + \frac{14}{9}u^6 + \dots - \frac{10}{3}u + \frac{5}{9} \\ -\frac{2}{9}u^7 + \frac{14}{9}u^6 + \dots - \frac{10}{3}u + \frac{14}{9} \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ -\frac{14}{9}u^7 - \frac{10}{9}u^6 + \dots - \frac{1}{3}u - \frac{1}{9} \end{pmatrix} \\ a_3 &= \begin{pmatrix} \frac{10}{9}u^7 + \frac{2}{9}u^6 + \dots + \frac{5}{3}u + \frac{2}{9} \\ \frac{2}{3}u^7 + 2u^5 + \dots + \frac{5}{3}u - \frac{4}{3} \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{20}{9}u^7 + \frac{10}{9}u^6 + \dots + 3u - \frac{11}{9} \\ -\frac{4}{9}u^7 - \frac{8}{9}u^6 + \dots + \frac{4}{3}u - \frac{8}{9} \end{pmatrix} \\ a_6 &= \begin{pmatrix} \frac{2}{3}u^6 + \frac{2}{3}u^5 + \dots - \frac{4}{3}u + \frac{1}{3} \\ \frac{2}{3}u^6 + \frac{2}{3}u^5 + \dots - \frac{4}{3}u + \frac{1}{3} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -\frac{8}{3}u^7 - \frac{2}{3}u^6 + \dots - \frac{10}{3}u + 1 \\ -\frac{10}{9}u^7 + \frac{4}{9}u^6 + \dots - 2u + \frac{10}{9} \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{10}{9}u^7 - \frac{2}{9}u^6 + \dots - \frac{5}{3}u - \frac{2}{9} \\ \frac{4}{3}u^7 + \frac{8}{3}u^6 + \dots - 2u + \frac{2}{3} \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{10}{9}u^7 - \frac{2}{9}u^6 + \dots - \frac{5}{3}u - \frac{2}{9} \\ \frac{4}{3}u^7 + \frac{8}{3}u^6 + \dots - 2u + \frac{2}{3} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$(iii) \text{ Cusp Shapes} = -\frac{166}{9}u^7 - \frac{92}{9}u^6 - \frac{194}{9}u^5 + \frac{103}{3}u^4 - \frac{128}{9}u^3 + \frac{344}{9}u^2 - 18u - \frac{59}{9}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $4(4u^8 - 8u^7 + 17u^5 - 13u^4 - 2u^3 + 13u^2 - 3u + 1)$ |
| c_2, c_5 | $2(2u^8 - 2u^7 + 4u^6 + u^5 - 11u^4 + 5u^3 + 6u^2 - 5u + 1)$ |
| c_3, c_{10} | $u^8 + 2u^7 + 3u^6 + 2u^5 + 2u^4 + 3u^3 + 6u^2 + 6u + 2$ |
| c_4, c_{11} | $2(2u^8 + 2u^6 - 5u^5 + 4u^4 - 6u^3 + 5u^2 - 2u + 1)$ |
| c_6, c_8 | $u^8 + u^7 + u^6 + 4u^5 + 7u^4 - u^3 - 2u^2 + 8u + 6$ |
| c_7 | $u^8 + 4u^7 + 9u^6 + 11u^5 + 9u^4 + 3u^3 - 2u + 1$ |
| c_9 | $u^8 - u^7 - 3u^6 - 2u^5 + 5u^4 + 6u^3 + 4u^2 + u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|--|
| c_1 | 16 $\cdot (16y^8 - 64y^7 + 168y^6 - 217y^5 + 197y^4 - 240y^3 + 131y^2 + 17y + 1)$ |
| c_2, c_5 | $4(4y^8 + 12y^7 - 24y^6 - 45y^5 + 143y^4 - 139y^3 + 64y^2 - 13y + 1)$ |
| c_3, c_{10} | $y^8 + 2y^7 + 5y^6 + 8y^5 + 8y^4 + 3y^3 + 8y^2 - 12y + 4$ |
| c_4, c_{11} | $4(4y^8 + 8y^7 + 20y^6 + 11y^5 - 20y^4 - 12y^3 + 9y^2 + 6y + 1)$ |
| c_6, c_8 | $y^8 + y^7 + 7y^6 - 4y^5 + 49y^4 - 81y^3 + 104y^2 - 88y + 36$ |
| c_7 | $y^8 + 2y^7 + 11y^6 + 17y^5 + 33y^4 + 53y^3 + 30y^2 - 4y + 1$ |
| c_9 | $y^8 - 7y^7 + 15y^6 - 14y^5 + 29y^4 + 2y^3 + 14y^2 + 7y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.081144 + 0.964537I$ $a = -1.00000$ $b = -0.344131 - 0.211497I$ | $-0.11790 + 2.52032I$ | $-8.47313 - 1.37245I$ |
