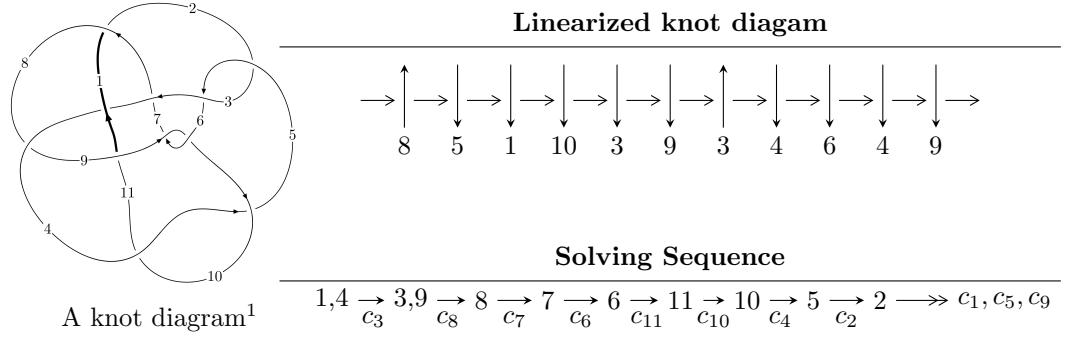


$11n_{164}$ ($K11n_{164}$)



Ideals for irreducible components² of X_{par}

$$\begin{aligned}
 I_1^u &= \langle -u^6 + u^5 - 2u^4 - 2u^2 + b - 2u - 1, -u^7 + 3u^6 - 3u^5 + 2u^4 + 2u^3 - u^2 + 3a + 6u + 3, \\
 &\quad u^8 - 3u^7 + 6u^6 - 5u^5 + 4u^4 + u^3 + 3u + 3 \rangle \\
 I_2^u &= \langle -2u^9 + 10u^8 - 24u^7 + 38u^6 - 49u^5 + 52u^4 - 32u^3 - u^2 + b + 14u - 5, \\
 &\quad 5u^9 - 23u^8 + 55u^7 - 86u^6 + 112u^5 - 116u^4 + 73u^3 + 2u^2 + a - 29u + 11, \\
 &\quad u^{10} - 5u^9 + 13u^8 - 22u^7 + 30u^6 - 33u^5 + 25u^4 - 6u^3 - 6u^2 + 5u - 1 \rangle \\
 I_3^u &= \langle -u^5 - 2u^4 - 4u^3 - 3u^2 + b - 2u + 1, -u^9 - 4u^8 - 11u^7 - 19u^6 - 25u^5 - 22u^4 - 14u^3 - 5u^2 + a - u - 1, \\
 &\quad u^{10} + 4u^9 + 11u^8 + 19u^7 + 25u^6 + 21u^5 + 12u^4 + u^3 - 2u^2 - u + 1 \rangle \\
 I_4^u &= \langle -3u^3 - au - 5u^2 + b - 3u + 4, 4u^3a + 7u^2a + u^3 + a^2 + 5au + 2u^2 - 5a + u - 2, u^4 + u^3 - 2u + 1 \rangle \\
 I_5^u &= \langle -au + b + u + 1, a^2 + au - 2u - 1, u^2 + u + 1 \rangle \\
 I_6^u &= \langle b - 2, a + 1, u + 1 \rangle \\
 I_7^u &= \langle b + 1, a - 2, u + 1 \rangle \\
 I_8^u &= \langle b - 1, a + 1, u + 1 \rangle \\
 \\
 I_1^v &= \langle a, b - 1, v - 1 \rangle
 \end{aligned}$$

