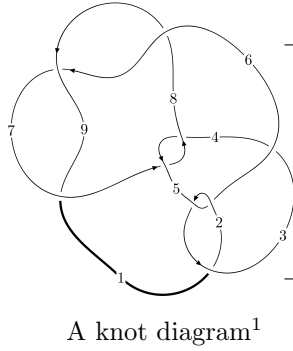
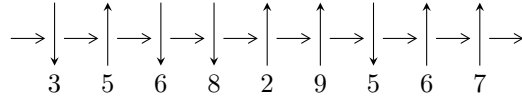


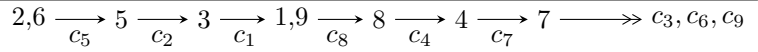
9<sub>42</sub> (K9n<sub>4</sub>)



**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^4 + u^3 + u^2 + b + 1, u^4 + u^3 + u^2 + a - u + 1, u^5 + 2u^4 + 2u^3 + u + 1 \rangle$$

$$I_2^u = \langle b + 1, a - u + 1, u^2 - u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 7 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle u^4 + u^3 + u^2 + b + 1, u^4 + u^3 + u^2 + a - u + 1, u^5 + 2u^4 + 2u^3 + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ -2u^4 - u^3 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^4 - u^3 - u^2 + u - 1 \\ -u^4 - u^3 - u^2 - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u^4 - u^3 - u^2 - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^4 - 2u^3 - u^2 + u - 1 \\ -u^3 - u^2 + u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^4 - 2u^3 - u^2 + u - 1 \\ -u^3 - u^2 + u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $u^4 + u^3 - 2u^2 - 5u + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^5 + 6u^3 + u - 1$
$c_2, c_5$	$u^5 + 2u^4 + 2u^3 + u + 1$
$c_3$	$u^5 - 2u^4 + 14u^3 + 16u^2 + 9u + 9$
$c_4, c_7$	$u^5 - u^4 + 8u^3 - u^2 - 4u - 4$
$c_6, c_8, c_9$	$u^5 + 3u^4 - u^3 - 6u^2 - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^5 + 12y^4 + 38y^3 + 12y^2 + y - 1$
$c_2, c_5$	$y^5 + 6y^3 + y - 1$
$c_3$	$y^5 + 24y^4 + 278y^3 + 32y^2 - 207y - 81$
$c_4, c_7$	$y^5 + 15y^4 + 54y^3 - 73y^2 + 8y - 16$
$c_6, c_8, c_9$	$y^5 - 11y^4 + 37y^3 - 30y^2 - 12y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.436447 + 0.655029I$		
$a = 0.423679 + 0.262806I$	$-0.057511 + 1.373620I$	$-0.45374 - 4.59823I$
$b = -0.012768 - 0.392223I$		
$u = 0.436447 - 0.655029I$		
$a = 0.423679 - 0.262806I$	$-0.057511 - 1.373620I$	$-0.45374 + 4.59823I$
$b = -0.012768 + 0.392223I$		
$u = -0.668466$		
$a = -2.01628$	$2.55277$	$4.34960$
$b = -1.34782$		
$u = -1.10221 + 1.09532I$		
$a = 1.084460 + 0.905094I$	$17.6979 - 4.0569I$	$4.27894 + 1.95729I$
$b = 2.18668 - 0.19022I$		
$u = -1.10221 - 1.09532I$		
$a = 1.084460 - 0.905094I$	$17.6979 + 4.0569I$	$4.27894 - 1.95729I$
$b = 2.18668 + 0.19022I$		

$$\text{II. } I_2^u = \langle b + 1, a - u + 1, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u - 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4u + 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$u^2 - u + 1$
$c_2$	$u^2 + u + 1$
$c_4, c_7$	$u^2$
$c_6$	$(u + 1)^2$
$c_8, c_9$	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$y^2 + y + 1$
$c_4, c_7$	$y^2$
$c_6, c_8, c_9$	$(y - 1)^2$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = -0.500000 + 0.866025I$ $b = -1.00000$	$1.64493 + 2.02988I$	$3.00000 - 3.46410I$
$u = 0.500000 - 0.866025I$ $a = -0.500000 - 0.866025I$ $b = -1.00000$	$1.64493 - 2.02988I$	$3.00000 + 3.46410I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)(u^5 + 6u^3 + u - 1)$
$c_2$	$(u^2 + u + 1)(u^5 + 2u^4 + 2u^3 + u + 1)$
$c_3$	$(u^2 - u + 1)(u^5 - 2u^4 + 14u^3 + 16u^2 + 9u + 9)$
$c_4, c_7$	$u^2(u^5 - u^4 + 8u^3 - u^2 - 4u - 4)$
$c_5$	$(u^2 - u + 1)(u^5 + 2u^4 + 2u^3 + u + 1)$
$c_6$	$(u + 1)^2(u^5 + 3u^4 - u^3 - 6u^2 - 1)$
$c_8, c_9$	$(u - 1)^2(u^5 + 3u^4 - u^3 - 6u^2 - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 + y + 1)(y^5 + 12y^4 + 38y^3 + 12y^2 + y - 1)$
$c_2, c_5$	$(y^2 + y + 1)(y^5 + 6y^3 + y - 1)$
$c_3$	$(y^2 + y + 1)(y^5 + 24y^4 + 278y^3 + 32y^2 - 207y - 81)$
$c_4, c_7$	$y^2(y^5 + 15y^4 + 54y^3 - 73y^2 + 8y - 16)$
$c_6, c_8, c_9$	$(y - 1)^2(y^5 - 11y^4 + 37y^3 - 30y^2 - 12y - 1)$