| $u = -0.081144 - 0.964537I$ $a = -1.00000$ $b = -0.344131 + 0.211497I$ | $-0.11790 - 2.52032I$ | $-8.47313 + 1.37245I$ |
| $u = 0.876567 + 0.170950I$ $a = -1.00000$ $b = 0.186359 + 1.054490I$ | $7.53561 + 5.92481I$ | $2.17560 - 4.89559I$ |
| $u = 0.876567 - 0.170950I$ $a = -1.00000$ $b = 0.186359 - 1.054490I$ | $7.53561 - 5.92481I$ | $2.17560 + 4.89559I$ |
| $u = 0.120498 + 0.535479I$ $a = -1.00000$ $b = 1.02903 - 1.25354I$ | $-2.49208 + 1.02158I$ | $-16.3238 - 6.0123I$ |
| $u = 0.120498 - 0.535479I$ $a = -1.00000$ $b = 1.02903 + 1.25354I$ | $-2.49208 - 1.02158I$ | $-16.3238 + 6.0123I$ |
| $u = -0.91592 + 1.17562I$ $a = -1.00000$ $b = 1.12874 - 0.87067I$ | $-1.63576 - 8.28057I$ | $-4.87863 + 7.63527I$ |
| $u = -0.91592 - 1.17562I$ $a = -1.00000$ $b = 1.12874 + 0.87067I$ | $-1.63576 + 8.28057I$ | $-4.87863 - 7.63527I$ |

$$\text{III. } I_3^u = \langle -1.76 \times 10^{54}u^{35} - 3.41 \times 10^{54}u^{34} + \dots + 1.62 \times 10^{53}b + 2.48 \times 10^{53}, 3.12 \times 10^{54}u^{35} + 4.43 \times 10^{54}u^{34} + \dots + 2.31 \times 10^{52}a - 3.75 \times 10^{54}, 2u^{36} + 2u^{35} + \dots - 14u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -135.297u^{35} - 192.047u^{34} + \dots - 1894.64u + 162.375 \\ 10.9190u^{35} + 21.1108u^{34} + \dots + 23.6339u - 1.53438 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -124.378u^{35} - 170.936u^{34} + \dots - 1871.00u + 160.840 \\ 10.9190u^{35} + 21.1108u^{34} + \dots + 23.6339u - 1.53438 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 140.578u^{35} + 183.175u^{34} + \dots + 2437.80u - 225.735 \\ -22.7951u^{35} - 26.5223u^{34} + \dots - 458.196u + 42.0517 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -203.081u^{35} - 272.115u^{34} + \dots - 3148.94u + 274.459 \\ 46.8092u^{35} + 61.5248u^{34} + \dots + 699.352u - 58.6705 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -177.136u^{35} - 236.734u^{34} + \dots - 2831.29u + 250.306 \\ 44.3327u^{35} + 58.6254u^{34} + \dots + 646.276u - 53.9528 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 28.2278u^{35} + 40.0599u^{34} + \dots + 373.025u - 32.8519 \\ -6.91942u^{35} - 4.84581u^{34} + \dots - 223.697u + 19.9655 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 104.432u^{35} + 141.715u^{34} + \dots + 1653.06u - 152.962 \\ -13.3506u^{35} - 14.9377u^{34} + \dots - 324.539u + 30.7209 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -117.271u^{35} - 167.192u^{34} + \dots - 1630.91u + 139.095 \\ 14.3939u^{35} + 26.3816u^{34} + \dots + 50.7212u - 3.21539 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -117.271u^{35} - 167.192u^{34} + \dots - 1630.91u + 139.095 \\ 14.3939u^{35} + 26.3816u^{34} + \dots + 50.7212u - 3.21539 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-284.262u^{35} - 374.406u^{34} + \dots - 4742.13u + 418.350$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $4(2u^{18} - 16u^{17} + \dots - 7u + 7)^2$ |