* 9 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 44 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^6 + u^5 - 2u^4 - 2u^2 + b - 2u - 1, -u^7 + 3u^6 + \dots + 3a + 3, u^8 - 3u^7 + 6u^6 - 5u^5 + 4u^4 + u^3 + 3u + 3 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} \frac{1}{3}u^7 - u^6 + \dots - 2u - 1 \\ u^6 - u^5 + 2u^4 + 2u^2 + 2u + 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} \frac{1}{3}u^7 + \frac{4}{3}u^4 - \frac{2}{3}u^3 + \frac{7}{3}u^2 \\ u^6 - u^5 + 2u^4 + 2u^2 + 2u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -\frac{2}{3}u^7 + 2u^6 + \dots + 2u + 2 \\ -u^7 - u^5 - 2u^4 - 3u^3 - 3u^2 - 4u - 2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{2}{3}u^7 + u^6 + \dots - \frac{2}{3}u^2 + 1 \\ -u^6 + u^5 - 2u^4 - u^3 - u^2 - 3u - 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -\frac{1}{3}u^7 - \frac{4}{3}u^4 + \dots - \frac{4}{3}u^2 - u \\ u^7 - 2u^6 + 3u^5 - u^4 + u^3 + u^2 - 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{2}{3}u^7 - 2u^6 + \dots - u - 1 \\ u^7 - 2u^6 + 3u^5 - u^4 + u^3 + u^2 - 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -\frac{2}{3}u^7 + 2u^6 + \dots + 2u + 2 \\ -2u^7 + 3u^6 - 4u^5 - 2u^3 - 2u^2 + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{2}{3}u^7 - u^6 + \dots + u + 1 \\ u^6 - u^5 + 2u^4 + u^3 + 2u^2 + 4u + 2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{2}{3}u^7 - u^6 + \dots + u + 1 \\ u^6 - u^5 + 2u^4 + u^3 + 2u^2 + 4u + 2 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = $-2u^7 + 6u^6 - 12u^5 + 12u^4 - 8u^3 + 2u^2 - 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^8 - u^7 + 9u^6 - 4u^5 + 26u^4 - 2u^3 + 28u^2 + 10$
c_2, c_5, c_8 c_{11}	$u^8 - u^7 - 4u^6 + 5u^5 + 4u^4 - 3u^3 + 4u^2 - u + 1$
c_3, c_6, c_9	$u^8 - 3u^7 + 6u^6 - 5u^5 + 4u^4 + u^3 + 3u + 3$
c_4, c_{10}	$u^8 + 6u^7 + 20u^6 + 42u^5 + 68u^4 + 82u^3 + 74u^2 + 32u + 8$
c_7	$u^8 + 2u^7 + 9u^6 + 10u^5 + 31u^4 + 30u^3 + 27u^2 + 26u + 12$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^8 + 17y^7 + \dots + 560y + 100$
c_2, c_5, c_8 c_{11}	$y^8 - 9y^7 + 34y^6 - 55y^5 + 14y^4 + 25y^3 + 18y^2 + 7y + 1$
c_3, c_6, c_9	$y^8 + 3y^7 + 14y^6 + 29y^5 + 50y^4 + 65y^3 + 18y^2 - 9y + 9$
c_4, c_{10}	$y^8 + 4y^7 + 32y^6 + 120y^5 + 328y^4 + 972y^3 + 1316y^2 + 160y + 64$
c_7	$y^8 + 14y^7 + 103y^6 + 392y^5 + 767y^4 + 470y^3 - 87y^2 - 28y + 144$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.010055 + 1.117600I$		
$a = -0.471916 - 0.347611I$	$5.09476 + 1.30932I$	$-1.82878 - 5.39060I$
$b = -0.383744 + 0.530909I$		
$u = 0.010055 - 1.117600I$		
$a = -0.471916 + 0.347611I$	$5.09476 - 1.30932I$	$-1.82878 + 5.39060I$
$b = -0.383744 - 0.530909I$		
$u = -0.576935 + 0.295827I$		
$a = 0.469090 - 0.674407I$	$-0.769995 + 1.158600I$	$-7.36601 - 5.92276I$
$b = 0.071127 - 0.527859I$		
$u = -0.576935 - 0.295827I$		
$a = 0.469090 + 0.674407I$	$-0.769995 - 1.158600I$	$-7.36601 + 5.92276I$
$b = 0.071127 + 0.527859I$		
$u = 0.97820 + 1.19005I$		
$a = -0.587535 + 0.812766I$	$-10.45920 - 2.83405I$	$-9.78328 + 2.02620I$
$b = 1.54196 - 0.09585I$		
$u = 0.97820 - 1.19005I$		
$a = -0.587535 - 0.812766I$	$-10.45920 + 2.83405I$	$-9.78328 - 2.02620I$
$b = 1.54196 + 0.09585I$		
$u = 1.08868 + 1.10558I$		
$a = 1.090360 - 0.490500I$	$-11.1373 - 13.1502I$	$-9.02192 + 6.51668I$
$b = -1.72934 - 0.67148I$		
$u = 1.08868 - 1.10558I$		
$a = 1.090360 + 0.490500I$	$-11.1373 + 13.1502I$	$-9.02192 - 6.51668I$
$b = -1.72934 + 0.67148I$		

II.