| c_2, c_5 | $2(2u^{36} + 2u^{35} + \dots + 1164u + 139)$ |
| c_3, c_{10} | $u^{36} - 5u^{35} + \dots - 20u + 2$ |
| c_4, c_{11} | $2(2u^{36} - 2u^{35} + \dots + 14u + 1)$ |
| c_6, c_8 | $u^{36} + u^{35} + \dots + 804u + 346$ |
| c_7 | $(u^{18} + 4u^{17} + \dots + 2u + 1)^2$ |
| c_9 | $(u^{18} + 6u^{17} + \dots - 17u - 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1 | $16(4y^{18} - 72y^{17} + \dots - 553y + 49)^2$ |
| c_2, c_5 | $4(4y^{36} + 156y^{35} + \dots - 52188y + 19321)$ |
| c_3, c_{10} | $y^{36} + 7y^{35} + \dots + 344y + 4$ |
| c_4, c_{11} | $4(4y^{36} - 20y^{35} + \dots - 8y + 1)$ |
| c_6, c_8 | $y^{36} + 15y^{35} + \dots - 174472y + 119716$ |
| c_7 | $(y^{18} - 2y^{17} + \dots - 12y + 1)^2$ |
| c_9 | $(y^{18} - 24y^{17} + \dots - 197y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.961570 + 0.451207I$ $a = -0.99137 + 1.45940I$ $b = 0.705308 + 0.173824I$ | $9.41487 + 6.35338I$ | $6.10831 - 5.82519I$ |
| $u = 0.961570 - 0.451207I$ $a = -0.99137 - 1.45940I$ $b = 0.705308 - 0.173824I$ | $9.41487 - 6.35338I$ | $6.10831 + 5.82519I$ |
| $u = 0.802634 + 0.723579I$ $a = -0.970908 + 0.553934I$ $b = 1.09375 + 1.07152I$ | $9.34056 + 3.99785I$ | $4.89270 - 3.37103I$ |
| $u = 0.802634 - 0.723579I$ $a = -0.970908 - 0.553934I$ $b = 1.09375 - 1.07152I$ | $9.34056 - 3.99785I$ | $4.89270 + 3.37103I$ |
| $u = 1.045790 + 0.309537I$ $a = 0.012525 - 0.502541I$ $b = 0.201172 + 0.954404I$ | $-1.66631 - 0.81812I$ | $-4.46509 + 7.48163I$ |
| $u = 1.045790 - 0.309537I$ $a = 0.012525 + 0.502541I$ $b = 0.201172 - 0.954404I$ | $-1.66631 + 0.81812I$ | $-4.46509 - 7.48163I$ |
| $u = -0.313395 + 0.785869I$ $a = 1.82670 + 0.98006I$ $b = -0.590040 + 0.925318I$ | $5.29155 - 6.58230I$ | $-1.74185 + 7.38738I$ |
| $u = -0.313395 - 0.785869I$ $a = 1.82670 - 0.98006I$ $b = -0.590040 - 0.925318I$ | $5.29155 + 6.58230I$ | $-1.74185 - 7.38738I$ |
| $u = -1.146610 + 0.289938I$ $a = 0.879803 + 0.475338I$ $b = -0.771930$ | 2.09741 | $6.92265 + 0.I$ |
| $u = -1.146610 - 0.289938I$ $a = 0.879803 - 0.475338I$ $b = -0.771930$ | 2.09741 | $6.92265 + 0.I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.925613 + 0.773706I$ $a = 0.177368 - 0.984145I$ $b = -0.377469$ | 0.191595 | 0 |
| $u = 0.925613 - 0.773706I$ $a = 0.177368 + 0.984145I$ $b = -0.377469$ | 0.191595 | 0 |
| $u = -1.180100 + 0.257922I$ $a = -0.777034 + 0.443323I$ $b = 1.09375 - 1.07152I$ | $9.34056 - 3.99785I$ | $4.89270 + 3.37103I$ |
| $u = -1.180100 - 0.257922I$ $a = -0.777034 - 0.443323I$ $b = 1.09375 + 1.07152I$ | $9.34056 + 3.99785I$ | $4.89270 - 3.37103I$ |
| $u = 0.445688 + 1.214900I$ $a = 0.262519 - 0.268046I$ $b = -1.212220 + 0.386817I$ | $7.83132 + 1.16760I$ | $4.47566 + 0.I$ |