$$I_2^u = \langle -2u^9 + 10u^8 + \dots + b - 5, 5u^9 - 23u^8 + \dots + a + 11, u^{10} - 5u^9 + \dots + 5u - 1 \rangle$$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -5u^9 + 23u^8 + \dots + 29u - 11 \\ 2u^9 - 10u^8 + 24u^7 - 38u^6 + 49u^5 - 52u^4 + 32u^3 + u^2 - 14u + 5 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -3u^9 + 13u^8 - 31u^7 + 48u^6 - 63u^5 + 64u^4 - 41u^3 - u^2 + 15u - 6 \\ 2u^9 - 10u^8 + 24u^7 - 38u^6 + 49u^5 - 52u^4 + 32u^3 + u^2 - 14u + 5 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -3u^9 + 15u^8 - 38u^7 + 61u^6 - 80u^5 + 85u^4 - 58u^3 + u^2 + 22u - 9 \\ -u^9 + 3u^8 - 3u^7 + u^6 - 4u^4 + 13u^3 - 8u^2 - 4u + 3 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -4u^9 + 17u^8 - 39u^7 + 58u^6 - 75u^5 + 74u^4 - 42u^3 - 9u^2 + 17u - 5 \\ 2u^9 - 9u^8 + 22u^7 - 34u^6 + 44u^5 - 45u^4 + 29u^3 + 3u^2 - 13u + 4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2u^9 - 9u^8 + 21u^7 - 32u^6 + 42u^5 - 43u^4 + 26u^3 + 2u^2 - 8u + 5 \\ -u^9 + 5u^8 - 12u^7 + 18u^6 - 23u^5 + 24u^4 - 14u^3 - 4u^2 + 6u - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^9 - 4u^8 + 9u^7 - 14u^6 + 19u^5 - 19u^4 + 12u^3 - 2u^2 - 2u + 3 \\ -u^9 + 5u^8 - 12u^7 + 18u^6 - 23u^5 + 24u^4 - 14u^3 - 4u^2 + 6u - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -4u^9 + 17u^8 - 38u^7 + 56u^6 - 72u^5 + 71u^4 - 38u^3 - 9u^2 + 15u - 4 \\ u^9 - 7u^8 + 19u^7 - 31u^6 + 40u^5 - 45u^4 + 31u^3 + 2u^2 - 13u + 4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^7 - 3u^6 + 5u^5 - 6u^4 + 8u^3 - 5u^2 - u + 2 \\ -u^9 + 4u^8 - 8u^7 + 11u^6 - 14u^5 + 13u^4 - 4u^3 - 3u^2 + 3u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^7 - 3u^6 + 5u^5 - 6u^4 + 8u^3 - 5u^2 - u + 2 \\ -u^9 + 4u^8 - 8u^7 + 11u^6 - 14u^5 + 13u^4 - 4u^3 - 3u^2 + 3u - 1 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes**

$$= -7u^9 + 30u^8 - 69u^7 + 104u^6 - 134u^5 + 134u^4 - 76u^3 - 14u^2 + 35u - 16$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$(u^5 + 2u^3 - 2u^2 - u + 1)^2$
c_2, c_5, c_8 c_{11}	$u^{10} - u^9 - 6u^8 + 6u^7 + 15u^6 - 19u^5 - 10u^4 + 17u^3 - u + 1$
c_3, c_6, c_9	$u^{10} - 5u^9 + 13u^8 - 22u^7 + 30u^6 - 33u^5 + 25u^4 - 6u^3 - 6u^2 + 5u - 1$
c_4, c_{10}	$(u^5 + 4u^4 + 9u^3 + 11u^2 + 10u + 4)^2$
c_7	$(u^5 - u^4 + 5u^3 - 2u^2 - 2u + 3)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$(y^5 + 4y^4 + 2y^3 - 8y^2 + 5y - 1)^2$
c_2, c_5, c_8 c_{11}	$y^{10} - 13y^9 + \dots - y + 1$
c_3, c_6, c_9	$y^{10} + y^9 + 9y^8 + 16y^7 + 26y^6 + 39y^5 + 63y^4 - 66y^3 + 46y^2 - 13y + 1$
c_4, c_{10}	$(y^5 + 2y^4 + 13y^3 + 27y^2 + 12y - 16)^2$
c_7	$(y^5 + 9y^4 + 17y^3 - 18y^2 + 16y - 9)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.625622 + 0.371117I$		
$a = 1.85638 - 0.01798I$	$2.23236 - 3.66584I$	$-2.77098 - 1.99903I$
$b = -1.168060 - 0.677685I$		
$u = 0.625622 - 0.371117I$		
$a = 1.85638 + 0.01798I$	$2.23236 + 3.66584I$	$-2.77098 + 1.99903I$
$b = -1.168060 + 0.677685I$		
$u = -0.347234 + 1.335500I$		
$a = 0.191634 - 0.192957I$	$2.23236 + 3.66584I$	$-2.77098 + 1.99903I$
$b = -0.191152 - 0.322929I$		
$u = -0.347234 - 1.335500I$		
$a = 0.191634 + 0.192957I$	$2.23236 - 3.66584I$	$-2.77098 - 1.99903I$
$b = -0.191152 + 0.322929I$		
$u = -0.531946$		
$a = 0.830218$	-1.48837	-7.29890
$b = 0.441631$		
$u = 1.14606 + 0.92119I$		
$a = -1.184760 + 0.383544I$	$-11.35780 - 4.96850I$	$-10.07956 + 2.53316I$
$b = 1.71113 + 0.65182I$		
$u = 1.14606 - 0.92119I$		
$a = -1.184760 - 0.383544I$	$-11.35780 + 4.96850I$	$-10.07956 - 2.53316I$
$b = 1.71113 - 0.65182I$		
$u = 1.16790 + 1.05893I$		
$a = 0.714063 - 0.714867I$	$-11.35780 + 4.96850I$	$-10.07956 - 2.53316I$
$b = -1.59095 + 0.07875I$		
$u = 1.16790 - 1.05893I$		
$a = 0.714063 + 0.714867I$	$-11.35780 - 4.96850I$	$-10.07956 + 2.53316I$
$b = -1.59095 - 0.07875I$		
$u = 0.347235$		
$a = -2.98485$	-1.48837	-7.29890
$b = 1.03645$		