| $u = 0.445688 - 1.214900I$ $a = 0.262519 + 0.268046I$ $b = -1.212220 - 0.386817I$ | $7.83132 - 1.16760I$ | $4.47566 + 0.I$ |
| $u = 0.242297 + 0.574880I$ $a = -0.483632 - 0.551179I$ $b = 0.620071 - 1.035940I$ | $-1.91252 + 0.92110I$ | $0.62272 - 2.27597I$ |
| $u = 0.242297 - 0.574880I$ $a = -0.483632 + 0.551179I$ $b = 0.620071 + 1.035940I$ | $-1.91252 - 0.92110I$ | $0.62272 + 2.27597I$ |
| $u = 0.168654 + 0.521676I$ $a = 0.04956 - 1.98865I$ $b = 0.201172 - 0.954404I$ | $-1.66631 + 0.81812I$ | $-4.46509 - 7.48163I$ |
| $u = 0.168654 - 0.521676I$ $a = 0.04956 + 1.98865I$ $b = 0.201172 + 0.954404I$ | $-1.66631 - 0.81812I$ | $-4.46509 + 7.48163I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = 1.04555 + 1.04502I$ $a = -1.025980 - 0.149246I$ $b = 1.129710 + 0.820643I$ | $-0.40495 + 7.64175I$ | 0 |
| $u = 1.04555 - 1.04502I$ $a = -1.025980 + 0.149246I$ $b = 1.129710 - 0.820643I$ | $-0.40495 - 7.64175I$ | 0 |
| $u = -0.61317 + 1.38045I$ $a = -0.131546 - 0.191009I$ $b = 0.626954 - 0.364844I$ | $0.56981 - 3.14278I$ | 0 |
| $u = -0.61317 - 1.38045I$ $a = -0.131546 + 0.191009I$ $b = 0.626954 + 0.364844I$ | $0.56981 + 3.14278I$ | 0 |
| $u = 0.442651 + 0.199469I$ $a = 1.86494 + 1.90421I$ $b = -1.212220 + 0.386817I$ | $7.83132 + 1.16760I$ | $4.47566 - 0.91080I$ |
| $u = 0.442651 - 0.199469I$ $a = 1.86494 - 1.90421I$ $b = -1.212220 - 0.386817I$ | $7.83132 - 1.16760I$ | $4.47566 + 0.91080I$ |
| $u = -0.91675 + 1.22821I$ $a = -0.954477 - 0.138844I$ $b = 1.129710 - 0.820643I$ | $-0.40495 - 7.64175I$ | 0 |
| $u = -0.91675 - 1.22821I$ $a = -0.954477 + 0.138844I$ $b = 1.129710 + 0.820643I$ | $-0.40495 + 7.64175I$ | 0 |
| $u = 0.199679 + 0.411580I$ $a = -0.899448 - 1.025070I$ $b = 0.620071 + 1.035940I$ | $-1.91252 - 0.92110I$ | $0.62272 + 2.27597I$ |
| $u = 0.199679 - 0.411580I$ $a = -0.899448 + 1.025070I$ $b = 0.620071 - 1.035940I$ | $-1.91252 + 0.92110I$ | $0.62272 - 2.27597I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|----------------------|
| $u = 0.344338 + 0.064471I$ | | |
| $a = -2.44560 - 3.55110I$ | $0.56981 + 3.14278I$ | $0.19751 - 9.10915I$ |
| $b = 0.626954 + 0.364844I$ | | |
| $u = 0.344338 - 0.064471I$ | | |
| $a = -2.44560 + 3.55110I$ | $0.56981 - 3.14278I$ | $0.19751 + 9.10915I$ |
| $b = 0.626954 - 0.364844I$ | | |
| $u = -1.34267 + 1.12840I$ | | |
| $a = 0.425077 - 0.228061I$ | $5.29155 - 6.58230I$ | 0 |
| $b = -0.590040 + 0.925318I$ | | |
| $u = -1.34267 - 1.12840I$ | | |
| $a = 0.425077 + 0.228061I$ | $5.29155 + 6.58230I$ | 0 |
| $b = -0.590040 - 0.925318I$ | | |
| $u = -1.61177 + 0.95600I$ | | |
| $a = -0.318496 - 0.468858I$ | $9.41487 + 6.35338I$ | 0 |
| $b = 0.705308 + 0.173824I$ | | |
| $u = -1.61177 - 0.95600I$ | | |
| $a = -0.318496 + 0.468858I$ | $9.41487 - 6.35338I$ | 0 |
| $b = 0.705308 - 0.173824I$ | | |

IV.