$$\text{III. } I_3^u = \langle -u^5 - 2u^4 - 4u^3 - 3u^2 + b - 2u + 1, -u^9 - 4u^8 + \dots + a - 1, u^{10} + 4u^9 + \dots - u + 1 \rangle$$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^9 + 4u^8 + 11u^7 + 19u^6 + 25u^5 + 22u^4 + 14u^3 + 5u^2 + u + 1 \\ u^5 + 2u^4 + 4u^3 + 3u^2 + 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^9 + 4u^8 + 11u^7 + 19u^6 + 26u^5 + 24u^4 + 18u^3 + 8u^2 + 3u \\ u^5 + 2u^4 + 4u^3 + 3u^2 + 2u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^9 + 4u^8 + 10u^7 + 16u^6 + 19u^5 + 15u^4 + 9u^3 + 4u^2 + 2u + 1 \\ u^9 + 3u^8 + 7u^7 + 9u^6 + 10u^5 + 6u^4 + 5u^3 + 2u^2 + 2u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^8 - 4u^7 - 11u^6 - 18u^5 - 22u^4 - 15u^3 - 6u^2 + 3u + 2 \\ -u^7 - 3u^6 - 6u^5 - 6u^4 - 4u^3 + u^2 + 2u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^7 + 3u^6 + 7u^5 + 9u^4 + 9u^3 + 3u^2 - 3 \\ u^8 + 3u^7 + 7u^6 + 9u^5 + 9u^4 + 3u^3 - 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^8 + 4u^7 + 10u^6 + 16u^5 + 18u^4 + 12u^3 + 3u^2 - 2u - 3 \\ u^8 + 3u^7 + 7u^6 + 9u^5 + 9u^4 + 3u^3 - 2u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^8 - 4u^7 - 11u^6 - 18u^5 - 22u^4 - 15u^3 - 5u^2 + 4u + 3 \\ -u^7 - 3u^6 - 6u^5 - 7u^4 - 5u^3 + 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^9 + 5u^8 + 14u^7 + 26u^6 + 34u^5 + 30u^4 + 15u^3 - 6u - 3 \\ u^9 + 4u^8 + 10u^7 + 16u^6 + 18u^5 + 12u^4 + 3u^3 - 3u^2 - 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^9 + 5u^8 + 14u^7 + 26u^6 + 34u^5 + 30u^4 + 15u^3 - 6u - 3 \\ u^9 + 4u^8 + 10u^7 + 16u^6 + 18u^5 + 12u^4 + 3u^3 - 3u^2 - 2u \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** = $-u^9 + u^8 + 4u^7 + 16u^6 + 20u^5 + 28u^4 + 12u^3 + 12u^2 - 3u - 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{10} + 5u^8 + 8u^6 + 3u^4 + 2u^2 + 4$
c_2	$u^{10} - 2u^8 - 2u^7 + u^6 + u^5 + 5u^4 + 2u^3 - 2u^2 - u + 1$
c_3, c_9	$u^{10} + 4u^9 + 11u^8 + 19u^7 + 25u^6 + 21u^5 + 12u^4 + u^3 - 2u^2 - u + 1$
c_4, c_{10}	$u^{10} + 4u^8 + u^6 - 7u^4 - 2u^2 + 4$
c_5, c_8, c_{11}	$u^{10} - 2u^8 + 2u^7 + u^6 - u^5 + 5u^4 - 2u^3 - 2u^2 + u + 1$
c_6	$u^{10} - 4u^9 + 11u^8 - 19u^7 + 25u^6 - 21u^5 + 12u^4 - u^3 - 2u^2 + u + 1$
c_7	$(u^5 - u^4 + 3u^3 + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$(y^5 + 5y^4 + 8y^3 + 3y^2 + 2y + 4)^2$
c_2, c_5, c_8 c_{11}	$y^{10} - 4y^9 + 6y^8 + 2y^7 - 19y^6 + 27y^5 + 9y^4 - 20y^3 + 18y^2 - 5y + 1$
c_3, c_6, c_9	$y^{10} + 6y^9 + \dots - 5y + 1$
c_4, c_{10}	$(y^5 + 4y^4 + y^3 - 7y^2 - 2y + 4)^2$
c_7	$(y^5 + 5y^4 + 9y^3 + 2y^2 - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.731699 + 0.572220I$		
$a = 1.48078 + 0.14546I$	$2.01963 + 4.25086I$	$-7.08888 - 9.27894I$
$b = -1.166730 + 0.740897I$		
$u = -0.731699 - 0.572220I$		
$a = 1.48078 - 0.14546I$	$2.01963 - 4.25086I$	$-7.08888 + 9.27894I$
$b = -1.166730 - 0.740897I$		
$u = -0.344685 + 1.213160I$		
$a = -0.136245 + 0.613767I$	4.38002	$-7.67593 + 0.I$
$b = -0.697636 - 0.376843I$		
$u = -0.344685 - 1.213160I$		
$a = -0.136245 - 0.613767I$	4.38002	$-7.67593 + 0.I$
$b = -0.697636 + 0.376843I$		
$u = -0.23712 + 1.40919I$		
$a = -0.238288 - 0.297862I$	$2.01963 + 4.25086I$	$-7.08888 - 9.27894I$
$b = 0.476249 - 0.265165I$		
$u = -0.23712 - 1.40919I$		
$a = -0.238288 + 0.297862I$	$2.01963 - 4.25086I$	$-7.08888 + 9.27894I$
$b = 0.476249 + 0.265165I$		
$u = -1.04039 + 1.04611I$		
$a = -0.849900 - 0.531699I$	$-4.20964 + 3.82188I$	$-5.57316 - 2.67833I$
$b = 1.44044 - 0.33592I$		
$u = -1.04039 - 1.04611I$		
$a = -0.849900 + 0.531699I$	$-4.20964 - 3.82188I$	$-5.57316 + 2.67833I$
$b = 1.44044 + 0.33592I$		
$u = 0.353890 + 0.196697I$		
$a = 1.24365 + 2.50355I$	$-4.20964 - 3.82188I$	$-5.57316 + 2.67833I$
$b = -0.052327 + 1.130600I$		
$u = 0.353890 - 0.196697I$		
$a = 1.24365 - 2.50355I$	$-4.20964 + 3.82188I$	$-5.57316 - 2.67833I$
$b = -0.052327 - 1.130600I$		