$$I_4^u = \langle 4u^3 + 6u^2 + 3b + 4u + 1, 4u^3 + 12u^2 + 3a + 10u + 1, 2u^4 + 4u^3 + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{4}{3}u^3 - 4u^2 - \frac{10}{3}u - \frac{1}{3} \\ -\frac{4}{3}u^3 - 2u^2 - \frac{4}{3}u - \frac{1}{3} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{8}{3}u^3 - 6u^2 - \frac{14}{3}u - \frac{2}{3} \\ -\frac{4}{3}u^3 - 2u^2 - \frac{4}{3}u - \frac{1}{3} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{4}{3}u^3 - 4u^2 - \frac{13}{3}u - \frac{4}{3} \\ -\frac{2}{3}u^3 - 2u^2 - \frac{2}{3}u - \frac{2}{3} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2u^3 - 4u^2 - 2u + 2 \\ -2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^3 - 4u^2 - u + 2 \\ -u^3 - 2u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{4}{3}u^3 - 6u^2 - \frac{28}{3}u - \frac{13}{3} \\ -2u^2 - 2u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{8}{3}u^3 - 8u^2 - \frac{26}{3}u - \frac{8}{3} \\ -\frac{2}{3}u^3 - 2u^2 - \frac{2}{3}u - \frac{2}{3} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{2}{3}u^3 - 4u^2 - \frac{14}{3}u - \frac{2}{3} \\ -\frac{10}{3}u^3 - 4u^2 - \frac{1}{3}u - \frac{4}{3} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{2}{3}u^3 - 4u^2 - \frac{14}{3}u - \frac{2}{3} \\ -\frac{10}{3}u^3 - 4u^2 - \frac{1}{3}u - \frac{4}{3} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -4

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--------------------------------|
| c_1 | $4(2u^2 - 2u + 1)^2$ |
| c_2, c_5 | $2(2u^4 - 4u^3 + 2u^2 + 1)$ |
| c_3, c_{10} | $u^4 + 4u^3 + 6u^2 + 4u + 2$ |
| c_4, c_{11} | $2(2u^4 + 4u^3 + 2u^2 + 1)$ |
| c_6, c_8 | $u^4 + 2u^2 + 4u + 2$ |
| c_7, c_9 | $(u^2 + 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|------------------------------------|
| c_1 | $16(4y^2 + 1)^2$ |
| c_2, c_4, c_5 c_{11} | $4(4y^4 - 8y^3 + 8y^2 + 4y + 1)$ |
| c_3, c_{10} | $y^4 - 4y^3 + 8y^2 + 8y + 4$ |
| c_6, c_8 | $y^4 + 4y^3 + 8y^2 - 8y + 4$ |
| c_7, c_9 | $(y + 1)^4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.207110 + 0.500000I$ | | |
| $a = 0.414214I$ | -1.64493 | -4.00000 |
| $b = -1.000000I$ | | |
| $u = -1.207110 - 0.500000I$ | | |
| $a = -0.414214I$ | -1.64493 | -4.00000 |
| $b = 1.000000I$ | | |
| $u = 0.207107 + 0.500000I$ | | |
| $a = -2.41421I$ | -1.64493 | -4.00000 |
| $b = -1.000000I$ | | |
| $u = 0.207107 - 0.500000I$ | | |
| $a = 2.41421I$ | -1.64493 | -4.00000 |
| $b = 1.000000I$ | | |

V. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1 | $256(2u^2 - 2u + 1)^2(4u^8 - 8u^7 + \dots - 3u + 1)$ $\cdot (4u^{14} + 43u^{13} + \dots + 336u + 64)(2u^{18} - 16u^{17} + \dots - 7u + 7)^2$ |
| c_2, c_5 | $16(2u^4 - 4u^3 + 2u^2 + 1)$ $\cdot (2u^8 - 2u^7 + 4u^6 + u^5 - 11u^4 + 5u^3 + 6u^2 - 5u + 1)$ $\cdot (2u^{14} - u^{13} + \dots + 9u^2 + 1)(2u^{36} + 2u^{35} + \dots + 1164u + 139)$ |
| c_3, c_{10} | $(u^4 + 4u^3 + 6u^2 + 4u + 2)$ $\cdot (u^8 + 2u^7 + 3u^6 + 2u^5 + 2u^4 + 3u^3 + 6u^2 + 6u + 2)$ $\cdot (u^{14} - 2u^{13} + \dots - 3u + 2)(u^{36} - 5u^{35} + \dots - 20u + 2)$ |
| c_4, c_{11} | $16(2u^4 + 4u^3 + 2u^2 + 1)(2u^8 + 2u^6 + \dots - 2u + 1)$ $\cdot (2u^{14} - 3u^{13} + \dots + 3u + 1)(2u^{36} - 2u^{35} + \dots + 14u + 1)$ |
| c_6, c_8 | $(u^4 + 2u^2 + 4u + 2)(u^8 + u^7 + u^6 + 4u^5 + 7u^4 - u^3 - 2u^2 + 8u + 6)$ $\cdot (u^{14} - u^{13} + \dots - 13u + 2)(u^{36} + u^{35} + \dots + 804u + 346)$ |
| c_7 | $(u^2 + 1)^2(u^8 + 4u^7 + 9u^6 + 11u^5 + 9u^4 + 3u^3 - 2u + 1)$ $\cdot (u^{14} - 9u^{13} + \dots - 24u + 8)(u^{18} + 4u^{17} + \dots + 2u + 1)^2$ |
| c_9 | $(u^2 + 1)^2(u^8 - u^7 - 3u^6 - 2u^5 + 5u^4 + 6u^3 + 4u^2 + u + 1)$ $\cdot (u^{14} - 10u^{13} + \dots - 80u + 32)(u^{18} + 6u^{17} + \dots - 17u - 1)^2$ |

VI. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1 | $65536(4y^2 + 1)^2$ $\cdot (16y^8 - 64y^7 + 168y^6 - 217y^5 + 197y^4 - 240y^3 + 131y^2 + 17y + 1)$ $\cdot (16y^{14} - 105y^{13} + \dots + 16128y + 4096)$ $\cdot (4y^{18} - 72y^{17} + \dots - 553y + 49)^2$ |
| c_2, c_5 | $256(4y^4 - 8y^3 + 8y^2 + 4y + 1)$ $\cdot (4y^8 + 12y^7 - 24y^6 - 45y^5 + 143y^4 - 139y^3 + 64y^2 - 13y + 1)$ $\cdot (4y^{14} + 83y^{13} + \dots + 18y + 1)$ $\cdot (4y^{36} + 156y^{35} + \dots - 52188y + 19321)$ |
| c_3, c_{10} | $(y^4 - 4y^3 + 8y^2 + 8y + 4)$ $\cdot (y^8 + 2y^7 + 5y^6 + 8y^5 + 8y^4 + 3y^3 + 8y^2 - 12y + 4)$ $\cdot (y^{14} + 4y^{13} + \dots - 5y + 4)(y^{36} + 7y^{35} + \dots + 344y + 4)$ |
| c_4, c_{11} | $256(4y^4 - 8y^3 + 8y^2 + 4y + 1)$ $\cdot (4y^8 + 8y^7 + 20y^6 + 11y^5 - 20y^4 - 12y^3 + 9y^2 + 6y + 1)$ $\cdot (4y^{14} + 15y^{13} + \dots + 5y + 1)(4y^{36} - 20y^{35} + \dots - 8y + 1)$ |
| c_6, c_8 | $(y^4 + 4y^3 + 8y^2 - 8y + 4)$ $\cdot (y^8 + y^7 + 7y^6 - 4y^5 + 49y^4 - 81y^3 + 104y^2 - 88y + 36)$ $\cdot (y^{14} + 7y^{13} + \dots - 33y + 4)(y^{36} + 15y^{35} + \dots - 174472y + 119716)$ |
| c_7 | $(y + 1)^4(y^8 + 2y^7 + 11y^6 + 17y^5 + 33y^4 + 53y^3 + 30y^2 - 4y + 1)$ $\cdot (y^{14} + 3y^{13} + \dots - 96y + 64)(y^{18} - 2y^{17} + \dots - 12y + 1)^2$ |
| c_9 | $(y + 1)^4(y^8 - 7y^7 + 15y^6 - 14y^5 + 29y^4 + 2y^3 + 14y^2 + 7y + 1)$ $\cdot (y^{14} - 10y^{13} + \dots + 5376y + 1024)(y^{18} - 24y^{17} + \dots - 197y + 1)^2$ |