IV.

$$I_4^u = \langle -3u^3 - au - 5u^2 + b - 3u + 4, \ 4u^3a + u^3 + \dots - 5a - 2, \ u^4 + u^3 - 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 3u^3 + au + 5u^2 + 3u - 4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 3u^3 + au + 5u^2 + a + 3u - 4 \\ 3u^3 + au + 5u^2 + 3u - 4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3a - u^2a - u^3 - 2u^2 + a - u + 2 \\ u^3a + 2u^2a + 4u^3 + 7u^2 + 5u - 7 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2u^3a - 3u^2a - u^3 - 2au - 2u^2 + 2a - u + 2 \\ -au + u^2 + a + 2u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -3u^3a - 5u^2a - u^3 - 3au - u^2 + 4a + 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3u^3a - 5u^2a - u^3 - 3au - u^2 + 4a + 2 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -3u^3a - 5u^2a - u^3 - 3au - u^2 + 4a + 3 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^3a - 3u^2a - u^3 - 2au - 3u^2 + 2a - 3u + 1 \\ u^3a + 2u^2a + au - 2u^2 - 2a - u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^3a - 3u^2a - u^3 - 2au - 3u^2 + 2a - 3u + 1 \\ u^3a + 2u^2a + au - 2u^2 - 2a - u - 1 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = $8u^3 + 16u^2 + 8u - 30$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$(u^4 + u^3 + 6u^2 + 4u + 7)^2$
c_2, c_5, c_8 c_{11}	$u^8 + u^7 + u^6 + u^5 - 14u^4 - 11u^3 + 25u^2 + 4u + 1$
c_3, c_6, c_9	$(u^4 + u^3 - 2u + 1)^2$
c_4, c_{10}	$(u - 1)^8$
c_7	$(u^4 + 9u^2 + 6u + 12)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$(y^4 + 11y^3 + 42y^2 + 68y + 49)^2$
c_2, c_5, c_8 c_{11}	$y^8 + y^7 - 29y^6 + 43y^5 + 262y^4 - 827y^3 + 685y^2 + 34y + 1$
c_3, c_6, c_9	$(y^4 - y^3 + 6y^2 - 4y + 1)^2$
c_4, c_{10}	$(y - 1)^8$
c_7	$(y^4 + 18y^3 + 105y^2 + 180y + 144)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.621964 + 0.187730I$		
$a = -0.196231 - 0.222403I$	$-4.93480 - 4.05977I$	$-18.0000 + 6.9282I$
$b = 0.06811 + 2.18939I$		
$u = 0.621964 + 0.187730I$		
$a = -1.07414 - 3.19591I$	$-4.93480 - 4.05977I$	$-18.0000 + 6.9282I$
$b = 0.080297 + 0.175165I$		
$u = 0.621964 - 0.187730I$		
$a = -0.196231 + 0.222403I$	$-4.93480 + 4.05977I$	$-18.0000 - 6.9282I$
$b = 0.06811 - 2.18939I$		
$u = 0.621964 - 0.187730I$		
$a = -1.07414 + 3.19591I$	$-4.93480 + 4.05977I$	$-18.0000 - 6.9282I$
$b = 0.080297 - 0.175165I$		
$u = -1.12196 + 1.05376I$		
$a = -0.740048 - 0.475381I$	$-4.93480 + 4.05977I$	$-18.0000 - 6.9282I$
$b = 1.68284 - 0.47999I$		
$u = -1.12196 + 1.05376I$		
$a = 1.010420 + 0.521174I$	$-4.93480 + 4.05977I$	$-18.0000 - 6.9282I$
$b = -1.331240 + 0.246470I$		
$u = -1.12196 - 1.05376I$		
$a = -0.740048 + 0.475381I$	$-4.93480 - 4.05977I$	$-18.0000 + 6.9282I$
$b = 1.68284 + 0.47999I$		
$u = -1.12196 - 1.05376I$		
$a = 1.010420 - 0.521174I$	$-4.93480 - 4.05977I$	$-18.0000 + 6.9282I$
$b = -1.331240 - 0.246470I$		

$$\mathbf{V. } I_5^u = \langle -au + b + u + 1, a^2 + au - 2u - 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u+1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} a \\ au-u-1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} au+a-u-1 \\ au-u-1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} au+a-u \\ au \end{pmatrix} \\ a_6 &= \begin{pmatrix} 2au+a-u \\ -a+1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} au+a-u-2 \\ 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} au+a-u-1 \\ 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} au+a-u \\ 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 2au+a-2u \\ au+u+1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 2au+a-2u \\ au+u+1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-8u - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^4 - 3u^3 + 4u^2 + 1$
c_2, c_5, c_8 c_{11}	$u^4 - u^3 - 2u^2 + 3$
c_3, c_6, c_9	$(u^2 + u + 1)^2$
c_4, c_7, c_{10}	$(u - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^4 - y^3 + 18y^2 + 8y + 1$
c_2, c_5, c_8 c_{11}	$y^4 - 5y^3 + 10y^2 - 12y + 9$
c_3, c_6, c_9	$(y^2 + y + 1)^2$
c_4, c_7, c_{10}	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 1.085370 + 0.474096I$	$-1.64493 + 4.05977I$	$-6.00000 - 6.92820I$
$b = -1.45326 - 0.16311I$		
$u = -0.500000 + 0.866025I$		
$a = -0.58537 - 1.34012I$	$-1.64493 + 4.05977I$	$-6.00000 - 6.92820I$
$b = 0.953264 - 0.702911I$		
$u = -0.500000 - 0.866025I$		
$a = 1.085370 - 0.474096I$	$-1.64493 - 4.05977I$	$-6.00000 + 6.92820I$
$b = -1.45326 + 0.16311I$		
$u = -0.500000 - 0.866025I$		
$a = -0.58537 + 1.34012I$	$-1.64493 - 4.05977I$	$-6.00000 + 6.92820I$
$b = 0.953264 + 0.702911I$		

$$\text{VI. } I_6^u = \langle b - 2, a + 1, u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2 \\ 5 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -3 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -18

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_6 c_9	$u + 1$
c_2, c_5, c_8	$u + 2$
c_4, c_{10}, c_{11}	$u - 1$
c_7	$u + 3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_4 c_6, c_9, c_{10} c_{11}	$y - 1$
c_2, c_5, c_8	$y - 4$
c_7	$y - 9$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = -1.00000$	-4.93480	-18.0000
$b = 2.00000$		

$$\text{VII. } I_7^u = \langle b+1, a-2, u+1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -4 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -18

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_6 c_9	$u + 1$
c_2, c_4, c_5 c_8, c_{10}	$u - 1$
c_7	u
c_{11}	$u + 2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_4, c_5, c_6 c_8, c_9, c_{10}	$y - 1$
c_7	y
c_{11}	$y - 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 2.00000$	-4.93480	-18.0000
$b = -1.00000$		

VIII. $I_8^u = \langle b - 1, a + 1, u + 1 \rangle$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** = -12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4, c_{10}	u
c_2, c_6	$u - 1$
c_3, c_5, c_7 c_8, c_9, c_{11}	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4, c_{10}	y
c_2, c_3, c_5 c_6, c_7, c_8 c_9, c_{11}	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_8^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = -1.00000$	-3.28987	-12.0000
$b = 1.00000$		

$$\text{IX. } I_1^v = \langle a, b - 1, v - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_4 c_5, c_7, c_8 c_{10}, c_{11}	$u + 1$
c_3, c_6, c_9	u

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_5, c_7, c_8 c_{10}, c_{11}	$y - 1$
c_3, c_6, c_9	y

(vi) Complex Volumes and Cusp Shapes

	Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v =$	1.00000		
$a =$	0	-1.64493	-6.00000
$b =$	1.00000		

X. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$u(u+1)^3(u^4 - 3u^3 + 4u^2 + 1)(u^4 + u^3 + 6u^2 + 4u + 7)^2$ $\cdot (u^5 + 2u^3 - 2u^2 - u + 1)^2$ $\cdot (u^8 - u^7 + 9u^6 - 4u^5 + 26u^4 - 2u^3 + 28u^2 + 10)$ $\cdot (u^{10} + 5u^8 + 8u^6 + 3u^4 + 2u^2 + 4)$
c_2	$(u-1)^2(u+1)(u+2)(u^4 - u^3 - 2u^2 + 3)$ $\cdot (u^8 - u^7 - 4u^6 + 5u^5 + 4u^4 - 3u^3 + 4u^2 - u + 1)$ $\cdot (u^8 + u^7 + u^6 + u^5 - 14u^4 - 11u^3 + 25u^2 + 4u + 1)$ $\cdot (u^{10} - 2u^8 - 2u^7 + u^6 + u^5 + 5u^4 + 2u^3 - 2u^2 - u + 1)$ $\cdot (u^{10} - u^9 - 6u^8 + 6u^7 + 15u^6 - 19u^5 - 10u^4 + 17u^3 - u + 1)$
c_3, c_9	$u(u+1)^3(u^2 + u + 1)^2(u^4 + u^3 - 2u + 1)^2$ $\cdot (u^8 - 3u^7 + 6u^6 - 5u^5 + 4u^4 + u^3 + 3u + 3)$ $\cdot (u^{10} - 5u^9 + 13u^8 - 22u^7 + 30u^6 - 33u^5 + 25u^4 - 6u^3 - 6u^2 + 5u - 1)$ $\cdot (u^{10} + 4u^9 + 11u^8 + 19u^7 + 25u^6 + 21u^5 + 12u^4 + u^3 - 2u^2 - u + 1)$
c_4, c_{10}	$u(u-1)^{14}(u+1)(u^5 + 4u^4 + 9u^3 + 11u^2 + 10u + 4)^2$ $\cdot (u^8 + 6u^7 + 20u^6 + 42u^5 + 68u^4 + 82u^3 + 74u^2 + 32u + 8)$ $\cdot (u^{10} + 4u^8 + u^6 - 7u^4 - 2u^2 + 4)$
c_5, c_8, c_{11}	$(u-1)(u+1)^2(u+2)(u^4 - u^3 - 2u^2 + 3)$ $\cdot (u^8 - u^7 - 4u^6 + 5u^5 + 4u^4 - 3u^3 + 4u^2 - u + 1)$ $\cdot (u^8 + u^7 + u^6 + u^5 - 14u^4 - 11u^3 + 25u^2 + 4u + 1)$ $\cdot (u^{10} - 2u^8 + 2u^7 + u^6 - u^5 + 5u^4 - 2u^3 - 2u^2 + u + 1)$ $\cdot (u^{10} - u^9 - 6u^8 + 6u^7 + 15u^6 - 19u^5 - 10u^4 + 17u^3 - u + 1)$
c_6	$u(u-1)(u+1)^2(u^2 + u + 1)^2(u^4 + u^3 - 2u + 1)^2$ $\cdot (u^8 - 3u^7 + 6u^6 - 5u^5 + 4u^4 + u^3 + 3u + 3)$ $\cdot (u^{10} - 5u^9 + 13u^8 - 22u^7 + 30u^6 - 33u^5 + 25u^4 - 6u^3 - 6u^2 + 5u - 1)$ $\cdot (u^{10} - 4u^9 + 11u^8 - 19u^7 + 25u^6 - 21u^5 + 12u^4 - u^3 - 2u^2 + u + 1)$
c_7	$u(u-1)^4(u+1)^2(u+3)(u^4 + 9u^2 + 6u + 12)^2(u^5 - u^4 + 3u^3 + 1)^2$ $\cdot (u^5 - u^4 + 5u^3 - 2u^2 - 2u + 3)^2$ $\cdot (u^8 + 2u^7 + 9u^6 + 10u^5 + 31u^4 + 30u^3 + 27u^2 + 26u + 12)$

XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$y(y - 1)^3(y^4 - y^3 + 18y^2 + 8y + 1)(y^4 + 11y^3 + 42y^2 + 68y + 49)^2$ $\cdot (y^5 + 4y^4 + 2y^3 - 8y^2 + 5y - 1)^2(y^5 + 5y^4 + 8y^3 + 3y^2 + 2y + 4)^2$ $\cdot (y^8 + 17y^7 + \dots + 560y + 100)$
c_2, c_5, c_8 c_{11}	$(y - 4)(y - 1)^3(y^4 - 5y^3 + 10y^2 - 12y + 9)$ $\cdot (y^8 - 9y^7 + 34y^6 - 55y^5 + 14y^4 + 25y^3 + 18y^2 + 7y + 1)$ $\cdot (y^8 + y^7 - 29y^6 + 43y^5 + 262y^4 - 827y^3 + 685y^2 + 34y + 1)$ $\cdot (y^{10} - 13y^9 + \dots - y + 1)$ $\cdot (y^{10} - 4y^9 + 6y^8 + 2y^7 - 19y^6 + 27y^5 + 9y^4 - 20y^3 + 18y^2 - 5y + 1)$
c_3, c_6, c_9	$y(y - 1)^3(y^2 + y + 1)^2(y^4 - y^3 + 6y^2 - 4y + 1)^2$ $\cdot (y^8 + 3y^7 + 14y^6 + 29y^5 + 50y^4 + 65y^3 + 18y^2 - 9y + 9)$ $\cdot (y^{10} + y^9 + 9y^8 + 16y^7 + 26y^6 + 39y^5 + 63y^4 - 66y^3 + 46y^2 - 13y + 1)$ $\cdot (y^{10} + 6y^9 + \dots - 5y + 1)$
c_4, c_{10}	$y(y - 1)^{15}(y^5 + 2y^4 + 13y^3 + 27y^2 + 12y - 16)^2$ $\cdot (y^5 + 4y^4 + y^3 - 7y^2 - 2y + 4)^2$ $\cdot (y^8 + 4y^7 + 32y^6 + 120y^5 + 328y^4 + 972y^3 + 1316y^2 + 160y + 64)$
c_7	$y(y - 9)(y - 1)^6(y^4 + 18y^3 + 105y^2 + 180y + 144)^2$ $\cdot (y^5 + 5y^4 + 9y^3 + 2y^2 - 1)^2(y^5 + 9y^4 + 17y^3 - 18y^2 + 16y - 9)^2$ $\cdot (y^8 + 14y^7 + 103y^6 + 392y^5 + 767y^4 + 470y^3 - 87y^2 - 28y + 144)$